

# STRANGE MESONS ( $S = \pm 1$ , $C = B = 0$ )

$K^+ = u\bar{s}$ ,  $K^0 = d\bar{s}$ ,  $\bar{K}^0 = \bar{d}s$ ,  $K^- = \bar{u}s$ , similarly for  $K^*$ 's

**$K^\pm$**

$$I(J^P) = \frac{1}{2}(0^-)$$

Mass  $m = 493.677 \pm 0.016$  MeV <sup>[a]</sup> ( $S = 2.8$ )

Mean life  $\tau = (1.2380 \pm 0.0020) \times 10^{-8}$  s ( $S = 1.8$ )

$$c\tau = 3.711 \text{ m}$$

### ***CPT* violation parameters ( $\Delta = \text{rate difference/sum}$ )**

$$\Delta(K^\pm \rightarrow \mu^\pm \nu_\mu) = (-0.27 \pm 0.21)\%$$

$$\Delta(K^\pm \rightarrow \pi^\pm \pi^0) = (0.4 \pm 0.6)\% \quad [b]$$

### ***CP* violation parameters ( $\Delta = \text{rate difference/sum}$ )**

$$\Delta(K^\pm \rightarrow \pi^\pm e^+ e^-) = (-2.2 \pm 1.6) \times 10^{-2}$$

$$\Delta(K^\pm \rightarrow \pi^\pm \mu^+ \mu^-) = 0.010 \pm 0.023$$

$$\Delta(K^\pm \rightarrow \pi^\pm \pi^0 \gamma) = (0.0 \pm 1.2) \times 10^{-3}$$

$$\Delta(K^\pm \rightarrow \pi^\pm \pi^+ \pi^-) = (0.04 \pm 0.06)\%$$

$$\Delta(K^\pm \rightarrow \pi^\pm \pi^0 \pi^0) = (-0.02 \pm 0.28)\%$$

### ***T* violation parameters**

$$K^+ \rightarrow \pi^0 \mu^+ \nu_\mu \quad P_T = (-1.7 \pm 2.5) \times 10^{-3}$$

$$K^+ \rightarrow \mu^+ \nu_\mu \gamma \quad P_T = (-0.6 \pm 1.9) \times 10^{-2}$$

$$K^+ \rightarrow \pi^0 \mu^+ \nu_\mu \quad \text{Im}(\xi) = -0.006 \pm 0.008$$

### **Slope parameter $g$** <sup>[c]</sup>

(See Particle Listings for quadratic coefficients and alternative parametrization related to  $\pi\pi$  scattering)

$$K^\pm \rightarrow \pi^\pm \pi^+ \pi^- \quad g = -0.21134 \pm 0.00017$$

$$(g_+ - g_-) / (g_+ + g_-) = (-1.5 \pm 2.2) \times 10^{-4}$$

$$K^\pm \rightarrow \pi^\pm \pi^0 \pi^0 \quad g = 0.626 \pm 0.007$$

$$(g_+ - g_-) / (g_+ + g_-) = (1.8 \pm 1.8) \times 10^{-4}$$

### **$K^\pm$ decay form factors** <sup>[d,e]</sup>

Assuming  $\mu$ -e universality

$$\lambda_+(K_{\mu 3}^+) = \lambda_+(K_{e 3}^+) = (2.97 \pm 0.05) \times 10^{-2}$$

$$\lambda_0(K_{\mu 3}^+) = (1.95 \pm 0.12) \times 10^{-2}$$

Not assuming  $\mu$ - $e$  universality

$$\lambda_+(K_{e3}^+) = (2.98 \pm 0.05) \times 10^{-2}$$

$$\lambda_+(K_{\mu 3}^+) = (2.96 \pm 0.17) \times 10^{-2}$$

$$\lambda_0(K_{\mu 3}^+) = (1.96 \pm 0.13) \times 10^{-2}$$

$K_{e3}$  form factor quadratic fit

$$\lambda'_+ (K_{e3}^\pm) \text{ linear coeff.} = (2.49 \pm 0.17) \times 10^{-2}$$

$$\lambda''_+ (K_{e3}^\pm) \text{ quadratic coeff.} = (0.19 \pm 0.09) \times 10^{-2}$$

$$K_{e3}^+ |f_S/f_+| = (-0.3^{+0.8}_{-0.7}) \times 10^{-2}$$

$$K_{e3}^+ |f_T/f_+| = (-1.2 \pm 2.3) \times 10^{-2}$$

$$K_{\mu 3}^+ |f_S/f_+| = (0.2 \pm 0.6) \times 10^{-2}$$

$$K_{\mu 3}^+ |f_T/f_+| = (-0.1 \pm 0.7) \times 10^{-2}$$

$$K^+ \rightarrow e^+ \nu_e \gamma \quad |F_A + F_V| = 0.133 \pm 0.008 \quad (S = 1.3)$$

$$K^+ \rightarrow \mu^+ \nu_\mu \gamma \quad |F_A + F_V| = 0.165 \pm 0.013$$

$$K^+ \rightarrow e^+ \nu_e \gamma \quad |F_A - F_V| < 0.49, \text{ CL} = 90\%$$

$$K^+ \rightarrow \mu^+ \nu_\mu \gamma \quad |F_A - F_V| = -0.21 \pm 0.06$$

### Charge radius

$$\langle r \rangle = 0.560 \pm 0.031 \text{ fm}$$

### Forward-backward asymmetry

$$A_{FB}(K_{\pi\mu\mu}^\pm) = \frac{\Gamma(\cos(\theta_{K\mu})>0)-\Gamma(\cos(\theta_{K\mu})<0)}{\Gamma(\cos(\theta_{K\mu})>0)+\Gamma(\cos(\theta_{K\mu})<0)} < 2.3 \times 10^{-2}, \text{ CL} = 90\%$$

$K^-$  modes are charge conjugates of the modes below.

<b><math>K^+</math> DECAY MODES</b>	Fraction ( $\Gamma_i/\Gamma$ )	Scale factor/ Confidence level(MeV/c)	$p$
<b>Leptonic and semileptonic modes</b>			
$e^+ \nu_e$	( $1.582 \pm 0.007$ ) $\times 10^{-5}$		247
$\mu^+ \nu_\mu$	( $63.56 \pm 0.11$ ) %	S=1.2	236
$\pi^0 e^+ \nu_e$	( $5.07 \pm 0.04$ ) %	S=2.1	228
Called $K_{e3}^+$ .			
$\pi^0 \mu^+ \nu_\mu$	( $3.352 \pm 0.033$ ) %	S=1.9	215
Called $K_{\mu 3}^+$ .			
$\pi^0 \pi^0 e^+ \nu_e$	( $2.55 \pm 0.04$ ) $\times 10^{-5}$	S=1.1	206
$\pi^+ \pi^- e^+ \nu_e$	( $4.247 \pm 0.024$ ) $\times 10^{-5}$		203
$\pi^+ \pi^- \mu^+ \nu_\mu$	( $1.4 \pm 0.9$ ) $\times 10^{-5}$		151
$\pi^0 \pi^0 \pi^0 e^+ \nu_e$	< $3.5 \times 10^{-6}$ CL=90%		135

**Hadronic modes**

$\pi^+ \pi^0$	( 20.67 $\pm$ 0.08 ) %	S=1.2	205
$\pi^+ \pi^0 \pi^0$	( 1.760 $\pm$ 0.023 ) %	S=1.1	133
$\pi^+ \pi^+ \pi^-$	( 5.583 $\pm$ 0.024 ) %		125

**Leptonic and semileptonic modes with photons**

$\mu^+ \nu_\mu \gamma$	[f,g] ( 6.2 $\pm$ 0.8 ) $\times 10^{-3}$		236
$\mu^+ \nu_\mu \gamma (\text{SD}^+)$	[d,h] ( 1.33 $\pm$ 0.22 ) $\times 10^{-5}$		—
$\mu^+ \nu_\mu \gamma (\text{SD}^+ \text{INT})$	[d,h] < 2.7 $\times 10^{-5}$	CL=90%	—
$\mu^+ \nu_\mu \gamma (\text{SD}^- + \text{SD}^- \text{INT})$	[d,h] < 2.6 $\times 10^{-4}$	CL=90%	—
$e^+ \nu_e \gamma$	( 9.4 $\pm$ 0.4 ) $\times 10^{-6}$		247
$\pi^0 e^+ \nu_e \gamma$	[f,g] ( 2.56 $\pm$ 0.16 ) $\times 10^{-4}$		228
$\pi^0 e^+ \nu_e \gamma (\text{SD})$	[d,h] < 5.3 $\times 10^{-5}$	CL=90%	228
$\pi^0 \mu^+ \nu_\mu \gamma$	[f,g] ( 1.25 $\pm$ 0.25 ) $\times 10^{-5}$		215
$\pi^0 \pi^0 e^+ \nu_e \gamma$	< 5 $\times 10^{-6}$	CL=90%	206

**Hadronic modes with photons or  $\ell\bar{\ell}$  pairs**

$\pi^+ \pi^0 \gamma (\text{INT})$	( - 4.2 $\pm$ 0.9 ) $\times 10^{-6}$		—
$\pi^+ \pi^0 \gamma (\text{DE})$	[f,i] ( 6.0 $\pm$ 0.4 ) $\times 10^{-6}$		205
$\pi^+ \pi^0 \pi^0 \gamma$	[f,g] ( 7.6 $\pm$ 6.0 ) $\times 10^{-6}$		133
$\pi^+ \pi^+ \pi^- \gamma$	[f,g] ( 1.04 $\pm$ 0.31 ) $\times 10^{-4}$		125
$\pi^+ \gamma \gamma$	[f] ( 1.01 $\pm$ 0.06 ) $\times 10^{-6}$		227
$\pi^+ 3\gamma$	[f] < 1.0 $\times 10^{-4}$	CL=90%	227
$\pi^+ e^+ e^- \gamma$	( 1.19 $\pm$ 0.13 ) $\times 10^{-8}$		227

**Leptonic modes with  $\ell\bar{\ell}$  pairs**

$e^+ \nu_e \nu \bar{\nu}$	< 6 $\times 10^{-5}$	CL=90%	247
$\mu^+ \nu_\mu \nu \bar{\nu}$	< 2.4 $\times 10^{-6}$	CL=90%	236
$e^+ \nu_e e^+ e^-$	( 2.48 $\pm$ 0.20 ) $\times 10^{-8}$		247
$\mu^+ \nu_\mu e^+ e^-$	( 7.06 $\pm$ 0.31 ) $\times 10^{-8}$		236
$e^+ \nu_e \mu^+ \mu^-$	( 1.7 $\pm$ 0.5 ) $\times 10^{-8}$		223
$\mu^+ \nu_\mu \mu^+ \mu^-$	< 4.1 $\times 10^{-7}$	CL=90%	185

**Lepton family number (*LF*), Lepton number (*L*),  $\Delta S = \Delta Q$  (*SQ*)  
violating modes, or  $\Delta S = 1$  weak neutral current (*S1*) modes**

$\pi^+ \pi^+ e^- \bar{\nu}_e$	SQ < 1.3 $\times 10^{-8}$	CL=90%	203
$\pi^+ \pi^+ \mu^- \bar{\nu}_\mu$	SQ < 3.0 $\times 10^{-6}$	CL=95%	151
$\pi^+ e^+ e^-$	S1 ( 3.00 $\pm$ 0.09 ) $\times 10^{-7}$		227
$\pi^+ \mu^+ \mu^-$	S1 ( 9.4 $\pm$ 0.6 ) $\times 10^{-8}$	S=2.6	172
$\pi^+ \nu \bar{\nu}$	S1 ( 1.7 $\pm$ 1.1 ) $\times 10^{-10}$		227
$\pi^+ \pi^0 \nu \bar{\nu}$	S1 < 4.3 $\times 10^{-5}$	CL=90%	205
$\mu^- \nu e^+ e^+$	LF < 2.1 $\times 10^{-8}$	CL=90%	236
$\mu^+ \nu_e$	LF [j] < 4 $\times 10^{-3}$	CL=90%	236

$\pi^+ \mu^+ e^-$	<i>LF</i>	<	1.3	$\times 10^{-11}$	CL=90%	214
$\pi^+ \mu^- e^+$	<i>LF</i>	<	5.2	$\times 10^{-10}$	CL=90%	214
$\pi^- \mu^+ e^+$	<i>L</i>	<	5.0	$\times 10^{-10}$	CL=90%	214
$\pi^- e^+ e^+$	<i>L</i>	<	6.4	$\times 10^{-10}$	CL=90%	227
$\pi^- \mu^+ \mu^+$	<i>L</i>	[ <i>j</i> ] <	1.1	$\times 10^{-9}$	CL=90%	172
$\mu^+ \bar{\nu}_e$	<i>L</i>	[ <i>j</i> ] <	3.3	$\times 10^{-3}$	CL=90%	236
$\pi^0 e^+ \bar{\nu}_e$	<i>L</i>	<	3	$\times 10^{-3}$	CL=90%	228
$\pi^+ \gamma$		[ <i>k</i> ] <	2.3	$\times 10^{-9}$	CL=90%	227

**$K^0$**

$$I(J^P) = \frac{1}{2}(0^-)$$

50%  $K_S$ , 50%  $K_L$

Mass  $m = 497.611 \pm 0.013$  MeV (S = 1.2)

$m_{K^0} - m_{K^\pm} = 3.934 \pm 0.020$  MeV (S = 1.6)

### Mean square charge radius

$$\langle r^2 \rangle = -0.077 \pm 0.010 \text{ fm}^2$$

### T-violation parameters in $K^0$ - $\bar{K}^0$ mixing [e]

$$\text{Asymmetry } A_T \text{ in } K^0\text{-}\bar{K}^0 \text{ mixing} = (6.6 \pm 1.6) \times 10^{-3}$$

### CP-violation parameters

$$\text{Re}(\epsilon) = (1.596 \pm 0.013) \times 10^{-3}$$

### CPT-violation parameters [e]

$$\text{Re } \delta = (2.5 \pm 2.3) \times 10^{-4}$$

$$\text{Im } \delta = (-1.5 \pm 1.6) \times 10^{-5}$$

$$\text{Re}(y), K_{e3} \text{ parameter} = (0.4 \pm 2.5) \times 10^{-3}$$

$$\text{Re}(x_-), K_{e3} \text{ parameter} = (-2.9 \pm 2.0) \times 10^{-3}$$

$$|m_{K^0} - m_{\bar{K}^0}| / m_{\text{average}} < 6 \times 10^{-19}, \text{ CL} = 90\% \text{ [l]}$$

$$(\Gamma_{K^0} - \Gamma_{\bar{K}^0}) / m_{\text{average}} = (8 \pm 8) \times 10^{-18}$$

### Tests of $\Delta S = \Delta Q$

$$\text{Re}(x_+), K_{e3} \text{ parameter} = (-0.9 \pm 3.0) \times 10^{-3}$$

**$K_S^0$**

$$I(J^P) = \frac{1}{2}(0^-)$$

Mean life  $\tau = (0.8954 \pm 0.0004) \times 10^{-10}$  s (S = 1.1) Assuming CPT

Mean life  $\tau = (0.89564 \pm 0.00033) \times 10^{-10}$  s Not assuming CPT

$c\tau = 2.6844$  cm Assuming CPT

### ***CP*-violation parameters [n]**

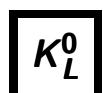
$$\text{Im}(\eta_{+-0}) = -0.002 \pm 0.009$$

$$\text{Im}(\eta_{000}) = -0.001 \pm 0.016$$

$$|\eta_{000}| = |A(K_S^0 \rightarrow 3\pi^0)/A(K_L^0 \rightarrow 3\pi^0)| < 0.0088, \text{ CL} = 90\%$$

$$CP \text{ asymmetry } A \text{ in } \pi^+ \pi^- e^+ e^- = (-0.4 \pm 0.8)\%$$

<b><math>K_S^0</math> DECAY MODES</b>	Fraction ( $\Gamma_i/\Gamma$ )	Scale factor/ Confidence level	<i>p</i> (MeV/c)
<b>Hadronic modes</b>			
$\pi^0 \pi^0$	(30.69 $\pm$ 0.05) %		209
$\pi^+ \pi^-$	(69.20 $\pm$ 0.05) %		206
$\pi^+ \pi^- \pi^0$	( 3.5 $\pm$ 1.1 ) $\times 10^{-7}$		133
<b>Modes with photons or <math>\ell\bar{\ell}</math> pairs</b>			
$\pi^+ \pi^- \gamma$	[g,o] ( 1.79 $\pm$ 0.05 ) $\times 10^{-3}$		206
$\pi^+ \pi^- e^+ e^-$	( 4.79 $\pm$ 0.15 ) $\times 10^{-5}$		206
$\pi^0 \gamma \gamma$	[o] ( 4.9 $\pm$ 1.8 ) $\times 10^{-8}$		230
$\gamma \gamma$	( 2.63 $\pm$ 0.17 ) $\times 10^{-6}$	S=3.0	249
<b>Semileptonic modes</b>			
$\pi^\pm e^\mp \nu_e$	[p] ( 7.04 $\pm$ 0.08 ) $\times 10^{-4}$		229
<b><i>CP</i> violating (<i>CP</i>) and <math>\Delta S = 1</math> weak neutral current (S1) modes</b>			
$3\pi^0$	$CP$ < 2.6 $\times 10^{-8}$	CL=90%	139
$\mu^+ \mu^-$	$S1$ < 9 $\times 10^{-9}$	CL=90%	225
$e^+ e^-$	$S1$ < 9 $\times 10^{-9}$	CL=90%	249
$\pi^0 e^+ e^-$	$S1$ [o] ( 3.0 $\pm$ 1.5 ) $\times 10^{-9}$		230
$\pi^0 \mu^+ \mu^-$	$S1$ ( 2.9 $\pm$ 1.5 ) $\times 10^{-9}$		177



$$I(J^P) = \frac{1}{2}(0^-)$$

$$\begin{aligned}
 m_{K_L} - m_{K_S} \\
 &= (0.5293 \pm 0.0009) \times 10^{10} \text{ } \hbar \text{ s}^{-1} \quad (S = 1.3) \quad \text{Assuming } CPT \\
 &= (3.484 \pm 0.006) \times 10^{-12} \text{ MeV} \quad \text{Assuming } CPT \\
 &= (0.5289 \pm 0.0010) \times 10^{10} \text{ } \hbar \text{ s}^{-1} \quad \text{Not assuming } CPT \\
 &\text{Mean life } \tau = (5.116 \pm 0.021) \times 10^{-8} \text{ s} \quad (S = 1.1) \\
 &c\tau = 15.34 \text{ m}
 \end{aligned}$$

### Slope parameters [c]

(See Particle Listings for other linear and quadratic coefficients)

$$K_L^0 \rightarrow \pi^+ \pi^- \pi^0: g = 0.678 \pm 0.008 \quad (S = 1.5)$$

$$K_L^0 \rightarrow \pi^+ \pi^- \pi^0: h = 0.076 \pm 0.006$$

$$K_L^0 \rightarrow \pi^+ \pi^- \pi^0: k = 0.0099 \pm 0.0015$$

$$K_L^0 \rightarrow \pi^0 \pi^0 \pi^0: h = (0.6 \pm 1.2) \times 10^{-3}$$

### $K_L$ decay form factors [e]

Linear parametrization assuming  $\mu$ -e universality

$$\lambda_+(K_{\mu 3}^0) = \lambda_+(K_{e 3}^0) = (2.82 \pm 0.04) \times 10^{-2} \quad (S = 1.1)$$

$$\lambda_0(K_{\mu 3}^0) = (1.38 \pm 0.18) \times 10^{-2} \quad (S = 2.2)$$

Quadratic parametrization assuming  $\mu$ -e universality

$$\lambda'_+(K_{\mu 3}^0) = \lambda'_+(K_{e 3}^0) = (2.40 \pm 0.12) \times 10^{-2} \quad (S = 1.2)$$

$$\lambda''_+(K_{\mu 3}^0) = \lambda''_+(K_{e 3}^0) = (0.20 \pm 0.05) \times 10^{-2} \quad (S = 1.2)$$

$$\lambda_0(K_{\mu 3}^0) = (1.16 \pm 0.09) \times 10^{-2} \quad (S = 1.2)$$

Pole parametrization assuming  $\mu$ -e universality

$$M_V^\mu(K_{\mu 3}^0) = M_V^e(K_{e 3}^0) = 878 \pm 6 \text{ MeV} \quad (S = 1.1)$$

$$M_S^\mu(K_{\mu 3}^0) = 1252 \pm 90 \text{ MeV} \quad (S = 2.6)$$

Dispersive parametrization assuming  $\mu$ -e universality

$$\Lambda_+ = (0.251 \pm 0.006) \times 10^{-1} \quad (S = 1.5)$$

$$\ln(C) = (1.75 \pm 0.18) \times 10^{-1} \quad (S = 2.0)$$

$$K_{e 3}^0 \quad |f_S/f_+| = (1.5^{+1.4}_{-1.6}) \times 10^{-2}$$

$$K_{e 3}^0 \quad |f_T/f_+| = (5^{+4}_{-5}) \times 10^{-2}$$

$$K_{\mu 3}^0 \quad |f_T/f_+| = (12 \pm 12) \times 10^{-2}$$

$$K_L \rightarrow \ell^+ \ell^- \gamma, K_L \rightarrow \ell^+ \ell^- \ell'^+ \ell'^-: \alpha_{K^*} = -0.205 \pm 0.022 \quad (S = 1.8)$$

$$K_L^0 \rightarrow \ell^+ \ell^- \gamma, K_L^0 \rightarrow \ell^+ \ell^- \ell'^+ \ell'^-: \alpha_{DIP} = -1.69 \pm 0.08 \quad (S = 1.7)$$

$$K_L \rightarrow \pi^+ \pi^- e^+ e^-: a_1/a_2 = -0.737 \pm 0.014 \text{ GeV}^2$$

$$K_L \rightarrow \pi^0 2\gamma: a_V = -0.43 \pm 0.06 \quad (S = 1.5)$$

### ***CP*-violation parameters [<sup>n</sup>]**

$$\begin{aligned} A_L &= (0.332 \pm 0.006)\% \\ |\eta_{00}| &= (2.220 \pm 0.011) \times 10^{-3} \quad (S = 1.8) \\ |\eta_{+-}| &= (2.232 \pm 0.011) \times 10^{-3} \quad (S = 1.8) \\ |\epsilon| &= (2.228 \pm 0.011) \times 10^{-3} \quad (S = 1.8) \\ |\eta_{00}/\eta_{+-}| &= 0.9950 \pm 0.0007 [q] \quad (S = 1.6) \\ \text{Re}(\epsilon'/\epsilon) &= (1.66 \pm 0.23) \times 10^{-3} [q] \quad (S = 1.6) \end{aligned}$$

Assuming *CPT*

$$\begin{aligned} \phi_{+-} &= (43.51 \pm 0.05)^\circ \quad (S = 1.2) \\ \phi_{00} &= (43.52 \pm 0.05)^\circ \quad (S = 1.3) \\ \phi_\epsilon = \phi_{SW} &= (43.52 \pm 0.05)^\circ \quad (S = 1.2) \\ \text{Im}(\epsilon'/\epsilon) &= -(\phi_{00} - \phi_{+-})/3 = (-0.002 \pm 0.005)^\circ \quad (S = 1.7) \end{aligned}$$

Not assuming *CPT*

$$\begin{aligned} \phi_{+-} &= (43.4 \pm 0.5)^\circ \quad (S = 1.2) \\ \phi_{00} &= (43.7 \pm 0.6)^\circ \quad (S = 1.2) \\ \phi_\epsilon &= (43.5 \pm 0.5)^\circ \quad (S = 1.3) \end{aligned}$$

*CP* asymmetry  $A$  in  $K_L^0 \rightarrow \pi^+ \pi^- e^+ e^- = (13.7 \pm 1.5)\%$

$\beta_{CP}$  from  $K_L^0 \rightarrow e^+ e^- e^+ e^- = -0.19 \pm 0.07$

$\gamma_{CP}$  from  $K_L^0 \rightarrow e^+ e^- e^+ e^- = 0.01 \pm 0.11 \quad (S = 1.6)$

$j$  for  $K_L^0 \rightarrow \pi^+ \pi^- \pi^0 = 0.0012 \pm 0.0008$

$f$  for  $K_L^0 \rightarrow \pi^+ \pi^- \pi^0 = 0.004 \pm 0.006$

$|\eta_{+-\gamma}| = (2.35 \pm 0.07) \times 10^{-3}$

$\phi_{+-\gamma} = (44 \pm 4)^\circ$

$|\epsilon'_{+-\gamma}|/\epsilon < 0.3$ , CL = 90%

$|g_{E1}|$  for  $K_L^0 \rightarrow \pi^+ \pi^- \gamma < 0.21$ , CL = 90%

### ***T*-violation parameters**

$\text{Im}(\xi)$  in  $K_{\mu 3}^0 = -0.007 \pm 0.026$

### ***CPT* invariance tests**

$$\begin{aligned} \phi_{00} - \phi_{+-} &= (0.34 \pm 0.32)^\circ \\ \text{Re}(\frac{2}{3}\eta_{+-} + \frac{1}{3}\eta_{00}) - \frac{A_L}{2} &= (-3 \pm 35) \times 10^{-6} \end{aligned}$$

### **$\Delta S = -\Delta Q$ in $K_{\ell 3}^0$ decay**

$\text{Re } x = -0.002 \pm 0.006$

$\text{Im } x = 0.0012 \pm 0.0021$

<b><math>K_L^0</math> DECAY MODES</b>	Fraction ( $\Gamma_i/\Gamma$ )	Scale factor/ Confidence level(MeV/c)	$p$
<b>Semileptonic modes</b>			
$\pi^\pm e^\mp \nu_e$ Called $K_{e3}^0$ .	[ $p$ ] $(40.55 \pm 0.11) \%$	S=1.7	229
$\pi^\pm \mu^\mp \nu_\mu$ Called $K_{\mu 3}^0$ .	[ $p$ ] $(27.04 \pm 0.07) \%$	S=1.1	216
$(\pi \mu \text{atom}) \nu$		$(1.05 \pm 0.11) \times 10^{-7}$	188
$\pi^0 \pi^\pm e^\mp \nu$	[ $p$ ] $(5.20 \pm 0.11) \times 10^{-5}$		207
$\pi^\pm e^\mp \nu e^+ e^-$	[ $p$ ] $(1.26 \pm 0.04) \times 10^{-5}$		229
<b>Hadronic modes, including Charge conjugation <math>\times</math> Parity Violating (CPV) modes</b>			
$3\pi^0$		$(19.52 \pm 0.12) \%$	S=1.6 139
$\pi^+ \pi^- \pi^0$		$(12.54 \pm 0.05) \%$	133
$\pi^+ \pi^-$	CPV [ $r$ ]	$(1.967 \pm 0.010) \times 10^{-3}$	S=1.5 206
$\pi^0 \pi^0$	CPV	$(8.64 \pm 0.06) \times 10^{-4}$	S=1.8 209
<b>Semileptonic modes with photons</b>			
$\pi^\pm e^\mp \nu_e \gamma$	[ $g,p,s$ ] $(3.79 \pm 0.06) \times 10^{-3}$		229
$\pi^\pm \mu^\mp \nu_\mu \gamma$		$(5.65 \pm 0.23) \times 10^{-4}$	216
<b>Hadronic modes with photons or <math>\ell\bar{\ell}</math> pairs</b>			
$\pi^0 \pi^0 \gamma$		$< 2.43 \times 10^{-7}$	CL=90% 209
$\pi^+ \pi^- \gamma$	[ $g,s$ ]	$(4.15 \pm 0.15) \times 10^{-5}$	S=2.8 206
$\pi^+ \pi^- \gamma$ (DE)		$(2.84 \pm 0.11) \times 10^{-5}$	S=2.0 206
$\pi^0 2\gamma$	[ $s$ ]	$(1.273 \pm 0.033) \times 10^{-6}$	230
$\pi^0 \gamma e^+ e^-$		$(1.62 \pm 0.17) \times 10^{-8}$	230
<b>Other modes with photons or <math>\ell\bar{\ell}</math> pairs</b>			
$2\gamma$		$(5.47 \pm 0.04) \times 10^{-4}$	S=1.1 249
$3\gamma$		$< 7.4 \times 10^{-8}$	CL=90% 249
$e^+ e^- \gamma$		$(9.4 \pm 0.4) \times 10^{-6}$	S=2.0 249
$\mu^+ \mu^- \gamma$		$(3.59 \pm 0.11) \times 10^{-7}$	S=1.3 225
$e^+ e^- \gamma\gamma$	[ $s$ ]	$(5.95 \pm 0.33) \times 10^{-7}$	249
$\mu^+ \mu^- \gamma\gamma$	[ $s$ ]	$(1.0 \pm 0.8) \times 10^{-8}$	225
<b>Charge conjugation <math>\times</math> Parity (CP) or Lepton Family number (LF) violating modes, or <math>\Delta S = 1</math> weak neutral current (S1) modes</b>			
$\mu^+ \mu^-$	S1	$(6.84 \pm 0.11) \times 10^{-9}$	225
$e^+ e^-$	S1	$(9 \pm 6) \times 10^{-12}$	249
$\pi^+ \pi^- e^+ e^-$	S1 [ $s$ ]	$(3.11 \pm 0.19) \times 10^{-7}$	206
$\pi^0 \pi^0 e^+ e^-$	S1	$< 6.6 \times 10^{-9}$	CL=90% 209
$\pi^0 \pi^0 \mu^+ \mu^-$	S1	$< 9.2 \times 10^{-11}$	CL=90% 57
$\mu^+ \mu^- e^+ e^-$	S1	$(2.69 \pm 0.27) \times 10^{-9}$	225

$e^+ e^- e^+ e^-$	$S1$	$(3.56 \pm 0.21) \times 10^{-8}$		249
$\pi^0 \mu^+ \mu^-$	$CP, S1$	$[t] < 3.8 \times 10^{-10}$	CL=90%	177
$\pi^0 e^+ e^-$	$CP, S1$	$[t] < 2.8 \times 10^{-10}$	CL=90%	230
$\pi^0 \nu \bar{\nu}$	$CP, S1$	$[u] < 2.6 \times 10^{-8}$	CL=90%	230
$\pi^0 \pi^0 \nu \bar{\nu}$	$S1$	$< 8.1 \times 10^{-7}$	CL=90%	209
$e^\pm \mu^\mp$	$LF$	$[p] < 4.7 \times 10^{-12}$	CL=90%	238
$e^\pm e^\pm \mu^\mp \mu^\mp$	$LF$	$[p] < 4.12 \times 10^{-11}$	CL=90%	225
$\pi^0 \mu^\pm e^\mp$	$LF$	$[p] < 7.6 \times 10^{-11}$	CL=90%	217
$\pi^0 \pi^0 \mu^\pm e^\mp$	$LF$	$< 1.7 \times 10^{-10}$	CL=90%	159

**K\*(892)**

$I(J^P) = \frac{1}{2}(1^-)$

 $K^{*}(892)^\pm$  hadroproduced mass  $m = 891.76 \pm 0.25$  MeV $K^{*}(892)^\pm$  in  $\tau$  decays mass  $m = 895.5 \pm 0.8$  MeV $K^{*}(892)^0$  mass  $m = 895.55 \pm 0.20$  MeV ( $S = 1.7$ ) $K^{*}(892)^\pm$  hadroproduced full width  $\Gamma = 50.3 \pm 0.8$  MeV $K^{*}(892)^\pm$  in  $\tau$  decays full width  $\Gamma = 46.2 \pm 1.3$  MeV $K^{*}(892)^0$  full width  $\Gamma = 47.3 \pm 0.5$  MeV ( $S = 1.9$ )

<b>K*(892) DECAY MODES</b>	Fraction ( $\Gamma_i/\Gamma$ )	Confidence level	$p$ (MeV/c)
$K\pi$	$\sim 100$ %		290
$K^0 \gamma$	$(2.46 \pm 0.21) \times 10^{-3}$		307
$K^\pm \gamma$	$(1.00 \pm 0.09) \times 10^{-3}$		309
$K\pi\pi$	$< 7 \times 10^{-4}$	95%	223

**K<sub>1</sub>(1270)**

$I(J^P) = \frac{1}{2}(1^+)$

Mass  $m = 1272 \pm 7$  MeV [v]Full width  $\Gamma = 90 \pm 20$  MeV [v]

<b>K<sub>1</sub>(1270) DECAY MODES</b>	Fraction ( $\Gamma_i/\Gamma$ )	$p$ (MeV/c)
$K\rho$	$(42 \pm 6) \%$	46
$K_0^*(1430)\pi$	$(28 \pm 4) \%$	†
$K^*(892)\pi$	$(16 \pm 5) \%$	302
$K\omega$	$(11.0 \pm 2.0) \%$	†
$Kf_0(1370)$	$(3.0 \pm 2.0) \%$	†
$\gamma K^0$	seen	539

**K<sub>1</sub>(1400)**

$I(J^P) = \frac{1}{2}(1^+)$

Mass  $m = 1403 \pm 7$  MeVFull width  $\Gamma = 174 \pm 13$  MeV ( $S = 1.6$ )

<b><math>K_1(1400)</math> DECAY MODES</b>	Fraction ( $\Gamma_i/\Gamma$ )	$p$ (MeV/c)
$K^*(892)\pi$	(94 $\pm$ 6) %	402
$K\rho$	( 3.0 $\pm$ 3.0) %	293
$Kf_0(1370)$	( 2.0 $\pm$ 2.0) %	†
$K\omega$	( 1.0 $\pm$ 1.0) %	284
$K_0^*(1430)\pi$	not seen	†
$\gamma K^0$	seen	613

### **$K^*(1410)$**

$$I(J^P) = \frac{1}{2}(1^-)$$

Mass  $m = 1421 \pm 9$  MeV

Full width  $\Gamma = 236 \pm 18$  MeV

<b><math>K^*(1410)</math> DECAY MODES</b>	Fraction ( $\Gamma_i/\Gamma$ )	Confidence level	$p$ (MeV/c)
$K^*(892)\pi$	> 40 %	95%	416
$K\pi$	( 6.6 $\pm$ 1.3) %	617	
$K\rho$	< 7 %	95%	313
$\gamma K^0$	< 2.2 $\times 10^{-4}$	90%	623

### **$K_0^*(1430)$ [x]**

$$I(J^P) = \frac{1}{2}(0^+)$$

Mass  $m = 1425 \pm 50$  MeV

Full width  $\Gamma = 270 \pm 80$  MeV

<b><math>K_0^*(1430)</math> DECAY MODES</b>	Fraction ( $\Gamma_i/\Gamma$ )	$p$ (MeV/c)
$K\pi$	(93 $\pm$ 10) %	619
$K\eta$	( 8.6 $\pm$ 2.7) %	486
$K\eta'(958)$	seen	†

### **$K_2^*(1430)$**

$$I(J^P) = \frac{1}{2}(2^+)$$

$K_2^*(1430)^{\pm}$  mass  $m = 1425.6 \pm 1.5$  MeV (S = 1.1)

$K_2^*(1430)^0$  mass  $m = 1432.4 \pm 1.3$  MeV

$K_2^*(1430)^{\pm}$  full width  $\Gamma = 98.5 \pm 2.7$  MeV (S = 1.1)

$K_2^*(1430)^0$  full width  $\Gamma = 109 \pm 5$  MeV (S = 1.9)

<b><math>K_2^*(1430)</math> DECAY MODES</b>	Fraction ( $\Gamma_i/\Gamma$ )	Scale factor/ Confidence level	$p$ (MeV/c)
$K\pi$	$(49.9 \pm 1.2) \%$		619
$K^*(892)\pi$	$(24.7 \pm 1.5) \%$		419
$K^*(892)\pi\pi$	$(13.4 \pm 2.2) \%$		372
$K\rho$	$(8.7 \pm 0.8) \%$	S=1.2	318
$K\omega$	$(2.9 \pm 0.8) \%$		311
$K^+\gamma$	$(2.4 \pm 0.5) \times 10^{-3}$	S=1.1	627
$K\eta$	$(1.5^{+3.4}_{-1.0}) \times 10^{-3}$	S=1.3	486
$K\omega\pi$	$< 7.2 \times 10^{-4}$	CL=95%	100
$K^0\gamma$	$< 9 \times 10^{-4}$	CL=90%	626

### **$K^*(1680)$**

$$I(J^P) = \frac{1}{2}(1^-)$$

Mass  $m = 1718 \pm 18$  MeV

Full width  $\Gamma = 322 \pm 110$  MeV (S = 4.2)

<b><math>K^*(1680)</math> DECAY MODES</b>	Fraction ( $\Gamma_i/\Gamma$ )	$p$ (MeV/c)
$K\pi$	$(38.7 \pm 2.5) \%$	782
$K\rho$	$(31.4^{+5.0}_{-2.1}) \%$	571
$K^*(892)\pi$	$(29.9^{+2.2}_{-5.0}) \%$	618
$K\phi$	seen	387

### **$K_2(1770)$ [y]**

$$I(J^P) = \frac{1}{2}(2^-)$$

Mass  $m = 1773 \pm 8$  MeV

Full width  $\Gamma = 186 \pm 14$  MeV

<b><math>K_2(1770)</math> DECAY MODES</b>	Fraction ( $\Gamma_i/\Gamma$ )	$p$ (MeV/c)
$K\pi\pi$		794
$K_2^*(1430)\pi$	dominant	288
$K^*(892)\pi$	seen	654
$Kf_2(1270)$	seen	53
$K\phi$	seen	441
$K\omega$	seen	607

### **$K_3^*(1780)$**

$$I(J^P) = \frac{1}{2}(3^-)$$

Mass  $m = 1776 \pm 7$  MeV ( $S = 1.1$ )  
 Full width  $\Gamma = 159 \pm 21$  MeV ( $S = 1.3$ )

<b><math>K_3^*(1780)</math> DECAY MODES</b>	Fraction ( $\Gamma_i/\Gamma$ )	Confidence level	$p$ (MeV/c)
$K\rho$	(31 $\pm$ 9) %		613
$K^*(892)\pi$	(20 $\pm$ 5) %		656
$K\pi$	(18.8 $\pm$ 1.0) %		813
$K\eta$	(30 $\pm$ 13) %		719
$K_2^*(1430)\pi$	< 16 %	95%	291

### **$K_2(1820)^{[z]}$**

$$I(J^P) = \frac{1}{2}(2^-)$$

Mass  $m = 1819 \pm 12$  MeV  
 Full width  $\Gamma = 264 \pm 34$  MeV

<b><math>K_2(1820)</math> DECAY MODES</b>	Fraction ( $\Gamma_i/\Gamma$ )	$p$ (MeV/c)
$K_2^*(1430)\pi$	seen	329
$K^*(892)\pi$	seen	683
$Kf_2(1270)$	seen	191
$K\omega$	seen	640
$K\phi$	seen	483

### **$K_4^*(2045)$**

$$I(J^P) = \frac{1}{2}(4^+)$$

Mass  $m = 2045 \pm 9$  MeV ( $S = 1.1$ )  
 Full width  $\Gamma = 198 \pm 30$  MeV

<b><math>K_4^*(2045)</math> DECAY MODES</b>	Fraction ( $\Gamma_i/\Gamma$ )	$p$ (MeV/c)
$K\pi$	(9.9 $\pm$ 1.2) %	958
$K^*(892)\pi\pi$	(9 $\pm$ 5) %	802
$K^*(892)\pi\pi\pi$	(7 $\pm$ 5) %	768
$\rho K\pi$	(5.7 $\pm$ 3.2) %	741
$\omega K\pi$	(5.0 $\pm$ 3.0) %	738
$\phi K\pi$	(2.8 $\pm$ 1.4) %	594
$\phi K^*(892)$	(1.4 $\pm$ 0.7) %	363

## NOTES

- [a] See the note in the  $K^\pm$  Particle Listings.
- [b] Neglecting photon channels. See, e.g., A. Pais and S.B. Treiman, Phys. Rev. **D12**, 2744 (1975).
- [c] The definition of the slope parameters of the  $K \rightarrow 3\pi$  Dalitz plot is as follows (see also “Note on Dalitz Plot Parameters for  $K \rightarrow 3\pi$  Decays” in the  $K^\pm$  Particle Listings):
 
$$|M|^2 = 1 + g(s_3 - s_0)/m_{\pi^+}^2 + \dots$$
- [d] See the “Note on  $\pi^\pm \rightarrow \ell^\pm \nu \gamma$  and  $K^\pm \rightarrow \ell^\pm \nu \gamma$  Form Factors” in the  $\pi^\pm$  Particle Listings for definitions and details.
- [e] For more details and definitions of parameters see the Particle Listings.
- [f] See the  $K^\pm$  Particle Listings for the energy limits used in this measurement.
- [g] Most of this radiative mode, the low-momentum  $\gamma$  part, is also included in the parent mode listed without  $\gamma$ ’s.
- [h] Structure-dependent part.
- [i] Direct-emission branching fraction.
- [j] Derived from an analysis of neutrino-oscillation experiments.
- [k] Violates angular-momentum conservation.

[l] Derived from measured values of  $\phi_{+-}$ ,  $\phi_{00}$ ,  $|\eta|$ ,  $|m_{K_L^0} - m_{K_S^0}|$ , and  $\tau_{K_S^0}$ , as described in the introduction to “Tests of Conservation Laws.”

- [n] The  $CP$ -violation parameters are defined as follows (see also “Note on  $CP$  Violation in  $K_S \rightarrow 3\pi$ ” and “Note on  $CP$  Violation in  $K_L^0$  Decay” in the Particle Listings):

$$\eta_{+-} = |\eta_{+-}| e^{i\phi_{+-}} = \frac{A(K_L^0 \rightarrow \pi^+ \pi^-)}{A(K_S^0 \rightarrow \pi^+ \pi^-)} = \epsilon + \epsilon'$$

$$\eta_{00} = |\eta_{00}| e^{i\phi_{00}} = \frac{A(K_L^0 \rightarrow \pi^0 \pi^0)}{A(K_S^0 \rightarrow \pi^0 \pi^0)} = \epsilon - 2\epsilon'$$

$$\delta = \frac{\Gamma(K_L^0 \rightarrow \pi^- \ell^+ \nu) - \Gamma(K_L^0 \rightarrow \pi^+ \ell^- \nu)}{\Gamma(K_L^0 \rightarrow \pi^- \ell^+ \nu) + \Gamma(K_L^0 \rightarrow \pi^+ \ell^- \nu)},$$

$$\text{Im}(\eta_{+-0})^2 = \frac{\Gamma(K_S^0 \rightarrow \pi^+ \pi^- \pi^0)^{CP \text{ viol.}}}{\Gamma(K_L^0 \rightarrow \pi^+ \pi^- \pi^0)},$$

$$\text{Im}(\eta_{000})^2 = \frac{\Gamma(K_S^0 \rightarrow \pi^0 \pi^0 \pi^0)}{\Gamma(K_L^0 \rightarrow \pi^0 \pi^0 \pi^0)}.$$

where for the last two relations  $CPT$  is assumed valid, *i.e.*,  $\text{Re}(\eta_{+-0}) \simeq 0$  and  $\text{Re}(\eta_{000}) \simeq 0$ .

- [o] See the  $K_S^0$  Particle Listings for the energy limits used in this measurement.
- [p] The value is for the sum of the charge states or particle/antiparticle states indicated.
- [q]  $\text{Re}(\epsilon'/\epsilon) = \epsilon'/\epsilon$  to a very good approximation provided the phases satisfy  $CPT$  invariance.
- [r] This mode includes gammas from inner bremsstrahlung but not the direct emission mode  $K_L^0 \rightarrow \pi^+ \pi^- \gamma$ (DE).
- [s] See the  $K_L^0$  Particle Listings for the energy limits used in this measurement.
- [t] Allowed by higher-order electroweak interactions.
- [u] Violates  $CP$  in leading order. Test of direct  $CP$  violation since the indirect  $CP$ -violating and  $CP$ -conserving contributions are expected to be suppressed.
- [v] This is only an educated guess; the error given is larger than the error on the average of the published values. See the Particle Listings for details.
- [x] See the “Note on  $f_0(1370)$ ” in the  $f_0(1370)$  Particle Listings and in the 1994 edition.
- [y] See the note in the  $L(1770)$  Particle Listings in Reviews of Modern Physics **56** S1 (1984), p. S200. See also the “Note on  $K_2(1770)$  and the  $K_2(1820)$ ” in the  $K_2(1770)$  Particle Listings .
- [z] See the “Note on  $K_2(1770)$  and the  $K_2(1820)$ ” in the  $K_2(1770)$  Particle Listings .