

$N(1710) P_{11}$

$$I(J^P) = \frac{1}{2}(\frac{1}{2}^+) \text{ Status: } ***$$

Most of the results published before 1975 were last included in our 1982 edition, Physics Letters **111B** 1 (1982). Some further obsolete results published before 1980 were last included in our 2006 edition, Journal of Physics, G **33** 1 (2006).

The latest GWU analysis (ARNDT 06) finds no evidence for this resonance.

$N(1710)$ BREIT-WIGNER MASS

<u>VALUE (MeV)</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
1680 to 1740 (≈ 1710) OUR ESTIMATE			
1717 \pm 28	MANLEY	92	IPWA $\pi N \rightarrow \pi N$ & $N\pi\pi$
1700 \pm 50	CUTKOSKY	80	IPWA $\pi N \rightarrow \pi N$
1723 \pm 9	HOEHLER	79	IPWA $\pi N \rightarrow \pi N$
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●			
1752 \pm 3	PENNER	02C	DPWA Multichannel
1699 \pm 65	VRANA	00	DPWA Multichannel
1720 \pm 10	ARNDT	96	IPWA $\gamma N \rightarrow \pi N$
1766 \pm 34	¹ BATINIC	95	DPWA $\pi N \rightarrow N\pi, N\eta$
1706	CUTKOSKY	90	IPWA $\pi N \rightarrow \pi N$
1692	CRAWFORD	80	DPWA $\gamma N \rightarrow \pi N$
1730	SAXON	80	DPWA $\pi^- p \rightarrow \Lambda K^0$
1720	² LONGACRE	77	IPWA $\pi N \rightarrow N\pi\pi$
1710	³ LONGACRE	75	IPWA $\pi N \rightarrow N\pi\pi$

$N(1710)$ BREIT-WIGNER WIDTH

<u>VALUE (MeV)</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
50 to 250 (≈ 100) OUR ESTIMATE			
480 \pm 230	MANLEY	92	IPWA $\pi N \rightarrow \pi N$ & $N\pi\pi$
93 \pm 30	CUTKOSKY	90	IPWA $\pi N \rightarrow \pi N$
90 \pm 30	CUTKOSKY	80	IPWA $\pi N \rightarrow \pi N$
120 \pm 15	HOEHLER	79	IPWA $\pi N \rightarrow \pi N$
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●			
386 \pm 59	PENNER	02C	DPWA Multichannel
143 \pm 100	VRANA	00	DPWA Multichannel
105 \pm 10	ARNDT	96	IPWA $\gamma N \rightarrow \pi N$
185 \pm 61	BATINIC	95	DPWA $\pi N \rightarrow N\pi, N\eta$
540	BELL	83	DPWA $\pi^- p \rightarrow \Lambda K^0$
200	CRAWFORD	80	DPWA $\gamma N \rightarrow \pi N$
550	SAXON	80	DPWA $\pi^- p \rightarrow \Lambda K^0$
120	² LONGACRE	77	IPWA $\pi N \rightarrow N\pi\pi$
75	³ LONGACRE	75	IPWA $\pi N \rightarrow N\pi\pi$

$N(1710)$ POLE POSITION**REAL PART**

<u>VALUE (MeV)</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
1670 to 1770 (≈ 1720) OUR ESTIMATE			
1690	⁴ HOEHLER	93	SPED $\pi N \rightarrow \pi N$
1698	CUTKOSKY	90	IPWA $\pi N \rightarrow \pi N$
1690 \pm 20	CUTKOSKY	80	IPWA $\pi N \rightarrow \pi N$
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●			
1679	VRANA	00	DPWA Multichannel
1770	ARNDT	95	DPWA $\pi N \rightarrow N\pi$
1636	ARNDT	91	DPWA $\pi N \rightarrow \pi N$ Soln SM90
1708 or 1712	⁵ LONGACRE	78	IPWA $\pi N \rightarrow N\pi\pi$
1720 or 1711	² LONGACRE	77	IPWA $\pi N \rightarrow N\pi\pi$

–2×IMAGINARY PART

<u>VALUE (MeV)</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
80 to 380 (≈ 230) OUR ESTIMATE			
200	⁴ HOEHLER	93	SPED $\pi N \rightarrow \pi N$
88	CUTKOSKY	90	IPWA $\pi N \rightarrow \pi N$
80 \pm 20	CUTKOSKY	80	IPWA $\pi N \rightarrow \pi N$
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●			
132	VRANA	00	DPWA Multichannel
378	ARNDT	95	DPWA $\pi N \rightarrow N\pi$
544	ARNDT	91	DPWA $\pi N \rightarrow \pi N$ Soln SM90
17 or 22	⁵ LONGACRE	78	IPWA $\pi N \rightarrow N\pi\pi$
123 or 115	² LONGACRE	77	IPWA $\pi N \rightarrow N\pi\pi$

 $N(1710)$ ELASTIC POLE RESIDUE**MODULUS $|r|$**

<u>VALUE (MeV)</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
15	HOEHLER	93	SPED $\pi N \rightarrow \pi N$
9	CUTKOSKY	90	IPWA $\pi N \rightarrow \pi N$
8 \pm 2	CUTKOSKY	80	IPWA $\pi N \rightarrow \pi N$
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●			
37	ARNDT	95	DPWA $\pi N \rightarrow N\pi$
149	ARNDT	91	DPWA $\pi N \rightarrow \pi N$ Soln SM90

PHASE θ

<u>VALUE ($^\circ$)</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
–167	CUTKOSKY	90	IPWA $\pi N \rightarrow \pi N$
175 \pm 35	CUTKOSKY	80	IPWA $\pi N \rightarrow \pi N$
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●			
–167	ARNDT	95	DPWA $\pi N \rightarrow N\pi$
149	ARNDT	91	DPWA $\pi N \rightarrow \pi N$ Soln SM90

N(1710) DECAY MODES

The following branching fractions are our estimates, not fits or averages.

Mode	Fraction (Γ_i/Γ)
Γ_1 $N\pi$	10–20 %
Γ_2 $N\eta$	(6.2±1.0) %
Γ_3 $N\omega$	(13.0±2.0) %
Γ_4 ΛK	5–25 %
Γ_5 ΣK	
Γ_6 $N\pi\pi$	40–90 %
Γ_7 $\Delta\pi$	15–40 %
Γ_8 $\Delta(1232)\pi$, <i>P</i> -wave	
Γ_9 $N\rho$	5–25 %
Γ_{10} $N\rho$, <i>S</i> =1/2, <i>P</i> -wave	
Γ_{11} $N\rho$, <i>S</i> =3/2, <i>P</i> -wave	
Γ_{12} $N(\pi\pi)_{S\text{-wave}}^{I=0}$	10–40 %
Γ_{13} $p\gamma$	0.002–0.05%
Γ_{14} $p\gamma$, helicity=1/2	0.002–0.05%
Γ_{15} $n\gamma$	0.0–0.02%
Γ_{16} $n\gamma$, helicity=1/2	0.0–0.02%

N(1710) BRANCHING RATIOS

$\Gamma(N\pi)/\Gamma_{\text{total}}$	Γ_1/Γ
<u>VALUE</u>	<u>DOCUMENT ID</u> <u>TECN</u> <u>COMMENT</u>
0.10 to 0.20 OUR ESTIMATE	
0.09±0.04	MANLEY 92 IPWA $\pi N \rightarrow \pi N$ & $N\pi\pi$
0.20±0.04	CUTKOSKY 80 IPWA $\pi N \rightarrow \pi N$
0.12±0.04	HOEHLER 79 IPWA $\pi N \rightarrow \pi N$
• • • We do not use the following data for averages, fits, limits, etc. • • •	
0.14±0.08	PENNER 02C DPWA Multichannel
0.27±0.13	VRANA 00 DPWA Multichannel
0.08±0.14	BATINIC 95 DPWA $\pi N \rightarrow N\pi, N\eta$
$\Gamma(N\eta)/\Gamma_{\text{total}}$	Γ_2/Γ
<u>VALUE</u>	<u>DOCUMENT ID</u> <u>TECN</u> <u>COMMENT</u>
0.062±0.010 OUR AVERAGE	
0.36 ±0.11	PENNER 02C DPWA Multichannel
0.06 ±0.01	VRANA 00 DPWA Multichannel
• • • We do not use the following data for averages, fits, limits, etc. • • •	
0.16 ±0.10	BATINIC 95 DPWA $\pi N \rightarrow N\pi, N\eta$
$\Gamma(N\omega)/\Gamma_{\text{total}}$	Γ_3/Γ
<u>VALUE</u>	<u>DOCUMENT ID</u> <u>TECN</u> <u>COMMENT</u>
0.13±0.02	PENNER 02C DPWA Multichannel

$(\Gamma_i \Gamma_f)^{1/2} / \Gamma_{\text{total}}$ in $N\pi \rightarrow N(1710) \rightarrow \Lambda K$				$(\Gamma_1 \Gamma_4)^{1/2} / \Gamma$
VALUE	DOCUMENT ID	TECN	COMMENT	
+0.12 to +0.18 OUR ESTIMATE				
+0.16	BELL	83	DPWA	$\pi^- p \rightarrow \Lambda K^0$
+0.14	SAXON	80	DPWA	$\pi^- p \rightarrow \Lambda K^0$

$\Gamma(\Lambda K) / \Gamma_{\text{total}}$				Γ_4 / Γ
VALUE	DOCUMENT ID	TECN	COMMENT	
0.05 ± 0.03	SHKLYAR	05	DPWA	Multichannel
0.05 ± 0.02	PENNER	02C	DPWA	Multichannel
0.1 ± 0.1	VRANA	00	DPWA	Multichannel

$\Gamma(\Sigma K) / \Gamma_{\text{total}}$				Γ_5 / Γ
VALUE	DOCUMENT ID	TECN	COMMENT	
• • • We do not use the following data for averages, fits, limits, etc. • • •				
0.07 ± 0.07	PENNER	02C	DPWA	Multichannel

$(\Gamma_i \Gamma_f)^{1/2} / \Gamma_{\text{total}}$ in $N\pi \rightarrow N(1710) \rightarrow \Sigma K$				$(\Gamma_1 \Gamma_5)^{1/2} / \Gamma$
VALUE	DOCUMENT ID	TECN	COMMENT	
• • • We do not use the following data for averages, fits, limits, etc. • • •				
-0.034	LIVANOS	80	DPWA	$\pi p \rightarrow \Sigma K$

Note: Signs of couplings from $\pi N \rightarrow N\pi\pi$ analyses were changed in the 1986 edition to agree with the baryon-first convention; the overall phase ambiguity is resolved by choosing a negative sign for the $\Delta(1620) S_{31}$ coupling to $\Delta(1232)\pi$.

$(\Gamma_i \Gamma_f)^{1/2} / \Gamma_{\text{total}}$ in $N\pi \rightarrow N(1710) \rightarrow \Delta(1232)\pi, P\text{-wave}$				$(\Gamma_1 \Gamma_8)^{1/2} / \Gamma$
VALUE	DOCUMENT ID	TECN	COMMENT	
±0.16 to ±0.22 OUR ESTIMATE				
-0.21 ± 0.04	MANLEY	92	IPWA	$\pi N \rightarrow \pi N$ & $N\pi\pi$
-0.17	² LONGACRE	77	IPWA	$\pi N \rightarrow N\pi\pi$
+0.20	³ LONGACRE	75	IPWA	$\pi N \rightarrow N\pi\pi$

$\Gamma(\Delta(1232)\pi, P\text{-wave}) / \Gamma_{\text{total}}$				Γ_8 / Γ
VALUE	DOCUMENT ID	TECN	COMMENT	
0.39 ± 0.08	VRANA	00	DPWA	Multichannel

$(\Gamma_i \Gamma_f)^{1/2} / \Gamma_{\text{total}}$ in $N\pi \rightarrow N(1710) \rightarrow N\rho, S=1/2, P\text{-wave}$				$(\Gamma_1 \Gamma_{10})^{1/2} / \Gamma$
VALUE	DOCUMENT ID	TECN	COMMENT	
±0.09 to ±0.19 OUR ESTIMATE				
+0.05 ± 0.06	MANLEY	92	IPWA	$\pi N \rightarrow \pi N$ & $N\pi\pi$
+0.19	² LONGACRE	77	IPWA	$\pi N \rightarrow N\pi\pi$
-0.20	³ LONGACRE	75	IPWA	$\pi N \rightarrow N\pi\pi$

$\Gamma(N\rho, S=1/2, P\text{-wave}) / \Gamma_{\text{total}}$				Γ_{10} / Γ
VALUE	DOCUMENT ID	TECN	COMMENT	
0.17 ± 0.01	VRANA	00	DPWA	Multichannel

$(\Gamma_i \Gamma_f)^{1/2} / \Gamma_{\text{total}}$ in $N\pi \rightarrow N(1710) \rightarrow N\rho, S=3/2, P\text{-wave}$	$(\Gamma_1 \Gamma_{11})^{1/2} / \Gamma$		
VALUE	DOCUMENT ID	TECN	COMMENT
+0.31	² LONGACRE	77	IPWA $\pi N \rightarrow N\pi\pi$

$(\Gamma_i \Gamma_f)^{1/2} / \Gamma_{\text{total}}$ in $N\pi \rightarrow N(1710) \rightarrow N(\pi\pi)_{S\text{-wave}}^{I=0}$	$(\Gamma_1 \Gamma_{12})^{1/2} / \Gamma$		
VALUE	DOCUMENT ID	TECN	COMMENT
± 0.14 to ± 0.22 OUR ESTIMATE			
+0.04 \pm 0.05	MANLEY	92	IPWA $\pi N \rightarrow \pi N$ & $N\pi\pi$
-0.26	² LONGACRE	77	IPWA $\pi N \rightarrow N\pi\pi$
-0.28	³ LONGACRE	75	IPWA $\pi N \rightarrow N\pi\pi$

$\Gamma(N(\pi\pi)_{S\text{-wave}}^{I=0}) / \Gamma_{\text{total}}$	Γ_{12} / Γ		
VALUE	DOCUMENT ID	TECN	COMMENT
0.01 \pm 0.01	VRANA	00	DPWA Multichannel

N(1710) PHOTON DECAY AMPLITUDES

N(1710) \rightarrow $p\gamma$, helicity-1/2 amplitude $A_{1/2}$

VALUE (GeV ^{-1/2})	DOCUMENT ID	TECN	COMMENT
+0.009 \pm 0.022 OUR ESTIMATE			
0.007 \pm 0.015	ARNDT	96	IPWA $\gamma N \rightarrow \pi N$
0.006 \pm 0.018	CRAWFORD	83	IPWA $\gamma N \rightarrow \pi N$
0.028 \pm 0.009	AWAJI	81	DPWA $\gamma N \rightarrow \pi N$
-0.009 \pm 0.006	ARAI	80	DPWA $\gamma N \rightarrow \pi N$ (fit 1)
-0.012 \pm 0.005	ARAI	80	DPWA $\gamma N \rightarrow \pi N$ (fit 2)
0.015 \pm 0.025	CRAWFORD	80	DPWA $\gamma N \rightarrow \pi N$
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●			
0.044	PENNER	02D	DPWA Multichannel
-0.037 \pm 0.002	LI	93	IPWA $\gamma N \rightarrow \pi N$

N(1710) \rightarrow $n\gamma$, helicity-1/2 amplitude $A_{1/2}$

VALUE (GeV ^{-1/2})	DOCUMENT ID	TECN	COMMENT
-0.002 \pm 0.014 OUR ESTIMATE			
-0.002 \pm 0.015	ARNDT	96	IPWA $\gamma N \rightarrow \pi N$
0.000 \pm 0.018	AWAJI	81	DPWA $\gamma N \rightarrow \pi N$
-0.001 \pm 0.003	FUJII	81	DPWA $\gamma N \rightarrow \pi N$
0.005 \pm 0.013	ARAI	80	DPWA $\gamma N \rightarrow \pi N$ (fit 1)
0.011 \pm 0.021	ARAI	80	DPWA $\gamma N \rightarrow \pi N$ (fit 2)
-0.017 \pm 0.020	CRAWFORD	80	DPWA $\gamma N \rightarrow \pi N$
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●			
-0.024	PENNER	02D	DPWA Multichannel
0.052 \pm 0.003	LI	93	IPWA $\gamma N \rightarrow \pi N$

$N(1710) \quad \gamma p \rightarrow \Lambda K^+$ AMPLITUDES

$(\Gamma_i \Gamma_f)^{1/2} / \Gamma_{\text{total}}$ in $p\gamma \rightarrow N(1710) \rightarrow \Lambda K^+$ (M_{1-} amplitude)

VALUE (units 10^{-3}) DOCUMENT ID TECN

• • • We do not use the following data for averages, fits, limits, etc. • • •

– 10.6 ± 0.4	WORKMAN	90	DPWA
– 7.21	TANABE	89	DPWA

$p\gamma \rightarrow N(1710) \rightarrow \Lambda K^+$ phase angle θ (M_{1-} amplitude)

VALUE (degrees) DOCUMENT ID TECN

• • • We do not use the following data for averages, fits, limits, etc. • • •

215 ± 3	WORKMAN	90	DPWA
176.3	TANABE	89	DPWA

$N(1710)$ FOOTNOTES

- ¹ BATINIC 95 finds a second state with a 6 MeV mass difference.
- ² LONGACRE 77 pole positions are from a search for poles in the unitarized T-matrix; the first (second) value uses, in addition to $\pi N \rightarrow N\pi\pi$ data, elastic amplitudes from a Saclay (CERN) partial-wave analysis. The other LONGACRE 77 values are from eyeball fits with Breit-Wigner circles to the T-matrix amplitudes.
- ³ From method II of LONGACRE 75: eyeball fits with Breit-Wigner circles to the T-matrix amplitudes.
- ⁴ See HOEHLER 93 for a detailed discussion of the evidence for and the pole parameters of N and Δ resonances as determined from Argand diagrams of πN elastic partial-wave amplitudes and from plots of the speeds with which the amplitudes traverse the diagrams.
- ⁵ LONGACRE 78 values are from a search for poles in the unitarized T-matrix. The first (second) value uses, in addition to $\pi N \rightarrow N\pi\pi$ data, elastic amplitudes from a Saclay (CERN) partial-wave analysis.

$N(1710)$ REFERENCES

For early references, see Physics Letters **111B** 1 (1982).

ARNDT	06	PR C74 045205	R.A. Arndt <i>et al.</i>	
PDG	06	JPG 33 1	W.-M. Yao <i>et al.</i>	(GWU)
SHKLYAR	05	PR C72 015210	V. Shklyar, H. Lenske, U. Mosel	(PDG Collab.)
PENNER	02C	PR C66 055211	G. Penner, U. Mosel	(GIES)
PENNER	02D	PR C66 055212	G. Penner, U. Mosel	(GIES)
VRANA	00	PRPL 328 181	T.P. Vrana, S.A. Dytman,, T.-S.H. Lee	(PITT+)
ARNDT	96	PR C53 430	R.A. Arndt, I.I. Strakovsky, R.L. Workman	(VPI)
ARNDT	95	PR C52 2120	R.A. Arndt <i>et al.</i>	(VPI, BRCO)
BATINIC	95	PR C51 2310	M. Batinic <i>et al.</i>	(BOSK, UCLA)
Also		PR C57 1004 (erratum)	M. Batinic <i>et al.</i>	
HOEHLER	93	πN Newsletter 9 1	G. Hohler	(KARL)
LI	93	PR C47 2759	Z.J. Li <i>et al.</i>	(VPI)
MANLEY	92	PR D45 4002	D.M. Manley, E.M. Saleski	(KENT) IJP
Also		PR D30 904	D.M. Manley <i>et al.</i>	(VPI)
ARNDT	91	PR D43 2131	R.A. Arndt <i>et al.</i>	(VPI, TELE) IJP
CUTKOSKY	90	PR D42 235	R.E. Cutkosky, S. Wang	(CMU)
WORKMAN	90	PR C42 781	R.L. Workman	(VPI)
TANABE	89	PR C39 741	H. Tanabe, M. Kohno, C. Bennhold	(MANZ)
Also		NC 102A 193	M. Kohno, H. Tanabe, C. Bennhold	(MANZ)
BELL	83	NP B222 389	K.W. Bell <i>et al.</i>	(RL) IJP

CRAWFORD	83	NP B211 1	R.L. Crawford, W.T. Morton	(GLAS)
PDG	82	PL 111B 1	M. Roos <i>et al.</i>	(HELSE, CIT, CERN)
AWAJI	81	Bonn Conf. 352	N. Awaji, R. Kajikawa	(NAGO)
Also		NP B197 365	K. Fujii <i>et al.</i>	(NAGO)
FUJII	81	NP B187 53	K. Fujii <i>et al.</i>	(NAGO, OSAK)
ARAI	80	Toronto Conf. 93	I. Arai	(INUS)
Also		NP B194 251	I. Arai, H. Fujii	(INUS)
CRAWFORD	80	Toronto Conf. 107	R.L. Crawford	(GLAS)
CUTKOSKY	80	Toronto Conf. 19	R.E. Cutkosky <i>et al.</i>	(CMU, LBL) IJP
Also		PR D20 2839	R.E. Cutkosky <i>et al.</i>	(CMU, LBL) IJP
LIVANOS	80	Toronto Conf. 35	P. Livanos <i>et al.</i>	(SACL) IJP
SAXON	80	NP B162 522	D.H. Saxon <i>et al.</i>	(RHEL, BRIS) IJP
HOEHLER	79	PDAT 12-1	G. Hohler <i>et al.</i>	(KARLT) IJP
Also		Toronto Conf. 3	R. Koch	(KARLT) IJP
LONGACRE	78	PR D17 1795	R.S. Longacre <i>et al.</i>	(LBL, SLAC)
LONGACRE	77	NP B122 493	R.S. Longacre, J. Dolbeau	(SACL) IJP
Also		NP B108 365	J. Dolbeau <i>et al.</i>	(SACL) IJP
LONGACRE	75	PL 55B 415	R.S. Longacre <i>et al.</i>	(LBL, SLAC) IJP
