

V_{cb} and V_{ub} CKM Matrix Elements

OMITTED FROM SUMMARY TABLE

See the related review(s):
[Semileptonic \$B\$ Hadron Decays, Determination of \$V_{cb}\$ and \$V_{ub}\$](#)

V_{cb} MEASUREMENTS

For the discussion of V_{cb} measurements, which is not repeated here, see the review on “Determination of $|V_{cb}|$ and $|V_{ub}|$.”

The CKM matrix element $|V_{cb}|$ can be determined by studying the rate of the semileptonic decay $B \rightarrow D^{(*)} \ell \nu$ as a function of the recoil kinematics of $D^{(*)}$ mesons. Taking advantage of theoretical constraints on the normalization and a linear ω dependence of the form factors ($F(\omega)$, $G(\omega)$) provided by Heavy Quark Effective Theory (HQET), the $|V_{cb}| \times F(\omega)$ and ρ^2 can be simultaneously extracted from data, where ω is the scalar product of the two-meson four velocities, $F(1)$ is the form factor at zero recoil ($\omega=1$) and ρ^2 is the slope. Using the theoretical input of $F(1)$, a value of $|V_{cb}|$ can be obtained.

$|V_{cb}| \times F(1)$ (from $B^0 \rightarrow D^{*-} \ell^+ \nu$)

| VALUE (units 10^{-2}) | DOCUMENT ID | TECN | COMMENT |
|---|------------------------|------|--|
| 3.522±0.037 OUR EVALUATION (Produced by HFLAV) with $\rho^2=1.139 \pm 0.020$ and a correlation 0.268. The fitted χ^2 is 63.2 for 27 degrees of freedom. | | | |
| 3.62 ±0.05 OUR AVERAGE Error includes scale factor of 1.6. See the ideogram below. | | | |
| 3.66 ±0.05 | ¹ PRIM | 24 | BELL $e^+ e^- \rightarrow \Upsilon(4S)$ |
| 3.676±0.028±0.086 | ² ADACHI | 23J | BEL2 $e^+ e^- \rightarrow \Upsilon(4S)$ |
| 3.506±0.015±0.056 | ³ WAHEED | 21 | BELL $e^+ e^- \rightarrow \Upsilon(4S)$ |
| 3.59 ±0.02 ±0.12 | ⁴ AUBERT | 09A | BABR $e^+ e^- \rightarrow \Upsilon(4S)$ |
| 3.92 ±0.18 ±0.23 | ⁵ ABDALLAH | 04D | DLPH $e^+ e^- \rightarrow Z^0$ |
| 4.31 ±0.13 ±0.18 | ⁶ ADAM | 03 | CLE2 $e^+ e^- \rightarrow \Upsilon(4S)$ |
| 3.55 ±0.14 ^{+0.23} _{−0.24} | ⁷ ABREU | 01H | DLPH $e^+ e^- \rightarrow Z$ |
| 3.71 ±0.10 ±0.20 | ⁸ ABBIENDI | 00Q | OPAL $e^+ e^- \rightarrow Z$ |
| 3.19 ±0.18 ±0.19 | ⁹ BUSKULIC | 97 | ALEP $e^+ e^- \rightarrow Z$ |
| ● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ● | | | |
| 3.64 ±0.09 | ¹⁰ PRIM | 23 | BELL $e^+ e^- \rightarrow \Upsilon(4S)$, Repl. by PRIM 24 |
| 3.483±0.015±0.056 | ³ WAHEED | 19 | BELL Repl. by WAHEED 21 |
| 3.46 ±0.02 ±0.10 | ¹¹ DUNGEL | 10 | BELL Rep. by WAHEED 19 |
| 3.59 ±0.06 ±0.14 | ¹² AUBERT | 08AT | BABR Repl. by AUBERT 09A |
| 3.44 ±0.03 ±0.11 | ¹³ AUBERT | 08R | BABR Repl. by AUBERT 09A |
| 3.55 ±0.03 ±0.16 | ¹⁴ AUBERT | 05E | BABR Repl. by AUBERT 08R |
| 3.77 ±0.11 ±0.19 | ¹⁵ ABDALLAH | 04D | DLPH $e^+ e^- \rightarrow Z^0$ |
| 3.54 ±0.19 ±0.18 | ¹⁶ ABE | 02F | BELL Repl. by DUNGEL 10 |

| | | | |
|----------------------------|------------|----------|-----------------------------------|
| 4.31 ± 0.13 ± 0.18 | 17 BRIERE | 02 CLE2 | $e^+e^- \rightarrow \Upsilon(4S)$ |
| 3.28 ± 0.19 ± 0.22 | ACKERSTAFF | 97G OPAL | Repl. by ABBIENDI 00Q |
| 3.50 ± 0.19 ± 0.23 | 18 ABREU | 96P DLPH | Repl. by ABREU 01H |
| 3.51 ± 0.19 ± 0.20 | 19 BARISH | 95 CLE2 | Repl. by ADAM 03 |
| 3.14 ± 0.23 ± 0.25 | BUSKULIC | 95N ALEP | Repl. by BUSKULIC 97 |

¹ PRIM 24 value established from a complete set of angular coefficients for exclusive $B \rightarrow \bar{D}^* \ell^+ \nu_\ell$ decays with hadronic tag-side reconstruction. The $|V_{cb}| \times F(1)$ is derived from the extracted the BGL and CNL form factor parameters: $|V_{cb}|_{\text{BGL}} = (40.7 \pm 0.7) \times 10^{-3}$ with the zero-recoil lattice QCD point $F(1) = 0.900 \pm 0.009$ and $|V_{cb}|_{\text{CNL}} = (40.3 \pm 0.6) \times 10^{-3}$.

² ADACHI 23J result comes from differential shapes of exclusive $B \rightarrow D^* \ell^- \nu_\ell$ ($\ell = e$ or μ) decays. Using CNL form factor parametrization and the zero-recoil lattice QCD point $F(1) = 0.906 \pm 0.013$ ADACHI 23J finds $|V_{cb}|_{\text{CNL}} = (40.57 \pm 0.31 \pm 0.95 \pm 0.58) \times 10^{-3}$ where the last uncertainty is due to the prediction of $F(1)$. Also reports a measurement of $|V_{cb}|_{\text{BGL}} = (40.13 \pm 0.27 \pm 0.93 \pm 0.58) \times 10^{-3}$ using BGL form factors parametrization.

³ WAHEED 21 uses fully reconstructed $D^{*-} \ell^+ \nu$ events ($\ell = e$ or μ) and $\eta_{EW} = 1.0066$.

⁴ Obtained from a global fit to $B \rightarrow D^{(*)} \ell \nu_\ell$ events, with reconstructed $D^0 \ell$ and $D^+ \ell$ final states and $\rho^2 = 1.22 \pm 0.02 \pm 0.07$.

⁵ Measurement using fully reconstructed D^* sample with a $\rho^2 = 1.32 \pm 0.15 \pm 0.33$.

⁶ Average of the $B^0 \rightarrow D^*(2010)^- \ell^+ \nu$ and $B^+ \rightarrow \bar{D}^*(2007) \ell^+ \nu$ modes with $\rho^2 = 1.61 \pm 0.09 \pm 0.21$ and $f_{+-} = 0.521 \pm 0.012$.

⁷ ABREU 01H measured using about 5000 partial reconstructed D^* sample with a $\rho^2 = 1.34 \pm 0.14^{+0.24}_{-0.22}$.

⁸ ABBIENDI 00Q: measured using both inclusively and exclusively reconstructed $D^{*\pm}$ samples with a $\rho^2 = 1.21 \pm 0.12 \pm 0.20$. The statistical and systematic correlations between $|V_{cb}| \times F(1)$ and ρ^2 are 0.90 and 0.54 respectively.

⁹ BUSKULIC 97: measured using exclusively reconstructed $D^{*\pm}$ with a $a^2 = 0.31 \pm 0.17 \pm 0.08$. The statistical correlation is 0.92.

¹⁰ Measured from differential shapes of exclusive $B \rightarrow D^* \ell^- \nu_\ell$ decays with hadronic tag-side reconstruction and extracting the CNL and BGL form factor parameters. PRIM 23 finds $|V_{cb}|_{\text{CNL}} = (40.2 \pm 0.9) \times 10^{-3}$ with the zero-recoil lattice QCD point $F(1) = 0.906 \pm 0.013$. PRIM 23 provides also a measurement of $|V_{cb}|_{\text{BGL}} = (40.7 \pm 1.0) \times 10^{-3}$.

¹¹ Uses fully reconstructed $D^{*-} \ell^+ \nu$ events ($\ell = e$ or μ).

¹² Measured using the dependence of $B^- \rightarrow D^{*0} e^- \bar{\nu}_e$ decay differential rate and the form factor description by CAPRINI 98 with $\rho^2 = 1.16 \pm 0.06 \pm 0.08$.

¹³ Measured using fully reconstructed D^* sample and a simultaneous fit to the Caprini-Lellouch-Neubert form factor parameters: $\rho^2 = 1.191 \pm 0.048 \pm 0.028$, $R_1(1) = 1.429 \pm 0.061 \pm 0.044$, and $R_2(1) = 0.827 \pm 0.038 \pm 0.022$.

¹⁴ Measurement using fully reconstructed D^* sample with a $\rho^2 = 1.29 \pm 0.03 \pm 0.27$.

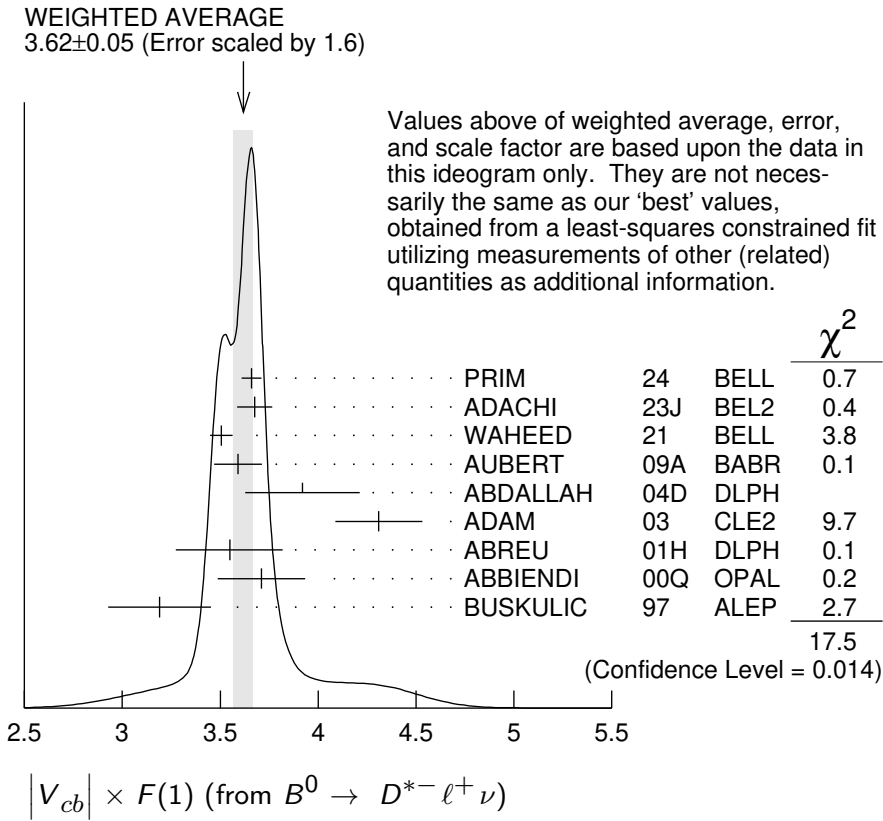
¹⁵ Combines with previous partial reconstructed D^* measurement with a $\rho^2 = 1.39 \pm 0.10 \pm 0.33$.

¹⁶ Measured using exclusive $B^0 \rightarrow D^*(892)^- e^+ \nu$ decays with $\rho^2 = 1.35 \pm 0.17 \pm 0.19$ and a correlation of 0.91.

¹⁷ BRIERE 02 result is based on the same analysis and data sample reported in ADAM 03.

¹⁸ ABREU 96P: measured using both inclusively and exclusively reconstructed $D^{*\pm}$ samples.

¹⁹ BARISH 95: measured using both exclusive reconstructed $B^0 \rightarrow D^{*-} \ell^+ \nu$ and $B^+ \rightarrow D^{*0} \ell^+ \nu$ samples. They report their experiment's uncertainties $\pm 0.0019 \pm 0.0018 \pm 0.0008$, where the first error is statistical, the second is systematic, and the third is the uncertainty in the lifetimes. We combine the last two in quadrature.



$|V_{cb}| \times G(1)$ (from $B \rightarrow D^- \ell^+ \nu$)

VALUE (units 10^{-2}) DOCUMENT ID TECN COMMENT

4.121±0.100 OUR EVALUATION (Produced by HFLAV) with $\rho^2=1.128 \pm 0.033$ and a correlation 0.747. The fitted χ^2 is 4.8 for 8 degrees of freedom.

4.17 ±0.08 OUR AVERAGE

| | | | | |
|---|------------------------|-----|------|------------------------------------|
| 4.109±0.116 | ¹ LEES | 24 | BABR | $e^+ e^- \rightarrow \Upsilon(4S)$ |
| 4.229±0.137 | ² GLATTAUER | 16 | BELL | $e^+ e^- \rightarrow \Upsilon(4S)$ |
| 4.23 ±0.19 ±0.14 | ³ AUBERT | 10 | BABR | $e^+ e^- \rightarrow \Upsilon(4S)$ |
| 4.31 ±0.08 ±0.23 | ⁴ AUBERT | 09A | BABR | $e^+ e^- \rightarrow \Upsilon(4S)$ |
| 4.16 ±0.47 ±0.37 | ⁵ BARTELT | 99 | CLE2 | $e^+ e^- \rightarrow \Upsilon(4S)$ |
| 2.78 ±0.68 ±0.65 | ⁶ BUSKULIC | 97 | ALEP | $e^+ e^- \rightarrow Z$ |
| ● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ● | | | | |
| 4.11 ±0.44 ±0.52 | ⁷ ABE | 02E | BELL | Repl. by GLATTAUER 16 |
| 3.37 ±0.44 ^{+0.72} _{-0.49} | ⁸ ATHANAS | 97 | CLE2 | Repl. by BARTELT 99 |

¹ Obtained from a 2D fit to the combined $B \rightarrow \bar{D} \ell^+ \nu_\ell$ sample with a model-independent parametrization according to Boyd-Grinstein-Lebed (BGL), in which a hadronic decay of the second B meson is fully reconstructed.

² Obtained from a fit to the combined partially reconstructed $B \rightarrow \bar{D} \ell \nu_\ell$ sample while tagged by the other fully reconstructed B meson in the event. Also reports fitted $\rho^2 = 1.09 \pm 0.05$.

³ Obtained from a fit to the combined $B \rightarrow \bar{D} \ell^+ \nu_\ell$ sample in which a hadronic decay of the second B meson is fully reconstructed and $\rho^2 = 1.20 \pm 0.09 \pm 0.04$.

⁴ Obtained from a global fit to $B \rightarrow D^{(*)} \ell \nu_\ell$ events, with reconstructed $D^0 \ell$ and $D^+ \ell$ final states and $\rho^2 = 1.20 \pm 0.04 \pm 0.07$.

- ⁵ BARTELT 99: measured using both exclusive reconstructed $B^0 \rightarrow D^- \ell^+ \nu$ and $B^+ \rightarrow D^0 \ell^+ \nu$ samples.
- ⁶ BUSKULIC 97: measured using exclusively reconstructed D^\pm with a $a^2 = -0.05 \pm 0.53 \pm 0.38$. The statistical correlation is 0.99.
- ⁷ Using the missing energy and momentum to extract kinematic information about the undetected neutrino in the $B^0 \rightarrow D^- \ell^+ \nu$ decay.
- ⁸ ATHANAS 97: measured using both exclusive reconstructed $B^0 \rightarrow D^- \ell^+ \nu$ and $B^+ \rightarrow D^0 \ell^+ \nu$ samples with a $\rho^2 = 0.59 \pm 0.22 \pm 0.12^{+0.59}_{-0}$. They report their experiment's uncertainties $\pm 0.0044 \pm 0.0048^{+0.0053}_{-0.0012}$, where the first error is statistical, the second is systematic, and the third is the uncertainty due to the form factor model variations. We combine the last two in quadrature.

$|V_{cb}|$ (from $D_s^{*-} \mu^+ \nu_\mu$)

| VALUE (units 10^{-3}) | DOCUMENT ID | TECN | COMMENT |
|--|-------------------|------|-----------------------|
| $41.4 \pm 0.6 \pm 0.9 \pm 1.2$ | ¹ AAIJ | 20E | LHCB pp at 7, 8 TeV |

- ¹ Measured from an inclusive sample of $D_s^- \mu^+$ candidates using CNL parameterization of the form factor. AAIJ 20E provides also measurement of $|V_{cb}| = (42.3 \pm 0.8 \pm 0.9 \pm 1.2) \times 10^{-3}$ using BGL parameterization of the form factor. The third uncertainty is due to the external inputs used in the measurement.

V_{ub} MEASUREMENTS

For the discussion of V_{ub} measurements, which is not repeated here, see the review on "Determination of $|V_{cb}|$ and $|V_{ub}|$."

The CKM matrix element $|V_{ub}|$ can be determined by studying the rate of the charmless semileptonic decay $b \rightarrow u \ell \nu$. The relevant branching ratio measurements based on exclusive and inclusive decays can be found in the B Listings, and are not repeated here.

V_{cb} and V_{ub} CKM Matrix Elements REFERENCES

| | | | | |
|------------|------|----------------|-------------------------------------|--------------------|
| LEES | 24 | PR D110 032018 | J.P. Lees <i>et al.</i> | (BABAR Collab.) |
| PRIM | 24 | PRL 133 131801 | M.T. Prim <i>et al.</i> | (BELLE Collab.) |
| ADACHI | 23J | PR D108 092013 | I. Adachi <i>et al.</i> | (BELLE II Collab.) |
| PRIM | 23 | PR D108 012002 | M.T. Prim <i>et al.</i> | (BELLE Collab.) |
| WAHEED | 21 | PR D103 079901 | E. Waheed <i>et al.</i> | (BELLE Collab.) |
| AAIJ | 20E | PR D101 072004 | R. Aaij <i>et al.</i> | (LHCb Collab.) |
| WAHEED | 19 | PR D100 052007 | E. Waheed <i>et al.</i> | (BELLE Collab.) |
| GLATTAUER | 16 | PR D93 032006 | R. Glattauer <i>et al.</i> | (BELLE Collab.) |
| AUBERT | 10 | PRL 104 011802 | B. Aubert <i>et al.</i> | (BABAR Collab.) |
| DUNGEL | 10 | PR D82 112007 | W. Dungen <i>et al.</i> | (BELLE Collab.) |
| AUBERT | 09A | PR D79 012002 | B. Aubert <i>et al.</i> | (BABAR Collab.) |
| AUBERT | 08AT | PRL 100 231803 | B. Aubert <i>et al.</i> | (BABAR Collab.) |
| AUBERT | 08R | PR D77 032002 | B. Aubert <i>et al.</i> | (BABAR Collab.) |
| AUBERT | 05E | PR D71 051502 | B. Aubert <i>et al.</i> | (BABAR Collab.) |
| ABDALLAH | 04D | EPJ C33 213 | J. Abdallah <i>et al.</i> | (DELPHI Collab.) |
| ADAM | 03 | PR D67 032001 | N.E. Adam <i>et al.</i> | (CLEO Collab.) |
| ABE | 02E | PL B526 258 | K. Abe <i>et al.</i> | (BELLE Collab.) |
| ABE | 02F | PL B526 247 | K. Abe <i>et al.</i> | (BELLE Collab.) |
| BRIERE | 02 | PRL 89 081803 | R. Briere <i>et al.</i> | (CLEO Collab.) |
| ABREU | 01H | PL B510 55 | P. Abreu <i>et al.</i> | (DELPHI Collab.) |
| ABBIENDI | 00Q | PL B482 15 | G. Abbiendi <i>et al.</i> | (OPAL Collab.) |
| BARTELT | 99 | PRL 82 3746 | J. Bartelt <i>et al.</i> | (CLEO Collab.) |
| CAPRINI | 98 | NP B530 153 | I. Caprini, L. Lellouch, M. Neubert | (BCIP, CERN) |
| ACKERSTAFF | 97G | PL B395 128 | K. Akerstaff <i>et al.</i> | (OPAL Collab.) |
| ATHANAS | 97 | PRL 79 2208 | M. Athanas <i>et al.</i> | (CLEO Collab.) |
| BUSKULIC | 97 | PL B395 373 | D. Buskulic <i>et al.</i> | (ALEPH Collab.) |
| ABREU | 96P | ZPHY C71 539 | P. Abreu <i>et al.</i> | (DELPHI Collab.) |

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|----------|-----|-------------|---------------------------|-----------------|
| BARISH | 95 | PR D51 1014 | B.C. Barish <i>et al.</i> | (CLEO Collab.) |
| BUSKULIC | 95N | PL B359 236 | D. Buskulic <i>et al.</i> | (ALEPH Collab.) |
