V_{cb} and V_{ub} CKM Matrix Elements

OMITTED FROM SUMMARY TABLE

See the related review(s):

Semileptonic B Hadron Decays, Determination of V_{cb} and V_{ub}

V_{cb} MEASUREMENTS

For the discussion of V_{cb} measurements, which is not repeated here, see the review on "Determination of $|V_{cb}|$ and $|V_{ub}|$."

The CKM matrix element $|V_{cb}|$ can be determined by studying the rate of the semileptonic decay $B \to D^{(*)} \ell \nu$ as a function of the recoil kinematics of $D^{(*)}$ mesons. Taking advantage of theoretical constraints on the normalization and a linear ω dependence of the form factors $(F(\omega), G(\omega))$ provided by Heavy Quark Effective Theory (HQET), the $|V_{cb}| \times F(\omega)$ and ρ^2 can be simultaneously extracted from data, where ω is the scalar product of the two-meson four velocities, F(1) is the form factor at zero recoil $(\omega=1)$ and ρ^2 is the slope. Using the theoretical input of F(1), a value of $|V_{cb}|$ can be obtained.

"OUR EVALUATION" is an average using rescaled values of the data listed below. The average and rescaling were performed by the Heavy Flavor Averaging Group (HFLAV) and are described at https://hflav.web.cern.ch/. The averaging/rescaling procedure takes into account correlations between the measurements.

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|V_{cb}| \times F(1) (from B^0 \rightarrow D^{*-}\ell^+\nu)
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VALUE (units 10⁻²) DOCUMENT ID TECN COMMENT

3.500 \pm 0.036 OUR EVALUATION with ρ^2 =1.121 \pm 0.024 and a correlation 0.317. The fitted χ^2 is 42.2 for 23 degrees of freedom.

3.57 \pm **0.08 OUR AVERAGE** Error includes scale factor of 1.6. See the ideogram below.

```
<sup>1</sup> WAHEED
3.506 \pm 0.015 \pm 0.056
                                                                          BELL e^+e^- \rightarrow \Upsilon(4S)
                                            <sup>2</sup> AUBERT
                                                                   09A BABR e^+e^- \rightarrow \Upsilon(4S)
3.59 \pm 0.02 \pm 0.12
                                                                   04D DLPH e^+e^- \rightarrow Z^0
3.92 \pm 0.18 \pm 0.23
                                            <sup>3</sup> ABDALLAH
4.31 \pm 0.13 \pm 0.18
                                            <sup>4</sup> ADAM
                                                                          CLE2
3.55 \ \pm 0.14 \ ^{+\, 0.23}_{-\, 0.24}
                                            <sup>5</sup> ABREU
                                                                   01H DLPH e^+e^- \rightarrow Z
                                            <sup>6</sup> ABBIENDI
                                                                   00Q OPAL e^+e^-
3.71 \pm 0.10 \pm 0.20
                                            <sup>7</sup> BUSKULIC
                                                                          ALEP
3.19 \pm 0.18 \pm 0.19
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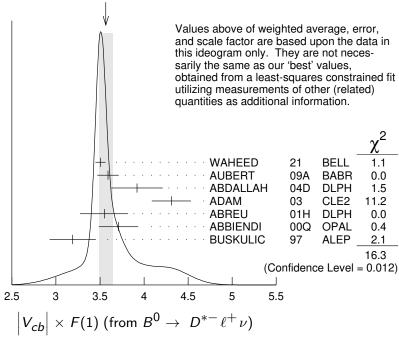
• • We do not use the following data for averages, fits, limits, etc.

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<sup>1</sup> WAHEED
3.483 \pm 0.015 \pm 0.056
                                                             BELL
                                                                      Repl. by WAHEED 21
                                    <sup>8</sup> DUNGEL
3.46 \pm 0.02 \pm 0.10
                                                             BELL
                                                                      Rep. by WAHEED 19
                                    <sup>9</sup> AUBERT
3.59 \pm 0.06 \pm 0.14
                                                       08AT BABR Repl. by AUBERT 09A
                                   <sup>10</sup> AUBERT
3.44 \pm 0.03 \pm 0.11
                                                       08R BABR Repl. by AUBERT 09A
                                   <sup>11</sup> AUBERT
3.55 \pm 0.03 \pm 0.16
                                                       05E BABR Repl. by AUBERT 08R
                                   <sup>12</sup> ABDALLAH
                                                       04D DLPH e^+e^- \rightarrow Z^0
3.77 \pm 0.11 \pm 0.19
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$3.54 \pm 0.19 \pm 0.18$			02F	BELL	Repl. by DUNGEL 10
$4.31 \pm 0.13 \pm 0.18$	3	^{L4} BRIERE	02	CLE2	$e^+e^- ightarrow ~ \varUpsilon(4S)$
$3.28 \pm 0.19 \pm 0.22$					Repl. by ABBIENDI 00Q
$3.50 \pm 0.19 \pm 0.23$			96 P	DLPH	Repl. by ABREU 01H
$3.51 \pm 0.19 \pm 0.20$) 1	^{l6} BARISH	95	CLE2	Repl. by ADAM 03
$3.14 \pm 0.23 \pm 0.25$;	BUSKULIC	95N	ALEP	Repl. by BUSKULIC 97

WEIGHTED AVERAGE 3.57±0.08 (Error scaled by 1.6)



- 1 WAHEED 21 uses fully reconstructed $\mathit{D^{*-}}\,\ell^{+}\,\nu$ events ($\ell=\mathit{e}$ or μ) and $\eta_{EW}=$ 1.0066.
- ²Obtained from a global fit to $B \to D^{(*)} \ell \nu_{\ell}$ events, with reconstructed $D^{0} \ell$ and $D^{+} \ell$ final states and $\rho^2=1.22\pm0.02\pm0.07$.
- ³ Measurement using fully reconstructed D^* sample with a $\rho^2=1.32\pm0.15\pm0.33$. ⁴ Average of the $B^0\to D^*(2010)^-\ell^+\nu$ and $B^+\to \overline{D}^*(2007))\ell^+\nu$ modes with $\rho^2=1.61\pm0.09\pm0.21$ and $f_{+-}=0.521\pm0.012$.
- 5 ABREU 01H measured using about 5000 partial reconstructed D^{st} sample with a $\rho^2 = 1.34 \pm 0.14 + 0.24$
- 6 ABBIENDI 00Q: measured using both inclusively and exclusively reconstructed $D^{*\pm}$ samples with a $ho^2=1.21\pm0.12\pm0.20$. The statistical and systematic correlations between $|V_{cb}| \times F(1)$ and ρ^2 are 0.90 and 0.54 respectively.
- 7 BUSKULIC 97: measured using exclusively reconstructed $D^{*\pm}$ with a a^2 =0.31 \pm 0.17 \pm
- 0.08. The statistical correlation is 0.92. 8 Uses fully reconstructed $D^{*-}\ell^+\nu$ events ($\ell=e$ or μ). 9 Measured using the dependence of $B^-\to D^{*0}e^-\overline{\nu}_e$ decay differential rate and the form factor description by CAPRINI 98 with $\rho^2 = 1.16 \pm 0.06 \pm 0.08$.
- 10 Measured using fully reconstructed D^{st} sample and a simultaneous fit to the Caprini-Lellouch-Neubert form factor parameters: $\rho^2=1.191\pm0.048\pm0.028$, $R_1(1)=1.429\pm0.061\pm0.044$, and $R_2(1)=0.827\pm0.038\pm0.022$.
- 11 Measurement using fully reconstructed D^* sample with a $ho^2=1.29\pm0.03\pm0.27.$
- 12 Combines with previous partial reconstructed D^* measurement with a $ho^2=1.39\pm0.10\pm$

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- ¹³ Measured using exclusive $B^0 \rightarrow D^*(892)^- e^+ \nu$ decays with $\rho^2 = 1.35 \pm 0.17 \pm 0.19$ and a correlation of 0.91.
- 14 BRIERE 02 result is based on the same analysis and data sample reported in ADAM 03.
- 15 ABREU 96P: measured using both inclusively and exclusively reconstructed $D^{*\pm}$ samples.
- ¹⁶ BARISH 95: measured using both exclusive reconstructed $B^0 \to D^{*-} \ell^+ \nu$ and $B^+ \to D^{*-} \ell^+ \nu$ $D^{*0}\ell^+
 u$ samples. They report their experiment's uncertainties $\pm 0.0019\pm 0.0018\pm 0.0019$ 0.0008, where the first error is statistical, the second is systematic, and the third is the uncertainty in the lifetimes. We combine the last two in quadrature.

$|V_{cb}| \times G(1) \text{ (from } B \rightarrow D^- \ell^+ \nu)$

 \underline{VALUE} $\underline{DOCUMENT\ ID}$ \underline{TECN} $\underline{COMMENT}$ 0.04153 \pm 0.00098 OUR EVALUATION with ρ^2 =1.129 \pm 0.033 and a correlation 0.758. The fitted χ^2 is 4.6 for 8 degrees of freedom.

0.0422 ±0.0010 OUR AVERAGE

0.04229 ± 0.00137	$^{ m 1}$ GLATTAUER	16	BELL	$e^+e^- \rightarrow$	$\Upsilon(4S)$
$0.0423\ \pm0.0019\ \pm0.0014$	² AUBERT	10	BABR	$e^+e^- \rightarrow$	$\Upsilon(4S)$
$0.0431\ \pm0.0008\ \pm0.0023$	³ AUBERT	09A	BABR	$e^+e^- \rightarrow$	$\Upsilon(4S)$
$0.0416\ \pm0.0047\ \pm0.0037$	⁴ BARTELT	99	CLE2	$e^+e^- \rightarrow$	$\Upsilon(4S)$
$0.0278 \pm 0.0068 \pm 0.0065$	⁵ BUSKULIC	97	ALEP	$e^+e^- ightarrow$	Z

• We do not use the following data for averages, fits, limits, etc.

$$0.0411 \pm 0.0044 \pm 0.0052$$
 6 ABE $02E$ BELL Repl. by GLATTAUER 16 $0.0337 \pm 0.0044 \stackrel{+0.0072}{-0.0049}$ 7 ATHANAS 97 CLE2 Repl. by BARTELT 99

- 1 Obtained from a fit to the combined partially reconstructed $B o \ \overline D\ell
 u_\ell$ sample while tagged by the other fully reconstructed B meson in the event. Also reports fitted ρ^2
- ² Obtained from a fit to the combined $B \to \overline{D} \ell^+ \nu_\ell$ sample in which a hadronic decay of the second *B* meson is fully reconstructed and $\rho^2 = 1.20 \pm 0.09 \pm 0.04$.
- ³Obtained from a global fit to $B o D^{(*)} \ell \nu_{\ell}$ events, with reconstructed $D^0 \ell$ and $D^+ \ell$ final states and $ho^2=1.20\pm0.04\pm0.07$.
- ⁴ BARTELT 99: measured using both exclusive reconstructed $B^0 \to D^- \ell^+ \nu$ and $B^+ \to D^- \ell^+ \nu$ $D^0\ell^+
 u$ samples.
- ⁵ BUSKULIC 97: measured using exclusively reconstructed D^{\pm} with a $a^2=-0.05\pm0.53\pm0.53$ 0.38. The statistical correlation is 0.99.
- ⁶ Using the missing energy and momentum to extract kinematic information about the undetected neutrino in the $B^0 \rightarrow D^- \ell^+ \nu$ decay.
- ⁷ ATHANAS 97: measured using both exclusive reconstructed $B^0 \to D^- \ell^+ \nu$ and $B^+ \to D^0 \ell^+ \nu$ samples with a $\rho^2 = 0.59 \pm 0.22 \pm 0.12^{+0.59}_{-0}$. They report their experiment's uncertainties $\pm 0.0044 \pm 0.0048 {+0.0053 \atop -0.0012}$, where the first error is statistical, the second is systematic, and the third is the uncertainty due to the form factor model variations. We combine the last two in quadrature.

$\left|\mathsf{V}_{cb}\right|$ (from $D_s^{*-}\mu^+\nu_\mu)$

DOCUMENT ID

TECN
COMMENT

AAIJ
206
1 HCR
2004
7 20 VALUE (units 10^{-3}) 20E LHCB pp at 7, 8 TeV $41.4\pm0.6\pm0.9\pm1.2$

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¹ Measured from an inclusive sample of $D_s^-\mu^+$ candidates using CNL parameterization of the form factor. AAIJ 20E provides also measurement of $|{
m V}_{cb}|$ = (42.3 \pm 0.8 \pm 0.9 \pm $1.2) \times 10^{-3}$ using BGL parameterization of the form factor. The third uncertainty is due to the external inputs used in the measurement.

Vub MEASUREMENTS

For the discussion of V_{ub} measurements, which is not repeated here, see the review on "Determination of $|V_{cb}|$ and $|V_{ub}|$."

The CKM matrix element $|V_{ub}|$ can be determined by studying the rate of the charmless semileptonic decay $b \to u\ell\nu$. The relevant branching ratio measurements based on exclusive and inclusive decays can be found in the B Listings, and are not repeated here.

V_{cb} and V_{ub} CKM Matrix Elements REFERENCES

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