



$$I(J^P) = 0(\frac{1}{2}^+)$$

$$\text{Charge} = -\frac{1}{3} e \quad \text{Bottom} = -1$$

## ***b*-QUARK MASS**

The first value is the “running mass”  $\overline{m}_b(\mu = \overline{m}_b)$  in the  $\overline{\text{MS}}$  scheme, and the second value is the  $1S$  mass, which is half the mass of the  $\Upsilon(1S)$  in perturbation theory. For a review of different quark mass definitions and their properties, see EL-KHADRA 02. The  $1S$  mass is better suited for use in analyzing  $B$  decays than the  $\overline{\text{MS}}$  mass because it gives a stable perturbative expansion. We have converted masses in other schemes to the  $\overline{\text{MS}}$  mass and  $1S$  mass using two-loop QCD perturbation theory with  $\alpha_s(\mu = \overline{m}_b) = 0.22$ . The range 4.1–4.4 for the  $\overline{\text{MS}}$  mass corresponds to 4.6–4.9 for the  $1S$  mass and 4.7–5.0 GeV for the pole mass.

<u><math>\overline{\text{MS}}</math> MASS (GeV)</u>	<u><math>1S</math> MASS (GeV)</u>	<u>DOCUMENT ID</u>	<u>TECN</u>
<b>4.20 ± 0.07 OUR EVALUATION</b> of $\overline{\text{MS}}$ Mass			
<b>4.70 ± 0.07 OUR EVALUATION</b> of $1S$ Mass			
4.4 ± 0.3	4.9 ± 0.3	1,2 GRAY	05 LATT
4.22 ± 0.06	4.72 ± 0.07	3 AUBERT	04x THEO
4.17 ± 0.03	4.68 ± 0.03	4 BAUER	04 THEO
4.22 ± 0.11	4.72 ± 0.12	2,5 HOANG	04 THEO
4.25 ± 0.11	4.76 ± 0.12	2,6 MCNEILE	04 LATT
4.22 ± 0.09	4.74 ± 0.10	7 BAUER	03 THEO
4.19 ± 0.05	4.66 ± 0.05	8 BORDES	03 THEO
4.20 ± 0.09	4.67 ± 0.10	9 CORCELLA	03 THEO
4.33 ± 0.10	4.84 ± 0.11	2,10 DEDIVITIIS	03 LATT
4.24 ± 0.10	4.72 ± 0.11	11 EIDEMULLER	03 THEO
4.207 ± 0.031	4.682 ± 0.035	12 ERLER	03 THEO
4.33 ± 0.06 ± 0.10	4.82 ± 0.07 ± 0.11	13 MAHMOOD	03 THEO
4.346 ± 0.070	4.837 ± 0.078	14 PENIN	02 THEO
3.95 ± 0.57	4.40 ± 0.63	15 ABBIENDI	01s OPAL
4.21 ± 0.05	4.69 ± 0.06	16 KUHN	01 THEO
4.05 ± 0.06	4.51 ± 0.07	17 NARISON	01B THEO
4.210 ± 0.090 ± 0.025	4.69 ± 0.100 ± 0.028	18 PINEDA	01 THEO
4.7 ± 0.74	5.23 ± 0.82	19 BARATE	00v ALEP
4.20 ± 0.06	4.71 ± 0.03	20 HOANG	00 THEO
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●			
4.437 <sup>+0.045</sup> <sub>-0.029</sub>	4.938 <sup>+0.050</sup> <sub>-0.032</sub>	21 LUCHA	00 THEO
4.454 <sup>+0.045</sup> <sub>-0.029</sub>	4.957 <sup>+0.050</sup> <sub>-0.032</sub>	21 PINEDA	00 THEO
4.25 ± 0.08	4.73 ± 0.09	22 BENEKE	99 THEO
3.8 <sup>+0.77</sup> <sub>-2.0</sub>	4.23 <sup>+0.86</sup> <sub>-2.0</sub>	23 BRANDENB...	99
4.25 ± 0.09	4.73 ± 0.10	24 HOANG	99 THEO
4.2 ± 0.1	4.67 ± 0.11	25 MELNIKOV	99 THEO

4.21 ± 0.11	4.69 ± 0.12	26 PENIN	99 THEO
3.91 ± 0.67	4.35 ± 0.75	27 ABREU	98 DLPH
4.14 ± 0.04	4.61 ± 0.05	28 KUEHN	98 THEO
4.15 ± 0.05 ± 0.20	4.62 ± 0.06 ± 0.22	29 GIMENEZ	97 LATT
4.19 ± 0.06	4.66 ± 0.07	30 JAMIN	97 THEO
4.16 ± 0.32 ± 0.60	4.63 ± 0.36 ± 0.67	31 RODRIGO	97 THEO

- <sup>1</sup> GRAY 05 determines  $\overline{m}_b(\overline{m}_b)$  from a lattice computation of the  $\Upsilon$  spectrum. The simulations have 2+1 dynamical light flavors. The  $b$  quark is implemented using NRQCD.
- <sup>2</sup> We have converted  $m_b$  to the 1S scheme.
- <sup>3</sup> AUBERT 04X obtain  $m_b$  from a fit to the hadron mass and lepton energy distributions in semileptonic  $B$  decay. The paper quotes values in the kinetic scheme. The  $\overline{MS}$  value has been provided by the BABAR collaboration, and we have converted this to the 1S scheme.
- <sup>4</sup> BAUER 04 determine  $m_b$ ,  $m_c$  and  $m_b - m_c$  by a global fit to inclusive  $B$  decay spectra.
- <sup>5</sup> HOANG 04 determines  $m_b$  ( $\overline{m}_b$ ) from moments at order  $\alpha_s^2$  of the bottom production cross-section in  $e^+e^-$  annihilation.
- <sup>6</sup> MCNEILE 04 use lattice QCD with dynamical light quarks and a static heavy quark to compute the masses of heavy-light mesons.
- <sup>7</sup> BAUER 03 determine the  $b$  quark mass by a global fit to  $B$  decay observables. The experimental data includes lepton energy and hadron invariant mass moments in semileptonic  $B \rightarrow X_c \ell \nu_\ell$  decay, and the inclusive photon spectrum in  $B \rightarrow X_s \gamma$  decay. The theoretical expressions used are of order  $1/m^3$ , and  $\alpha_s^2 \beta_0$ .
- <sup>8</sup> BORDES 03 determines  $m_b$  using QCD finite energy sum rules to order  $\alpha_s^2$ .
- <sup>9</sup> CORCELLA 03 determines  $\overline{m}_b$  using sum rules computed to order  $\alpha_s^2$ . Includes charm quark mass effects.
- <sup>10</sup> DEDIVITIIS 03 use a quenched lattice computation of heavy-heavy and heavy-light meson masses.
- <sup>11</sup> EIDEMULLER 03 determines  $\overline{m}_b$  and  $\overline{m}_c$  using QCD sum rules.
- <sup>12</sup> ERLER 03 determines  $\overline{m}_b$  and  $\overline{m}_c$  using QCD sum rules. Includes recent BES data.
- <sup>13</sup> MAHMOOD 03 determines  $m_b^{1S}$  by a fit to the lepton energy moments in  $B \rightarrow X_c \ell \nu_\ell$  decay. The theoretical expressions used are of order  $1/m^3$  and  $\alpha_s^2 \beta_0$ . We have converted their result to the  $\overline{MS}$  scheme.
- <sup>14</sup> PENIN 02 determines  $\overline{m}_b$  from the spectrum of the  $\Upsilon$  system.
- <sup>15</sup> ABBIENDI 01S find  $\overline{m}_b(M_Z)$  to be  $2.67 \pm 0.4$  GeV from an analysis of  $Z \rightarrow b$  decays.
- <sup>16</sup> KUHN 01 uses an analysis of the  $e^+e^-$  total cross section to hadrons.
- <sup>17</sup> NARISON 01B uses pseudoscalar sum rules in the  $B$  and  $D$  meson channels.
- <sup>18</sup> PINEDA 01 uses the  $\Upsilon(1S)$  system to determine the quark mass. The errors are due to theory, and the uncertainty in  $\alpha_s$ .
- <sup>19</sup> BARATE 00V obtain the  $b$  quark mass  $\overline{m}_b(M_Z) = 3.27 \pm 0.22(\text{stat}) \pm 0.22(\text{exp}) \pm 0.38(\text{had}) \pm 0.16(\text{thy})$  from an analysis of event shape variables in  $Z$  decays. We have converted this to  $\mu = \overline{m}_b$ .
- <sup>20</sup> HOANG 00 uses a NNLO calculation of the vacuum polarization function to determine spectral moments of the masses and electronic decay widths of the  $\Upsilon$  mesons.
- <sup>21</sup> LUCHA 00, PINEDA 00 obtain the  $b$ -quark mass from a perturbative calculation of the  $\Upsilon$  spectrum and decay widths to order  $\alpha_s^4$ .
- <sup>22</sup> BENEKE 99 uses a calculation of the  $b\overline{b}$  production cross section and the mass of the  $\Upsilon$  meson at NNLO.
- <sup>23</sup> BRANDENBURG 99 obtain a  $b$ -quark mass of  $\overline{m}_b(M_Z) = 2.56 \pm 0.27^{+0.28+0.49}_{-0.38-1.48}$  from a study of three-jet events at the  $Z$ . We have converted this to  $\mu = \overline{m}_b$ .
- <sup>24</sup> HOANG 99 uses a NNLO calculation of the vacuum polarization function to determine spectral moments of the masses and electronic decay widths of the  $\Upsilon$  mesons.

- 25 MELNIKOV 99 compute the quark mass using  $\Upsilon$  sum rules at NNLO.
- 26 PENIN 99 compute the quark mass using  $\Upsilon$  sum rules at NNLO.
- 27 ABREU 98i determines the  $\overline{\text{MS}}$  mass  $\overline{m}_b = 2.67 \pm 0.25 \pm 0.34 \pm 0.27$  GeV at  $\mu=M_Z$  from three jet heavy quark production at LEP. ABREU 98i have rescaled the result to  $\mu = \overline{m}_b$  using  $\alpha_s=0.118 \pm 0.003$ .
- 28 KUEHN 98 uses a calculation of the vacuum polarization function, including resumming threshold effects, to determine spectral moments of the masses of the  $\Upsilon$  mesons. We have converted their extracted value of  $4.75 \pm 0.04$  for the pole mass to the  $\overline{\text{MS}}$  scheme.
- 29 GIMENEZ 97 uses lattice computations of the  $B$ -meson propagator and the  $B$ -meson binding energy  $\overline{\Lambda}$  in the HQET. Their systematic (second) error for the  $\overline{\text{MS}}$  mass is an estimate of the effects of higher-order corrections in the matching of the HQET operators (renormalon effects).
- 30 JAMIN 97 apply the QCD moment method to the  $\Upsilon$  system. They also find a pole mass of  $4.60 \pm 0.02$ .
- 31 RODRIGO 97 determines the  $\overline{\text{MS}}$  mass  $\overline{m}_b = 2.85 \pm 0.22 \pm 0.20 \pm 0.36$  GeV at  $\mu=M_Z$  from three jet heavy quark production at LEP. We have rescaled the result.

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## b-QUARK REFERENCES

GRAY	05	PR D72 094507	A. Gray <i>et al.</i>	(HPQCD, UKQCD Collab.)
AUBERT	04X	PRL 93 011803	B. Aubert <i>et al.</i>	(BABAR Collab.)
BAUER	04	PR D70 094017	C. Bauer <i>et al.</i>	
HOANG	04	PL B594 127	A.H. Hoang, M. Jamin	
MCNEILE	04	PL B600 77	C. McNeile, C. Michael, G. Thompson	(UKQCD Collab.)
BAUER	03	PR D67 054012	C.W. Bauer <i>et al.</i>	
BORDES	03	PL B562 81	J. Bordes, J. Penarrocha, K. Schilcher	
CORCELLA	03	PL B554 133	G. Corcella, A.H. Hoang	
DEDIVITIIS	03	NP B675 309	G.M. de Divitiis <i>et al.</i>	
EIDEMULLER	03	PR D67 113002	M. Eidemuller	
ERLER	03	PL B558 125	J. Erler, M. Luo	
MAHMOOD	03	PR D67 072001	A.H. Mahmood <i>et al.</i>	(CLEO Collab.)
EL-KHADRA	02	ARNPS 52 201	A.X. El-Khadra, M. Luke	
PENIN	02	PL B538 335	A. Penin, M. Steinhauser	
ABBIENDI	01S	EPJ C21 411	G. Abbiendi <i>et al.</i>	(OPAL Collab.)
KUHN	01	NP B619 588	J.H. Kuhn, M. Steinhauser	
NARISON	01B	PL B520 115	S. Narison	
PINEDA	01	JHEP 0106 022	A. Pineda	
BARATE	00V	EPJ C18 1	R. Barate <i>et al.</i>	(ALEPH Collab.)
HOANG	00	PR D61 034005	A.H. Hoang	
LUCHA	00	PR D62 097501	W. Lucha, F.F. Schoeberl	
PINEDA	00	PR D61 077505	A. Pineda, F.J. Yndurain	
BENEKE	99	PL B471 233	M. Beneke, A. Signer	
BRANDENB...	99	PL B468 168	A. Brandenburg <i>et al.</i>	
HOANG	99	PR D59 014039	A.H. Hoang	
MELNIKOV	99	PR D59 114009	K. Melnikov, A. Yelkhovsky	
PENIN	99	NP B549 217	A.A. Penin, A.A. Pivovarov	
ABREU	98i	PL B418 430	P. Abreu <i>et al.</i>	(DELPHI Collab.)
KUEHN	98	NP B534 356	J.H. Kuehn, A.A. Penin, A.A. Pivovarov	
GIMENEZ	97	PL B393 124	V. Gimenez, G. Martinelli, C.T. Sachrajda	
JAMIN	97	NP B507 334	M. Jamin, A. Pich	
RODRIGO	97	PRL 79 193	G. Rodrigo, A. Santamaria, M.S. Bilenky	

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