



$$I(J^P) = \frac{1}{2}(0^-)$$

$$m_{K_L^0} - m_{K_S^0}$$

For earlier measurements, beginning with GOOD 61 and FITCH 61, see our 1986 edition, Physics Letters **170B** 132 (1986).

OUR FIT is described in the note on “Fits for  $K_L^0$   $CP$ -Violation Parameters” in the  $K_L^0$  Particle Listings.

The FITS given below are from the 2002 edition and do NOT include the new data which are indicated by the change bars at the right.

VALUE ( $10^{10} \hbar s^{-1}$ )	DOCUMENT ID	TECN	COMMENT
<b>0.5303 ± 0.0009</b> <b>OUR FIT</b>	Assuming $CPT$		
<b>0.5301 ± 0.0016</b> <b>OUR FIT</b>	Not assuming $CPT$		
0.5261 ± 0.0015	<sup>1</sup> ALAVI-HARATI03	KTEV	40–160 GeV $K$ beams
0.5288 ± 0.0042	<sup>2</sup> ALAVI-HARATI03	KTEV	40–160 GeV $K$ beams
0.5343 ± 0.0063 ± 0.0025	<sup>3</sup> ANGELOPO... 01	CPLR	
0.5240 ± 0.0044 ± 0.0033	APOSTOLA... 99C	CPLR	$K^0 - \bar{K}^0$ to $\pi^+ \pi^-$
0.5295 ± 0.0020 ± 0.0003	<sup>4</sup> ANGELOPO... 98D	CPLR	
0.5297 ± 0.0030 ± 0.0022	<sup>5</sup> SCHWINGEN...95	E773	20–160 GeV $K$ beams
0.5257 ± 0.0049 ± 0.0021	<sup>5</sup> GIBBONS 93C	E731	20–160 GeV $K$ beams
0.5340 ± 0.00255 ± 0.0015	<sup>6</sup> GEWENIGER 74C	SPEC	Gap method
0.5334 ± 0.0040 ± 0.0015	<sup>6</sup> GJESDAL 74	SPEC	Charge asymmetry in $K_{\ell 3}^0$
0.542 ± 0.006	CULLEN 70	CNTR	
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●			
0.5307 ± 0.0013	<sup>7</sup> ADLER 96C	RVUE	
0.5274 ± 0.0029 ± 0.0005	<sup>4</sup> ADLER 95	CPLR	Sup. by ANGELOPOULOS 98D
0.5286 ± 0.0028	<sup>8</sup> GIBBONS 93	E731	20–160 GeV $K$ beams
0.482 ± 0.014	<sup>9</sup> ARONSON 82B	SPEC	$E=30$ –110 GeV
0.534 ± 0.007	<sup>10</sup> CARNEGIE 71	ASPK	Gap method
0.542 ± 0.006	<sup>10</sup> ARONSON 70	ASPK	Gap method

<sup>1</sup> ALAVI-HARATI 03 fit  $\Delta m$  and  $K_S^0$  mean life simultaneously. See “ $K_S^0$  Mean Life” section for correlation information. Assumes  $CPT$ .

<sup>2</sup> ALAVI-HARATI 03 fit  $\Delta m$ ,  $\phi_{+-}$ , and  $\tau_{K_S}$  simultaneously. See  $\phi_{+-}$  in the “ $K_L$   $CP$  violation” section for correlation information.  $CPT$  is not assumed.

<sup>3</sup> ANGELOPOULOS 01 uses strong interactions strangeness tagging at two different times.

<sup>4</sup> Uses  $\bar{K}_{e3}^0$  and  $K_{e3}^0$  strangeness tagging at production and decay. Assumes  $CPT$  conservation on  $\Delta S = -\Delta Q$  transitions.

<sup>5</sup> Fits  $\Delta m$  and  $\phi_{+-}$  simultaneously. GIBBONS 93C systematic error is from B. Winstein via private communication.

<sup>6</sup> These two experiments have a common systematic error due to the uncertainty in the momentum scale, as pointed out in WAHL 89.

<sup>7</sup> ADLER 96C is the result of a fit which includes nearly the same data as entered into the “OUR FIT” value above.

<sup>8</sup> GIBBONS 93 value assume  $\phi_{+-} = \phi_{00} = \phi_{SW} = (43.7 \pm 0.2)^\circ$ .

<sup>9</sup> ARONSON 82 find that  $\Delta m$  may depend on the kaon energy.

<sup>10</sup> ARONSON 70 and CARNEGIE 71 use  $K_S^0$  mean life =  $(0.862 \pm 0.006) \times 10^{-10}$  s. We have not attempted to adjust these values for the subsequent change in the  $K_S^0$  mean life or in  $\eta_{+-}$ .

## $K_L^0$ MEAN LIFE

VALUE ( $10^{-8}$ s)	EVTS	DOCUMENT ID	TECN
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**5.17 ± 0.04 OUR FIT** Error includes scale factor of 1.1.

**5.15 ± 0.04 OUR AVERAGE**

5.154 ± 0.044	0.4M	VOSBURGH	72 CNTR
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5.15 ± 0.14		DEVLIN	67 CNTR
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• • • We do not use the following data for averages, fits, limits, etc. • • •

5.0 ± 0.5		<sup>11</sup> LOWYS	67 HLBC
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6.1 $\begin{smallmatrix} +1.5 \\ -1.2 \end{smallmatrix}$	1700	ASTBURY	65C CNTR
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5.3 ± 0.6		FUJII	64 OSPK
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5.1 $\begin{smallmatrix} +2.4 \\ -1.3 \end{smallmatrix}$	15	DARMON	62 FBC
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8.1 $\begin{smallmatrix} +3.2 \\ -2.4 \end{smallmatrix}$	34	BARDON	58 CNTR
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<sup>11</sup> Sum of partial decay rates.

## $K_L^0$ DECAY MODES

Mode	Fraction ( $\Gamma_i/\Gamma$ )	Scale factor/ Confidence level
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### Semileptonic modes

$\Gamma_1$ $\pi^\pm e^\mp \nu_{e3}$ Called $K_{e3}^0$ .	[a] (38.78 ± 0.27) %	S=1.1
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$\Gamma_2$ $\pi^- e^+ \nu_e$		
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$\Gamma_3$ $\pi^+ e^- \bar{\nu}_e$		
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$\Gamma_4$ $\pi^\pm \mu^\mp \nu_{\mu3}$ Called $K_{\mu3}^0$ .	[a] (27.17 ± 0.25) %	S=1.1
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$\Gamma_5$ $\pi^- \mu^+ \nu_\mu$		
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$\Gamma_6$ $\pi^+ \mu^- \bar{\nu}_\mu$		
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$\Gamma_7$ ( $\pi \mu$ atom) $\nu$	(1.06 ± 0.11) × 10 <sup>-7</sup>	
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$\Gamma_8$ $\pi^0 \pi^\pm e^\mp \nu$	[a] (5.18 ± 0.29) × 10 <sup>-5</sup>	
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### Hadronic modes, including Charge conjugation × Parity Violating (CPV) modes

$\Gamma_9$ $3\pi^0$	(21.11 ± 0.23) %	
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$\Gamma_{10}$ $\pi^+ \pi^- \pi^0$	(12.57 ± 0.19) %	S=1.7
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$\Gamma_{11}$ $\pi^+ \pi^-$	CPV (2.081 ± 0.026) × 10 <sup>-3</sup>	S=1.1
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$\Gamma_{12}$ $\pi^0 \pi^0$	CPV (9.40 ± 0.13) × 10 <sup>-4</sup>	
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### Semileptonic modes with photons

$\Gamma_{13}$ $\pi^\pm e^\mp \nu_e \gamma$	[a,b,c] (3.53 ± 0.06) × 10 <sup>-3</sup>	
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$\Gamma_{14}$ $\pi^\pm \mu^\mp \nu_\mu \gamma$	(5.7 $\begin{smallmatrix} +0.6 \\ -0.7 \end{smallmatrix}$ ) × 10 <sup>-4</sup>	
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### Hadronic modes with photons or $\ell\bar{\ell}$ pairs

$\Gamma_{15}$	$\pi^0\pi^0\gamma$		$< 5.6 \times 10^{-6}$	
$\Gamma_{16}$	$\pi^+\pi^-\gamma$	[b,c]	$(4.37 \pm 0.13) \times 10^{-5}$	S=1.9
$\Gamma_{17}$	$\pi^0 2\gamma$	[c]	$(1.40 \pm 0.12) \times 10^{-6}$	S=2.9
$\Gamma_{18}$	$\pi^0\gamma e^+e^-$		$(2.3 \pm 0.4) \times 10^{-8}$	

### Other modes with photons or $\ell\bar{\ell}$ pairs

$\Gamma_{19}$	$2\gamma$		$(5.93 \pm 0.07) \times 10^{-4}$	
$\Gamma_{20}$	$3\gamma$		$< 2.4 \times 10^{-7}$	CL=90%
$\Gamma_{21}$	$e^+e^-\gamma$		$(10.0 \pm 0.5) \times 10^{-6}$	S=1.5
$\Gamma_{22}$	$\mu^+\mu^-\gamma$		$(3.59 \pm 0.11) \times 10^{-7}$	S=1.3
$\Gamma_{23}$	$e^+e^-\gamma\gamma$	[c]	$(5.95 \pm 0.33) \times 10^{-7}$	
$\Gamma_{24}$	$\mu^+\mu^-\gamma\gamma$	[c]	$(1.0^{+0.8}_{-0.6}) \times 10^{-8}$	

### Charge conjugation $\times$ Parity ( $CP$ ) or Lepton Family number ( $LF$ ) violating modes, or $\Delta S = 1$ weak neutral current ( $S1$ ) modes

$\Gamma_{25}$	$\mu^+\mu^-$	$S1$	$(7.24 \pm 0.14) \times 10^{-9}$	
$\Gamma_{26}$	$e^+e^-$	$S1$	$(9^{+6}_{-4}) \times 10^{-12}$	
$\Gamma_{27}$	$\pi^+\pi^-e^+e^-$	$S1$ [c]	$(3.5 \pm 0.6) \times 10^{-7}$	
$\Gamma_{28}$	$\pi^0\pi^0e^+e^-$	$S1$	$< 6.6 \times 10^{-9}$	CL=90%
$\Gamma_{29}$	$\mu^+\mu^-e^+e^-$	$S1$	$(2.6 \pm 0.4) \times 10^{-9}$	
$\Gamma_{30}$	$e^+e^-e^+e^-$	$S1$	$(3.75 \pm 0.27) \times 10^{-8}$	
$\Gamma_{31}$	$\pi^0\mu^+\mu^-$	$CP,S1$ [d]	$< 3.8 \times 10^{-10}$	CL=90%
$\Gamma_{32}$	$\pi^0e^+e^-$	$CP,S1$ [d]	$< 5.1 \times 10^{-10}$	CL=90%
$\Gamma_{33}$	$\pi^0\nu\bar{\nu}$	$CP,S1$ [e]	$< 5.9 \times 10^{-7}$	CL=90%
$\Gamma_{34}$	$e^\pm\mu^\mp$	$LF$ [a]	$< 4.7 \times 10^{-12}$	CL=90%
$\Gamma_{35}$	$e^\pm e^\pm\mu^\mp\mu^\mp$	$LF$ [a]	$< 1.23 \times 10^{-10}$	CL=90%
$\Gamma_{36}$	$\pi^0\mu^\pm e^\mp$	$LF$ [a]	$< 6.2 \times 10^{-9}$	CL=90%

[a] The value is for the sum of the charge states or particle/antiparticle states indicated.

[b] Most of this radiative mode, the low-momentum  $\gamma$  part, is also included in the parent mode listed without  $\gamma$ 's.

[c] See the Particle Listings below for the energy limits used in this measurement.

[d] Allowed by higher-order electroweak interactions.

[e] Violates  $CP$  in leading order. Test of direct  $CP$  violation since the indirect  $CP$ -violating and  $CP$ -conserving contributions are expected to be suppressed.

## CONSTRAINED FIT INFORMATION

An overall fit to the mean life, 3 decay rate, and 15 branching ratios uses 49 measurements and one constraint to determine 9 parameters. The overall fit has a  $\chi^2 = 43.6$  for 41 degrees of freedom.

The following *off-diagonal* array elements are the correlation coefficients  $\langle \delta p_i \delta p_j \rangle / (\delta p_i \cdot \delta p_j)$ , in percent, from the fit to parameters  $p_i$ , including the branching fractions,  $x_i \equiv \Gamma_i / \Gamma_{\text{total}}$ . The fit constrains the  $x_i$  whose labels appear in this array to sum to one.

$x_4$	-39							
$x_9$	-47	-36						
$x_{10}$	-33	-33	-7					
$x_{11}$	-21	-18	23	23				
$x_{12}$	-26	-21	43	11	63			
$x_{16}$	-8	-7	9	9	37	24		
$x_{19}$	-39	-30	79	-2	33	56	12	
$\Gamma$	0	0	0	0	0	0	0	0
	$x_1$	$x_4$	$x_9$	$x_{10}$	$x_{11}$	$x_{12}$	$x_{16}$	$x_{19}$

	Mode	Rate ( $10^8 \text{ s}^{-1}$ )	Scale factor
$\Gamma_1$	$\pi^\pm e^\mp \nu_e$ Called $K_{e3}^0$ .	[a] $0.0750 \pm 0.0008$	1.1
$\Gamma_4$	$\pi^\pm \mu^\mp \nu_\mu$ Called $K_{\mu 3}^0$ .	[a] $0.0525 \pm 0.0007$	1.1
$\Gamma_9$	$3\pi^0$	$0.0408 \pm 0.0006$	
$\Gamma_{10}$	$\pi^+ \pi^- \pi^0$	$0.0243 \pm 0.0004$	1.5
$\Gamma_{11}$	$\pi^+ \pi^-$	$(4.02 \pm 0.06) \times 10^{-4}$	1.1
$\Gamma_{12}$	$\pi^0 \pi^0$	$(1.817 \pm 0.029) \times 10^{-4}$	
$\Gamma_{16}$	$\pi^+ \pi^- \gamma$	[b,c] $(8.45 \pm 0.26) \times 10^{-6}$	1.7
$\Gamma_{19}$	$2\gamma$	$(1.147 \pm 0.017) \times 10^{-4}$	

## $K_L^0$ DECAY RATES

$\Gamma(\pi^+ \pi^- \pi^0)$					$\Gamma_{10}$
VALUE ( $10^6 \text{ s}^{-1}$ )	EVTS	DOCUMENT ID	TECN	COMMENT	
<b><math>2.43 \pm 0.04</math> OUR FIT</b>	Error includes scale factor of 1.5.				
<b><math>2.38 \pm 0.09</math> OUR AVERAGE</b>					
$2.32^{+0.13}_{-0.15}$	192	BALDO-...	75	HLBC	Assumes <i>CP</i>
$2.35 \pm 0.20$	180	<sup>12</sup> JAMES	72	HBC	Assumes <i>CP</i>
$2.71 \pm 0.28$	99	CHO	71	DBC	Assumes <i>CP</i>

$2.12 \pm 0.33$	50	MEISNER	71	HBC	Assumes $CP$
$2.20 \pm 0.35$	53	WEBBER	70	HBC	Assumes $CP$
$2.62^{+0.28}_{-0.27}$	136	BEHR	66	HLBC	Assumes $CP$

• • • We do not use the following data for averages, fits, limits, etc. • • •

$2.5 \pm 0.3$	98	<sup>12</sup> JAMES	71	HBC	Assumes $CP$
$3.26 \pm 0.77$	18	ANDERSON	65	HBC	
$1.4 \pm 0.4$	14	FRANZINI	65	HBC	

<sup>12</sup>JAMES 72 is a final measurement and includes JAMES 71.

### $\Gamma(\pi^\pm e^\mp \nu_e)$ $\Gamma_1$

<u>VALUE (<math>10^6 \text{ s}^{-1}</math>)</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
<b><math>7.50 \pm 0.08</math> OUR FIT</b>	Error includes scale factor of 1.1.			
<b><math>7.7 \pm 0.5</math> OUR AVERAGE</b>				
$7.81 \pm 0.56$	620	CHAN	71	HBC
$7.52^{+0.85}_{-0.72}$		AUBERT	65	HLBC $\Delta S = \Delta Q, CP$ assumed

### $\Gamma(\pi^\pm e^\mp \nu_e) + \Gamma(\pi^\pm \mu^\mp \nu_\mu)$ $(\Gamma_1 + \Gamma_4)$

<u>VALUE (<math>10^6 \text{ s}^{-1}</math>)</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
<b><math>12.75 \pm 0.12</math> OUR FIT</b>	Error includes scale factor of 1.1.			
<b><math>11.9 \pm 0.6</math> OUR AVERAGE</b>	Error includes scale factor of 1.2.			
$12.4 \pm 0.7$	410	<sup>13</sup> BURGUN	72	HBC $K^+ p \rightarrow K^0 p \pi^+$
$13.1 \pm 1.3$	252	<sup>13</sup> WEBBER	71	HBC $K^- p \rightarrow n \bar{K}^0$
$11.6 \pm 0.9$	393	<sup>13,14</sup> CHO	70	DBC $K^+ n \rightarrow K^0 p$
$9.85^{+1.15}_{-1.05}$	109	<sup>13</sup> FRANZINI	65	HBC

• • • We do not use the following data for averages, fits, limits, etc. • • •

$8.47 \pm 1.69$	126	<sup>13</sup> MANN	72	HBC	$K^- p \rightarrow n \bar{K}^0$
$10.3 \pm 0.8$	335	<sup>14</sup> HILL	67	DBC	$K^+ n \rightarrow K^0 p$

<sup>13</sup>Assumes  $\Delta S = \Delta Q$  rule.

<sup>14</sup>CHO 70 includes events of HILL 67.

## $K_L^0$ BRANCHING RATIOS

### Semileptonic modes

### $[\Gamma(\pi^\pm e^\mp \nu_e) + \Gamma(\pi^\pm \mu^\mp \nu_\mu)] / \Gamma_{\text{total}}$ $(\Gamma_1 + \Gamma_4) / \Gamma$

<u>VALUE</u>	<u>DOCUMENT ID</u>
<b><math>0.6595 \pm 0.0029</math> OUR FIT</b>	Error includes scale factor of 1.3.

### $\Gamma(\pi^\pm \mu^\mp \nu_\mu) / \Gamma(\pi^\pm e^\mp \nu_e)$ $\Gamma_4 / \Gamma_1$

<u>VALUE</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>
<b><math>0.701 \pm 0.009</math> OUR FIT</b>			

### **$0.697^{+0.010}_{-0.009}$ OUR AVERAGE**

$0.702 \pm 0.011$	33k	CHO	80	HBC
$0.662 \pm 0.037$	10k	WILLIAMS	74	ASPK
$0.741 \pm 0.044$	6700	BRANDENB...	73	HBC
$0.662 \pm 0.030$	1309	EVANS	73	HLBC
$0.71 \pm 0.05$	770	BUDAGOV	68	HLBC

• • • We do not use the following data for averages, fits, limits, etc. • • •

$0.68 \pm 0.08$	3548	BASILE	70	OSPK
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$\Gamma((\pi\mu\text{atom})\nu)/\Gamma(\pi^\pm\mu^\mp\nu_\mu)$

$\Gamma_7/\Gamma_4$

VALUE (units $10^{-7}$ )	EVTS	DOCUMENT ID	TECN
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<b>3.90±0.39</b>	155	<sup>15</sup> ARONSON	86 SPEC
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• • • We do not use the following data for averages, fits, limits, etc. • • •

seen	18	COOMBES	76 WIRE
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<sup>15</sup> ARONSON 86 quote theoretical value of  $(4.31 \pm 0.08) \times 10^{-7}$ .

$\Gamma(\pi^0\pi^\pm e^\mp\nu)/\Gamma_{\text{total}}$

$\Gamma_8/\Gamma$

VALUE (units $10^{-5}$ )	CL%	EVTS	DOCUMENT ID	TECN
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**5.18±0.29 OUR AVERAGE**

5.16±0.20±0.22		729	MAKOFF	93 E731
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6.2 ±2.0		16	CARROLL	80c SPEC
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• • • We do not use the following data for averages, fits, limits, etc. • • •

<220	90	<sup>16</sup> DONALDSON	74 SPEC
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<sup>16</sup> DONALDSON 74 uses  $K_L^0 \rightarrow \pi^+\pi^-\pi^0$ /(all  $K_L^0$ ) decays = 0.126.

———— Hadronic modes, ————

———— including Charge conjugation×Parity Violating (CPV) modes ————

$\Gamma(3\pi^0)/\Gamma_{\text{total}}$

$\Gamma_9/\Gamma$

VALUE	EVTS	DOCUMENT ID	TECN
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**0.2111±0.0023 OUR FIT**

<b>0.2105±0.0028</b>	38k	<sup>17</sup> KREUTZ	95 NA31
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<sup>17</sup> KREUTZ 95 measure  $3\pi^0$ ,  $\pi^+\pi^-\pi^0$ , and  $\pi e\nu_e$  modes. They assume PDG 1992 values for  $\pi\mu\nu_\mu$ ,  $2\pi$ , and  $2\gamma$  modes.

$\Gamma(3\pi^0)/\Gamma(\pi^\pm e^\mp\nu_e)$

$\Gamma_9/\Gamma_1$

VALUE	EVTS	DOCUMENT ID	TECN
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**0.544±0.008 OUR FIT** Error includes scale factor of 1.1.

<b>0.545±0.004±0.009</b>	38k	<sup>18</sup> KREUTZ	95 NA31
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<sup>18</sup> KREUTZ 95 measurement excluded from fit because it is not independent of their  $\Gamma(3\pi^0)/\Gamma_{\text{total}}$  measurement, which is in the fit.

$\Gamma(3\pi^0)/[\Gamma(\pi^\pm e^\mp\nu_e) + \Gamma(\pi^\pm\mu^\mp\nu_\mu) + \Gamma(\pi^+\pi^-\pi^0)]$   $\Gamma_9/(\Gamma_1+\Gamma_4+\Gamma_{10})$

VALUE	EVTS	DOCUMENT ID	TECN	COMMENT
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**0.269±0.004 OUR FIT**

**0.260±0.011 OUR AVERAGE**

0.251±0.014	549	BUDAGOV	68 HLBC	ORSAY measur.
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0.277±0.021	444	BUDAGOV	68 HLBC	Ecole polytec.meas
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0.31 <sup>+0.07</sup> <sub>-0.06</sub>	29	KULYUKINA	68 CC	
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0.24 ±0.08	24	ANIKINA	64 CC	
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$\Gamma(3\pi^0)/\Gamma(\pi^+\pi^-\pi^0)$   $\Gamma_9/\Gamma_{10}$

<u>VALUE</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
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**1.678±0.032 OUR FIT** Error includes scale factor of 1.3.

**1.63 ±0.05 OUR AVERAGE** Error includes scale factor of 1.4.

1.611±0.014±0.034 38k <sup>19</sup>KREUTZ 95 NA31

1.80 ±0.13 1010 BUDAGOV 68 HLBC

2.0 ±0.6 188 ALEKSANYAN 64B FBC

• • • We do not use the following data for averages, fits, limits, etc. • • •

1.65 ±0.07 883 BARMIN 72B HLBC Error statistical only

<sup>19</sup>KREUTZ 95 excluded from fit because it is not independent of their  $\Gamma(3\pi^0)/\Gamma_{\text{total}}$  measurement, which is in the fit.

$\Gamma(\pi^+\pi^-\pi^0)/\Gamma_{\text{total}}$   $\Gamma_{10}/\Gamma$

<u>VALUE</u>	<u>DOCUMENT ID</u>
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**0.1257±0.0019 OUR FIT** Error includes scale factor of 1.7.

$\Gamma(\pi^+\pi^-\pi^0)/\Gamma(\pi^\pm e^\mp \nu_e)$   $\Gamma_{10}/\Gamma_1$

<u>VALUE</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>
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**0.324±0.006 OUR FIT** Error includes scale factor of 1.6.

**0.336±0.003±0.007** 28k KREUTZ 95 NA31

$\Gamma(\pi^+\pi^-\pi^0)/[\Gamma(\pi^\pm e^\mp \nu_e) + \Gamma(\pi^\pm \mu^\mp \nu_\mu) + \Gamma(\pi^+\pi^-\pi^0)]$   $\Gamma_{10}/(\Gamma_1+\Gamma_4+\Gamma_{10})$

<u>VALUE</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
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**0.1601±0.0024 OUR FIT** Error includes scale factor of 1.7.

**0.1588±0.0024 OUR AVERAGE** Error includes scale factor of 1.4. See the ideogram below.

0.163 ±0.003 6499 CHO 77 HBC

0.1605±0.0038 1590 ALEXANDER 73B HBC

0.146 ±0.004 3200 BRANDENB... 73 HBC

0.159 ±0.010 558 EVANS 73 HLBC

0.167 ±0.016 1402 KULYUKINA 68 CC

0.161 ±0.005 HOPKINS 67 HBC

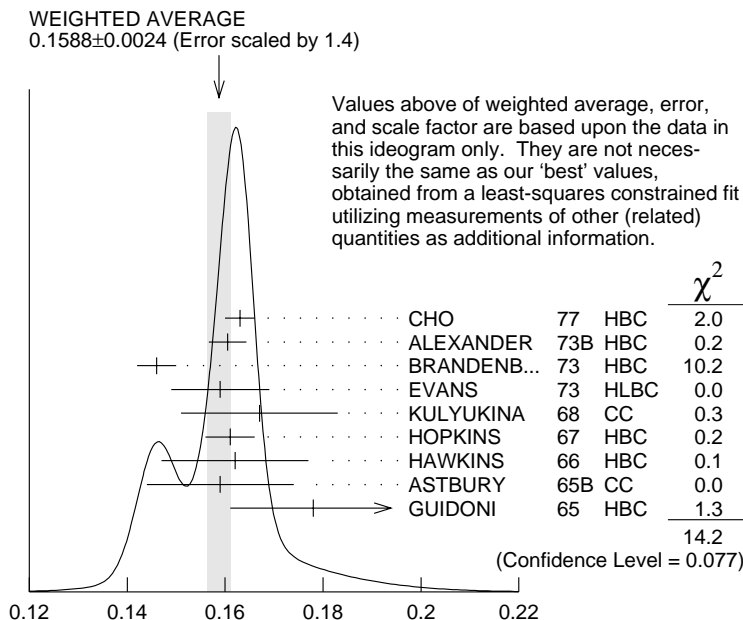
0.162 ±0.015 126 HAWKINS 66 HBC

0.159 ±0.015 326 ASTBURY 65B CC

0.178 ±0.017 566 GUIDONI 65 HBC

• • • We do not use the following data for averages, fits, limits, etc. • • •

0.144 ±0.004 1729 HOPKINS 65 HBC See HOPKINS 67



$$\Gamma(\pi^+ \pi^- \pi^0) / [\Gamma(\pi^\pm e^\mp \nu_e) + \Gamma(\pi^\pm \mu^\mp \nu_\mu) + \Gamma(\pi^+ \pi^- \pi^0)]$$

$\Gamma(\pi^+ \pi^-) / \Gamma_{\text{total}}$

Violates  $CP$  conservation.

$\Gamma_{11} / \Gamma$

VALUE (units  $10^{-3}$ )

DOCUMENT ID

**2.081±0.026 OUR FIT** Error includes scale factor of 1.1.

**2.075±0.049** <sup>20</sup> ETAFIT 02

<sup>20</sup> This ETAFIT value is computed from fitted values of  $|\eta_{+-}|$ , the  $K_L^0$  and  $K_S^0$  lifetimes, and the  $K_S^0 \rightarrow \pi^+ \pi^-$  branching fraction. See the discussion in the note "Fits for  $K_L^0$   $CP$ -Violation Parameters."

$\Gamma(\pi^+ \pi^-) / [\Gamma(\pi^\pm e^\mp \nu_e) + \Gamma(\pi^\pm \mu^\mp \nu_\mu)]$

Violates  $CP$  conservation.

$\Gamma_{11} / (\Gamma_1 + \Gamma_4)$

VALUE (units  $10^{-3}$ )

EVTS

DOCUMENT ID

TECN

COMMENT

**3.16±0.05 OUR FIT** Error includes scale factor of 1.1.

**3.08±0.10 OUR AVERAGE**

3.13±0.14 1687 COUPAL 85 SPEC  $\eta_{+-} = 2.28 \pm 0.06$

3.04±0.14 2703 DEVOE 77 SPEC  $\eta_{+-} = 2.25 \pm 0.05$

• • • We do not use the following data for averages, fits, limits, etc. • • •

2.51±0.23 309 <sup>21</sup> DEBOUARD 67 OSPK  $\eta_{+-} = 2.00 \pm 0.09$

2.35±0.19 525 <sup>21</sup> FITCH 67 OSPK  $\eta_{+-} = 1.94 \pm 0.08$

<sup>21</sup> Old experiments excluded from fit. See subsection on  $\eta_{+-}$  in section on "PARAMETERS FOR  $K_L^0 \rightarrow 2\pi$  DECAY" below for average  $\eta_{+-}$  of these experiments and for note on discrepancy.



$$\Gamma(\pi^+\pi^-)/[\Gamma(\pi^\pm e^\mp \nu_e) + \Gamma(\pi^\pm \mu^\mp \nu_\mu) + \Gamma(\pi^+\pi^-\pi^0)] \quad \Gamma_{11}/(\Gamma_1+\Gamma_4+\Gamma_{10})$$

Violates *CP* conservation.

VALUE (units $10^{-3}$ )	EVTS	DOCUMENT ID	TECN	COMMENT
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**2.65±0.04 OUR FIT** Error includes scale factor of 1.1.

• • • We do not use the following data for averages, fits, limits, etc. • • •

2.60±0.07	4200	<sup>22</sup> MESSNER	73	ASPK $\eta_{+-} = 2.23 \pm 0.05$
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<sup>22</sup> From same data as  $\Gamma(\pi^+\pi^-)/\Gamma(\pi^+\pi^-\pi^0)$  MESSNER 73, but with different normalization.

$$\Gamma(\pi^+\pi^-)/\Gamma(\pi^+\pi^-\pi^0) \quad \Gamma_{11}/\Gamma_{10}$$

Violates *CP* conservation.

VALUE (units $10^{-2}$ )	EVTS	DOCUMENT ID	TECN	COMMENT
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**1.655±0.028 OUR FIT** Error includes scale factor of 1.2.

<b>1.64 ±0.04</b>	4200	MESSNER	73	ASPK $\eta_{+-} = 2.23$
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$$\Gamma(\pi^0\pi^0)/\Gamma_{\text{total}} \quad \Gamma_{12}/\Gamma$$

Violates *CP* conservation.

VALUE (units $10^{-3}$ )	DOCUMENT ID
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**0.940±0.013 OUR FIT**

$$\Gamma(\pi^0\pi^0)/\Gamma(\pi^+\pi^-) \quad \Gamma_{12}/\Gamma_{11}$$

Violates *CP* conservation.

VALUE	DOCUMENT ID
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**0.452 ±0.005 OUR FIT**

<b>0.4528±0.0058</b>	<sup>23</sup> ETAFIT	02
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<sup>23</sup> This ETAFIT value is computed from fitted values of  $|\eta_{00} / \eta_{+-}|$  and the  $\Gamma(K_S^0 \rightarrow \pi^+\pi^-) / \Gamma(K_S^0 \rightarrow \pi^0\pi^0)$  branching fraction. See the discussion in the note "Fits for  $K_L^0$  *CP*-Violation Parameters."

$$\Gamma(\pi^0\pi^0)/\Gamma(3\pi^0) \quad \Gamma_{12}/\Gamma_9$$

Violates *CP* conservation.

VALUE (units $10^{-2}$ )	EVTS	DOCUMENT ID	TECN	COMMENT
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**0.445±0.006 OUR FIT**

**0.39 ±0.06 OUR AVERAGE**

0.37 ±0.08	29	BARMIN	70	HLBC $\eta_{00}=2.02 \pm 0.23$
0.32 ±0.15	30	BUDAGOV	70	HLBC $\eta_{00}=1.9 \pm 0.5$
0.46 ±0.11	57	BANNER	69	OSPK $\eta_{00}=2.2 \pm 0.3$

### ———— Semileptonic modes with photons ————

$$\Gamma(\pi^\pm e^\mp \nu_e \gamma)/\Gamma(\pi^\pm e^\mp \nu_e) \quad \Gamma_{13}/\Gamma_1$$

VALUE (units $10^{-2}$ )	EVTS	DOCUMENT ID	TECN	COMMENT
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**0.910±0.014 OUR AVERAGE**

$0.908 \pm 0.008^{+0.013}_{-0.012}$	15k	ALAVI-HARATI01J	KTEV	$E_\gamma^* \geq 30 \text{ MeV}$ , $\theta_{e\gamma}^* \geq 20^\circ$
$0.934 \pm 0.036^{+0.055}_{-0.039}$	1384	LEBER	96 NA31	$E_\gamma^* \geq 30 \text{ MeV}$ , $\theta_{e\gamma}^* \geq 20^\circ$

$\Gamma(\pi^\pm \mu^\mp \nu_\mu \gamma)/\Gamma(\pi^\pm \mu^\mp \nu_\mu)$ <span style="float:right"><math>\Gamma_{14}/\Gamma_4</math></span>					
VALUE (units $10^{-3}$ )	EVTS	DOCUMENT ID	TECN	COMMENT	
<b>2.08 ± 0.17<sup>+0.16</sup><sub>-0.21</sub></b>	4261	BENDER	98 NA48	$E_\gamma^* \geq 30$ MeV	

————— Hadronic modes with photons or  $\ell\bar{\ell}$  pairs —————

$\Gamma(\pi^0 \pi^0 \gamma)/\Gamma_{\text{total}}$ <span style="float:right"><math>\Gamma_{15}/\Gamma</math></span>					
VALUE (units $10^{-6}$ )	CL%	EVTS	DOCUMENT ID	TECN	COMMENT
< <b>5.6</b>			BARR	94 NA31	
• • • We do not use the following data for averages, fits, limits, etc. • • •					
<230	90	0	ROBERTS	94 E799	

$\Gamma(\pi^+ \pi^- \gamma)/\Gamma_{\text{total}}$ <span style="float:right"><math>\Gamma_{16}/\Gamma</math></span>					
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For earlier limits see our 1992 edition Physical Review **D45**, 1 June, Part II (1992).

VALUE (units $10^{-5}$ )	EVTS	DOCUMENT ID	TECN	COMMENT	
<b>4.37 ± 0.13 OUR FIT</b>	Error includes scale factor of 1.9.				
<b>4.61 ± 0.14 OUR AVERAGE</b>					
4.66 ± 0.15	3136	<sup>24</sup> RAMBERG	93 E731	$E_\gamma > 20$ MeV	
4.41 ± 0.32	1062	<sup>25</sup> CARROLL	80B SPEC	$E_\gamma > 20$ MeV	
• • • We do not use the following data for averages, fits, limits, etc. • • •					
1.52 ± 0.16	516	<sup>26</sup> CARROLL	80B SPEC	$E_\gamma > 20$ MeV	
2.89 ± 0.28	546	<sup>27</sup> CARROLL	80B SPEC		

<sup>24</sup> RAMBERG 93 finds that fraction of Direct Emission (DE) decays with  $E_\gamma > 20$  MeV is  $0.685 \pm 0.041$ .

<sup>25</sup> Both components. Uses  $K_L^0 \rightarrow \pi^+ \pi^- \pi^0 / (\text{all } K_L^0 \text{ decays}) = 0.1239$ .

<sup>26</sup> Internal Bremsstrahlung component only.

<sup>27</sup> Direct  $\gamma$  emission component only.

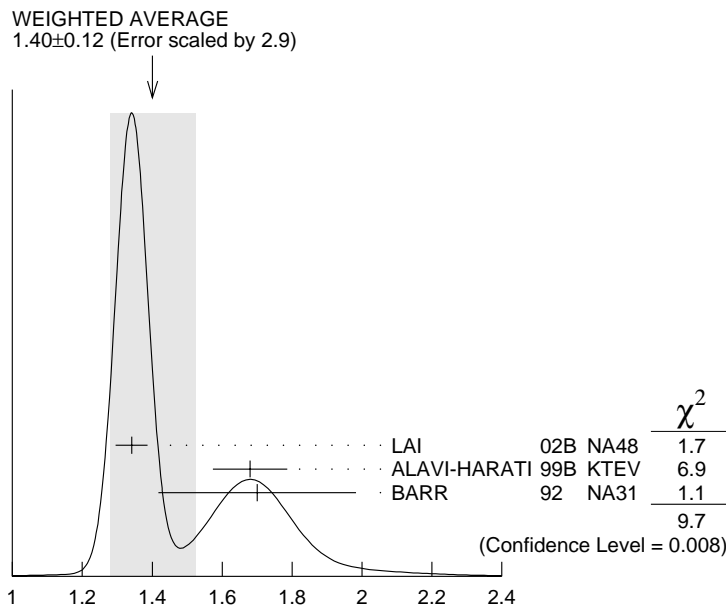
$\Gamma(\pi^+ \pi^- \gamma)/\Gamma(\pi^+ \pi^-)$ <span style="float:right"><math>\Gamma_{16}/\Gamma_{11}</math></span>					
VALUE (units $10^{-2}$ )	EVTS	DOCUMENT ID	TECN	COMMENT	
<b>2.10 ± 0.06 OUR FIT</b>	Error includes scale factor of 2.2.				
<b>2.08 ± 0.02 ± 0.02</b>	8669	<sup>28</sup> ALAVI-HARATI01B	KTEV	$E_\gamma^* > 20$ MeV	

<sup>28</sup> ALAVI-HARATI 01B includes both Direct Emission (DE) and Inner Bremsstrahlung (IB) processes. They also report  $DE/(DE+IB) = 0.683 \pm 0.011$ . The paper reports results for  $\rho$  propagator, linear, and quadratic form factors.

$\Gamma(\pi^0 2\gamma)/\Gamma_{\text{total}}$ <span style="float:right"><math>\Gamma_{17}/\Gamma</math></span>					
VALUE (units $10^{-6}$ )	CL%	EVTS	DOCUMENT ID	TECN	COMMENT
<b>1.40 ± 0.12 OUR AVERAGE</b>	Error includes scale factor of 2.9. See the ideogram below.				
1.34 ± 0.04 ± 0.02		2.5k	<sup>29</sup> LAI	02B NA48	
1.68 ± 0.07 ± 0.08		884	ALAVI-HARATI99B	KTEV	
1.7 ± 0.2 ± 0.2		63	<sup>30</sup> BARR	92 NA31	

• • • We do not use the following data for averages, fits, limits, etc. • • •					
1.86 ± 0.60 ± 0.60		60	PAPADIMITR...91	E731	$m_{\gamma\gamma} > 280$ MeV
<5.1	90		PAPADIMITR...91	E731	$m_{\gamma\gamma} < 264$ MeV
2.1 ± 0.6		14	<sup>31</sup> BARR	90C NA31	$m_{\gamma\gamma} > 280$ MeV

- <sup>29</sup> LAI 02B reports  $1.36 \pm 0.03 \pm 0.03$  for  $B(K_L^0 \rightarrow \pi^0 \pi^0) = 9.27 \times 10^{-4}$ . We rescale to our best value  $B(K_L^0 \rightarrow \pi^0 \pi^0) = (9.40 \pm 0.13) \times 10^{-4}$ . Our first error is their experiment's error and our second error is the systematic error from using our best value.
- <sup>30</sup> BARR 92 find that  $\Gamma(\pi^0 2\gamma, m_{\gamma\gamma} < 240 \text{ MeV})/\Gamma(\pi^0 2\gamma) < 0.09$  (90% CL).
- <sup>31</sup> BARR 90C superseded by BARR 92.



$$\Gamma(\pi^0 2\gamma)/\Gamma_{\text{total}} \quad \Gamma_{17}/\Gamma$$

$$\Gamma(\pi^0 \gamma e^+ e^-)/\Gamma_{\text{total}} \quad \Gamma_{18}/\Gamma$$

VALUE (units $10^{-8}$ )	CL%	EVTS	DOCUMENT ID	TECN
<b>2.34±0.35±0.13</b>		44	ALAVI-HARATI01E	KTEV

• • • We do not use the following data for averages, fits, limits, etc. • • •

<71	90	0	MURAKAMI 99	SPEC
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———— Other modes with photons or  $l\bar{l}$  pairs ————

$$\Gamma(2\gamma)/\Gamma_{\text{total}} \quad \Gamma_{19}/\Gamma$$

VALUE (units $10^{-4}$ )	EVTS	DOCUMENT ID	TECN	COMMENT
<b>5.93±0.07 OUR FIT</b>				

• • • We do not use the following data for averages, fits, limits, etc. • • •

4.54±0.84		32 BANNER	72B OSPK	
4.5 ±1.0	23	ENSTROM	71 OSPK	$K_L^0$ 1.5–9 GeV/c
5.0 ±1.0		33 REPELLIN	71 OSPK	
5.5 ±1.1	90	KUNZ	68 OSPK	Norm.to 3 $\pi(C+N)$

<sup>32</sup> This value uses  $(\eta_{00}/\eta_{+-})^2 = 1.05 \pm 0.14$ . In general,  $\Gamma(2\gamma)/\Gamma_{\text{total}} = [(4.32 \pm 0.55) \times 10^{-4}] [(\eta_{00}/\eta_{+-})^2]$ .

<sup>33</sup> Assumes regeneration amplitude in copper at 2 GeV is 22 mb. To evaluate for a given regeneration amplitude and error, multiply by  $(\text{regeneration amplitude}/22\text{mb})^2$ .

**$\Gamma(2\gamma)/\Gamma(3\pi^0)$   $\Gamma_{19}/\Gamma_9$**

<u>VALUE (units <math>10^{-3}</math>)</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
<b>2.811 ± 0.022 OUR FIT</b>				
<b>2.81 ± 0.01 ± 0.02</b>		LAI	03 NA48	
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●				
2.13 ± 0.43	28	BARMIN	71 HLBC	
2.24 ± 0.28	115	BANNER	69 OSPK	
2.5 ± 0.7	16	ARNOLD	68B HLBC	Vacuum decay

**$\Gamma(2\gamma)/\Gamma(\pi^0\pi^0)$   $\Gamma_{19}/\Gamma_{12}$**

<u>VALUE</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>
<b>0.631 ± 0.008 OUR FIT</b>			
<b>0.632 ± 0.004 ± 0.008</b>	110k	BURKHARDT	87 NA31

**$\Gamma(3\gamma)/\Gamma_{\text{total}}$   $\Gamma_{20}/\Gamma$**

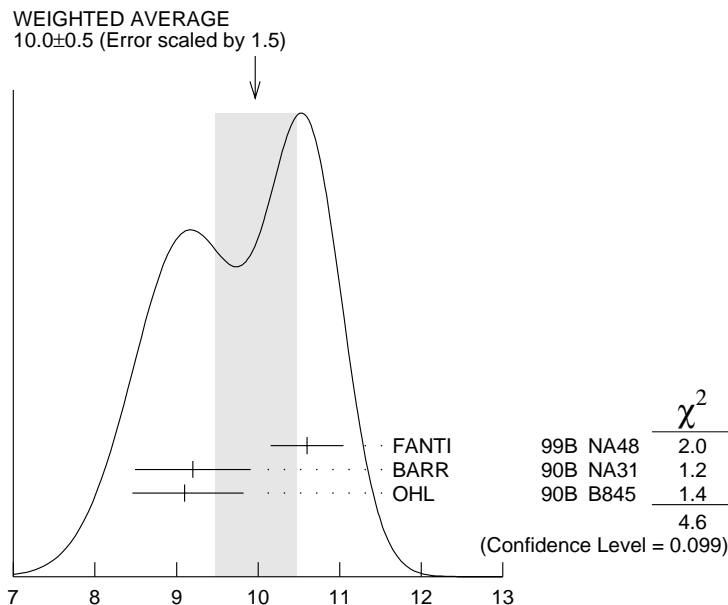
<u>VALUE</u>	<u>CL%</u>	<u>DOCUMENT ID</u>	<u>TECN</u>
<b>&lt; 2.4 × 10<sup>-7</sup></b>	90	<sup>34</sup> BARR	95C NA31

<sup>34</sup> Assumes a phase-space decay distribution.

**$\Gamma(e^+e^-\gamma)/\Gamma_{\text{total}}$   $\Gamma_{21}/\Gamma$**

<u>VALUE (units <math>10^{-6}</math>)</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>
<b>10.0 ± 0.5 OUR AVERAGE</b>			Error includes scale factor of 1.5. See the ideogram below.
10.6 ± 0.2 ± 0.4	6864	<sup>35</sup> FANTI	99B NA48
9.2 ± 0.5 ± 0.5	1053	BARR	90B NA31
9.1 ± 0.4 <sup>+0.6</sup> / <sub>-0.5</sub>	919	OHL	90B B845

<sup>35</sup> For FANTI 99B, the ±0.4 systematic error includes for uncertainties in the calculation, primarily uncertainties in the  $\pi^0 \rightarrow e^+e^-\gamma$  and  $K_L^0 \rightarrow \pi^0\pi^0$  branching ratios, evaluated using our 1999 Web edition values.



$$\Gamma(e^+ e^- \gamma) / \Gamma_{\text{total}} \text{ (units } 10^{-6}\text{)}$$

### $\Gamma(\mu^+ \mu^- \gamma) / \Gamma_{\text{total}}$

$\Gamma_{22} / \Gamma$

VALUE (units $10^{-7}$ )	EVTS	DOCUMENT ID	TECN
<b>3.59±0.11 OUR AVERAGE</b>		Error includes scale factor of 1.3.	
3.62±0.04±0.08	9100	ALAVI-HARATI01G	KTEV
3.4 ±0.6 ±0.4	45	FANTI	97 NA48
3.23±0.23±0.19	197	SPENCER	95 E799

### $\Gamma(e^+ e^- \gamma\gamma) / \Gamma_{\text{total}}$

$\Gamma_{23} / \Gamma$

VALUE (units $10^{-7}$ )	EVTS	DOCUMENT ID	TECN	COMMENT
<b>5.95±0.33 OUR AVERAGE</b>				
5.84±0.15±0.32	1543	ALAVI-HARATI01F	KTEV	$E_\gamma^* > 5 \text{ MeV}$
8.0 ±1.5 $\begin{smallmatrix} +1.4 \\ -1.2 \end{smallmatrix}$	40	SETZU	98 NA31	$E_\gamma > 5 \text{ MeV}$
6.5 ±1.2 ±0.6	58	NAKAYA	94 E799	$E_\gamma > 5 \text{ MeV}$
6.6 ±3.2		MORSE	92 B845	$E_\gamma > 5 \text{ MeV}$

### $\Gamma(\mu^+ \mu^- \gamma\gamma) / \Gamma_{\text{total}}$

$\Gamma_{24} / \Gamma$

VALUE (units $10^{-9}$ )	EVTS	DOCUMENT ID	TECN	COMMENT
<b>10.4 <math>\begin{smallmatrix} +7.5 \\ -5.9 \end{smallmatrix}</math> ±0.7</b>	4	ALAVI-HARATI00E	KTEV	$m_{\gamma\gamma} \geq 1 \text{ MeV}/c^2$

————— **Charge conjugation × Parity (CP) or Lepton Family number (LF)** —————  
 ————— **violating modes, or  $\Delta S = 1$  weak neutral current (SI) modes** —————

**$\Gamma(\mu^+ \mu^-)/\Gamma(\pi^+ \pi^-)$**   **$\Gamma_{25}/\Gamma_{11}$**   
 Test for  $\Delta S = 1$  weak neutral current. Allowed by higher-order electroweak interaction.

<u>VALUE (units <math>10^{-6}</math>)</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
<b>3.48 ± 0.05 OUR AVERAGE</b>				
3.474 ± 0.057	6210	AMBROSE	00 B871	
3.87 ± 0.30	179	<sup>36</sup> AKAGI	95 SPEC	
3.38 ± 0.17	707	HEINSON	95 B791	
• • • We do not use the following data for averages, fits, limits, etc. • • •				
3.9 ± 0.3 ± 0.1	178	<sup>37</sup> AKAGI	91B SPEC	In AKAGI 95
3.45 ± 0.18 ± 0.13	368	<sup>38</sup> HEINSON	91 SPEC	In HEINSON 95
4.1 ± 0.5	54	INAGAKI	89 SPEC	In AKAGI 91B
2.8 ± 0.3 ± 0.2	87	MATHIAZHA...	89B SPEC	In HEINSON 91

<sup>36</sup> AKAGI 95 gives this number multiplied by the PDG 1992 average for  $\Gamma(K_L^0 \rightarrow \pi^+ \pi^-)/\Gamma(\text{total})$ .

<sup>37</sup> AKAGI 91B give this number multiplied by the 1990 PDG average for  $\Gamma(K_L^0 \rightarrow \pi^+ \pi^-)/\Gamma(\text{total})$ .

<sup>38</sup> HEINSON 91 give  $\Gamma(K_L^0 \rightarrow \mu\mu)/\Gamma_{\text{total}}$ . We divide out the  $\Gamma(K_L^0 \rightarrow \pi^+ \pi^-)/\Gamma_{\text{total}}$  PDG average which they used.

**$\Gamma(e^+ e^-)/\Gamma_{\text{total}}$**   **$\Gamma_{26}/\Gamma$**   
 Test for  $\Delta S = 1$  weak neutral current. Allowed by higher-order electroweak interaction.

<u>VALUE (units <math>10^{-10}</math>)</u>	<u>CL%</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>
<b>0.087<sup>+0.057</sup><sub>-0.041</sub></b>		4	AMBROSE	98 B871

• • • We do not use the following data for averages, fits, limits, etc. • • •

<1.6                      90            1            AKAGI            95 SPEC

<0.41                    90            0            <sup>39</sup> ARISAKA        93B B791

<sup>39</sup> ARISAKA 93B includes all events with <6 MeV radiated energy.

**$\Gamma(\pi^+ \pi^- e^+ e^-)/\Gamma_{\text{total}}$**   **$\Gamma_{27}/\Gamma$**   
 Test for  $\Delta S = 1$  weak neutral current. Allowed by higher-order electroweak interaction.

<u>VALUE (units <math>10^{-7}</math>)</u>	<u>CL%</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
<b>3.5 ± 0.6 OUR AVERAGE</b>					
3.2 ± 0.6 ± 0.4		37	ADAMS	98 KTEV	
4.4 ± 1.3 ± 0.5		13	TAKEUCHI	98 SPEC	

• • • We do not use the following data for averages, fits, limits, etc. • • •

<4.6                      90                      NOMURA            97 SPEC         $m_{ee} > 4$  MeV

**$\Gamma(\pi^0 \pi^0 e^+ e^-)/\Gamma_{\text{total}}$**   **$\Gamma_{28}/\Gamma$**   
 Test for  $\Delta S = 1$  weak neutral current. Allowed by higher-order electroweak interaction.

<u>VALUE (units <math>10^{-9}</math>)</u>	<u>CL%</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>
<b>&lt;6.6</b>	90	1	ALAVI-HARATI02C	E799

$\Gamma(\mu^+ \mu^- e^+ e^-)/\Gamma_{\text{total}}$   $\Gamma_{29}/\Gamma$

Test for  $\Delta S = 1$  weak neutral current. Allowed by higher-order electroweak interaction.

VALUE (units $10^{-9}$ )	CL%	EVTS	DOCUMENT ID	TECN
<b>2.6 ± 0.4</b>				
<b>OUR AVERAGE</b>				
2.62 ± 0.40 ± 0.17		43	ALAVI-HARATI01H	KTEV
2.9 <sup>+6.7</sup> <sub>-2.4</sub>		1	GU	96 E799

• • • We do not use the following data for averages, fits, limits, etc. • • •

<4900	90		BALATS	83 SPEC
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$\Gamma(e^+ e^- e^+ e^-)/\Gamma_{\text{total}}$   $\Gamma_{30}/\Gamma$

Test for  $\Delta S = 1$  weak neutral current. Allowed by higher-order electroweak interaction.

VALUE (units $10^{-8}$ )	CL%	EVTS	DOCUMENT ID	TECN	COMMENT
<b>3.75 ± 0.27</b>					
<b>OUR AVERAGE</b>					
3.72 ± 0.18 ± 0.23		441	ALAVI-HARATI01D	KTEV	
6 ± 2 ± 1		18	<sup>40</sup> AKAGI	95 SPEC	$m_{ee} > 470$ MeV
3.96 ± 0.78 ± 0.32		27	GU	94 E799	
3.07 ± 1.25 ± 0.26		6	VAGINS	93 B845	

• • • We do not use the following data for averages, fits, limits, etc. • • •

7 ± 3 ± 2		6	<sup>40</sup> AKAGI	95 SPEC	$m_{ee} > 470$ MeV
10.4 ± 3.7 ± 1.1		8	<sup>41</sup> BARR	95 NA31	
6 ± 2 ± 1		18	AKAGI	93 CNTR	Sup. by AKAGI 95
4 ± 3		2	BARR	91 NA31	Sup. by BARR 95

<sup>40</sup> Values are for the total branching fraction, acceptance-corrected for the  $m_{ee}$  cuts shown.

<sup>41</sup> Distribution of angles between two  $e^+ e^-$  pair planes favors  $CP = -1$  for  $K_L^0$ .

$\Gamma(\pi^0 \mu^+ \mu^-)/\Gamma_{\text{total}}$   $\Gamma_{31}/\Gamma$

Violates  $CP$  in leading order. Test for  $\Delta S = 1$  weak neutral current. Allowed by higher-order electroweak interaction.

VALUE (units $10^{-9}$ )	CL%	EVTS	DOCUMENT ID	TECN
<b>&lt;0.38</b>				
	90		ALAVI-HARATI00D	KTEV

• • • We do not use the following data for averages, fits, limits, etc. • • •

<5.1	90	0	HARRIS	93 E799
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$\Gamma(\pi^0 e^+ e^-)/\Gamma_{\text{total}}$   $\Gamma_{32}/\Gamma$

Violates  $CP$  in leading order. Direct and indirect  $CP$ -violating contributions are expected to be comparable and to dominate the  $CP$ -conserving part. LAI 02B result suggests that  $CP$ -violation effects dominate. Test for  $\Delta S = 1$  weak neutral current. Allowed by higher-order electroweak interaction.

VALUE (units $10^{-10}$ )	CL%	EVTS	DOCUMENT ID	TECN	COMMENT
<b>&lt; 5.1</b>					
	90	2	ALAVI-HARATI01	KTEV	

• • • We do not use the following data for averages, fits, limits, etc. • • •

0.0047 <sup>+0.0022</sup> <sub>-0.0018</sub>			<sup>42</sup> LAI	02B NA48	$CP$ -conserving part
< 43	90	0	HARRIS	93B E799	
< 75	90	0	BARKER	90 E731	
< 55	90	0	OHL	90 B845	
< 400	90		BARR	88 NA31	
< 3200	90		JASTRZEM...	88 SPEC	

<sup>42</sup> LAI 02B uses the absence of a signal in  $K_L^0 \rightarrow \pi^0 \gamma \gamma$  with  $m(\gamma \gamma) < m(\pi^0)$  and their  $a_V$  value to predict this value.

$\Gamma(\pi^0 \nu \bar{\nu})/\Gamma_{\text{total}}$

$\Gamma_{33}/\Gamma$

Violates *CP* in leading order. Test of direct *CP* violation since the indirect *CP*-violating and *CP*-conserving contributions are expected to be suppressed. Test of  $\Delta S = 1$  weak neutral current.

VALUE (units $10^{-5}$ )	CL%	EVTS	DOCUMENT ID	TECN
< 0.059	90	0	ALAVI-HARATI00	KTEV
< 0.16	90	0	ADAMS	99 KTEV
< 5.8	90	0	WEAVER	94 E799
< 22	90	0	GRAHAM	92 CNTR

$\Gamma(e^\pm \mu^\mp)/\Gamma_{\text{total}}$

$\Gamma_{34}/\Gamma$

Test of lepton family number conservation.

VALUE (units $10^{-11}$ )	CL%	EVTS	DOCUMENT ID	TECN
< 0.47	90		AMBROSE	98B B871
< 9.4	90	0	AKAGI	95 SPEC
< 3.9	90	0	ARISAKA	93 B791
< 3.3	90	0	<sup>43</sup> ARISAKA	93 B791

<sup>43</sup>This is the combined result of ARISAKA 93 and MATHIAZHAGAN 89.

$\Gamma(e^\pm e^\pm \mu^\mp \mu^\mp)/\Gamma_{\text{total}}$

$\Gamma_{35}/\Gamma$

Test of lepton family number conservation.

VALUE (units $10^{-10}$ )	CL%	EVTS	DOCUMENT ID	TECN
< 1.23	90	64	<sup>44</sup> ALAVI-HARATI01H	KTEV
< 61	90	0	<sup>44</sup> GU	96 E799

<sup>44</sup>Assuming uniform phase space distribution.

$\Gamma(\pi^0 \mu^\pm e^\mp)/\Gamma_{\text{total}}$

$\Gamma_{36}/\Gamma$

Test of lepton family number conservation.

VALUE	CL%	DOCUMENT ID	TECN
< $6.2 \times 10^{-9}$	90	ARISAKA	98 E799

**ENERGY DEPENDENCE OF  $K_L^0$  DALITZ PLOT**

For discussion, see note on Dalitz plot parameters in the  $K^\pm$  section of the Particle Listings above. For definitions of  $a_v$ ,  $a_t$ ,  $a_u$ , and  $a_y$ , see the earlier version of the same note in the 1982 edition of this *Review* published in Physics Letters **111B** 70 (1982).

$$|\text{matrix element}|^2 = 1 + gu + hu^2 + jv + kv^2 + fuv$$

where  $u = (s_3 - s_0) / m_\pi^2$  and  $v = (s_1 - s_2) / m_\pi^2$

**LINEAR COEFFICIENT  $g$  FOR  $K_L^0 \rightarrow \pi^+ \pi^- \pi^0$**

VALUE	EVTS	DOCUMENT ID	TECN	COMMENT
<b>0.678 ± 0.008</b>	<b>OUR AVERAGE</b>	Error includes scale factor of 1.5. See the ideogram below.		
0.6823 ± 0.0044 ± 0.0044	500k	ANGELOPO...	98c	CPLR
0.681 ± 0.024	6499	CHO	77	HBC
0.620 ± 0.023	4709	PEACH	77	HBC
0.677 ± 0.010	509k	MESSNER	74	ASPK $a_y = -0.917 \pm 0.013$



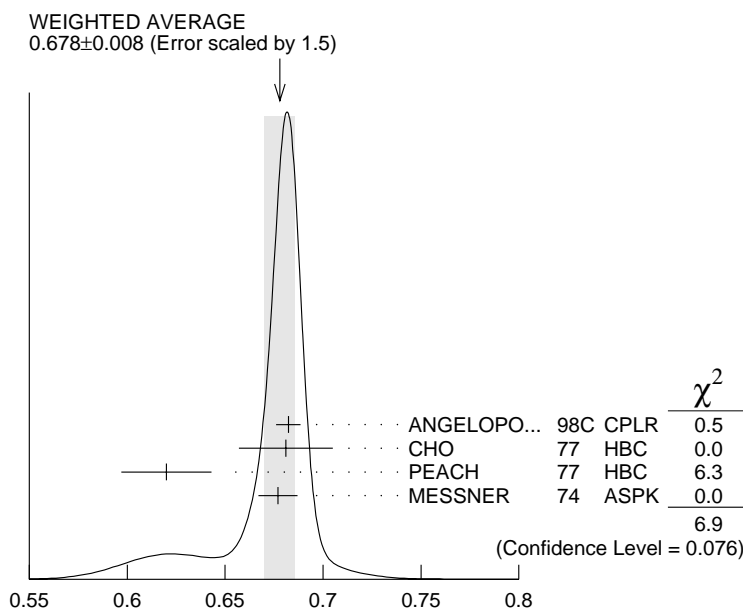
• • • We do not use the following data for averages, fits, limits, etc. • • •

0.69 ±0.07	192	<sup>45</sup> BALDO-...	75	HLBC	
0.590 ±0.022	56k	<sup>45</sup> BUCHANAN	75	SPEC	$a_U = -0.277 \pm 0.010$
0.619 ±0.027	20k	<sup>45,46</sup> BISI	74	ASPK	$a_t = -0.282 \pm 0.011$
0.612 ±0.032		<sup>45</sup> ALEXANDER	73B	HBC	
0.73 ±0.04	3200	<sup>45</sup> BRANDENB...	73	HBC	
0.608 ±0.043	1486	<sup>45</sup> KRENZ	72	HLBC	$a_t = -0.277 \pm 0.018$
0.650 ±0.012	29k	<sup>45</sup> ALBROW	70	ASPK	$a_y = -0.858 \pm 0.015$
0.593 ±0.022	36k	<sup>45,47</sup> BUCHANAN	70	SPEC	$a_U = -0.278 \pm 0.010$
0.664 ±0.056	4400	<sup>45</sup> SMITH	70	OSPK	$a_t = -0.306 \pm 0.024$
0.400 ±0.045	2446	<sup>45</sup> BASILE	68B	OSPK	$a_t = -0.188 \pm 0.020$
0.649 ±0.044	1350	<sup>45</sup> HOPKINS	67	HBC	$a_t = -0.294 \pm 0.018$
0.428 ±0.055	1198	<sup>45</sup> NEFKENS	67	OSPK	$a_U = -0.204 \pm 0.025$

<sup>45</sup> Quadratic dependence required by some experiments. (See sections on "QUADRATIC COEFFICIENT *h*" and "QUADRATIC COEFFICIENT *k*" below.) Correlations prevent us from averaging results of fits not including *g*, *h*, and *k* terms.

<sup>46</sup> BISI 74 value comes from quadratic fit with quad. term consistent with zero. *g* error is thus larger than if linear fit were used.

<sup>47</sup> BUCHANAN 70 result revised by BUCHANAN 75 to include radiative correlations and to use more reliable  $K_L^0$  momentum spectrum of second experiment (had same beam).



Linear coeff. *g* for  $K_L^0 \rightarrow \pi^+ \pi^- \pi^0$  matrix element squared

### QUADRATIC COEFFICIENT $h$ FOR $K_L^0 \rightarrow \pi^+ \pi^- \pi^0$

<u>VALUE</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>
<b>0.076 ± 0.006 OUR AVERAGE</b>			
0.061 ± 0.004 ± 0.015	500k	ANGELOPO...	98C CPLR
0.095 ± 0.032	6499	CHO	77 HBC
0.048 ± 0.036	4709	PEACH	77 HBC
0.079 ± 0.007	509k	MESSNER	74 ASPK

• • • We do not use the following data for averages, fits, limits, etc. • • •

-0.011 ± 0.018	29k	<sup>48</sup> ALBROW	70 ASPK
0.043 ± 0.052	4400	<sup>48</sup> SMITH	70 OSPK

See notes in section "LINEAR COEFFICIENT  $g$  FOR  $K_L^0 \rightarrow \pi^+ \pi^- \pi^0$  | MATRIX ELEMENT<sup>2</sup>" above.

<sup>48</sup> Quadratic coefficients  $h$  and  $k$  required by some experiments. (See section on "QUADRATIC COEFFICIENT  $k$ " below.) Correlations prevent us from averaging results of fits not including  $g$ ,  $h$ , and  $k$  terms.

### QUADRATIC COEFFICIENT $k$ FOR $K_L^0 \rightarrow \pi^+ \pi^- \pi^0$

<u>VALUE</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>
<b>0.0099 ± 0.0015 OUR AVERAGE</b>			
0.0104 ± 0.0017 ± 0.0024	500k	ANGELOPO...	98C CPLR
0.024 ± 0.010	6499	CHO	77 HBC
-0.008 ± 0.012	4709	PEACH	77 HBC
0.0097 ± 0.0018	509k	MESSNER	74 ASPK

### LINEAR COEFFICIENT $j$ FOR $K_L^0 \rightarrow \pi^+ \pi^- \pi^0$ ( $CP$ -VIOLATING TERM)

Listed in  $CP$ -violation section below.

### QUADRATIC COEFFICIENT $f$ FOR $K_L^0 \rightarrow \pi^+ \pi^- \pi^0$ ( $CP$ -VIOLATING TERM)

Listed in  $CP$ -violation section below.

### QUADRATIC COEFFICIENT $h$ FOR $K_L^0 \rightarrow \pi^0 \pi^0 \pi^0$

<u>VALUE (units <math>10^{-3}</math>)</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>
<b>-5.0 ± 1.4 OUR AVERAGE</b> Error includes scale factor of 1.7.			
-6.1 ± 0.9 ± 0.5	14.7M	LAI	01B NA48
-3.3 ± 1.1 ± 0.7	5M	<sup>49</sup> SOMALWAR	92 E731

<sup>49</sup> SOMALWAR 92 chose  $m_{\pi^+}$  as normalization to make it compatible with the Particle Data Group  $K_L^0 \rightarrow \pi^+ \pi^- \pi^0$  definitions.

## $K_L^0$ FORM FACTORS

For discussion, see note on form factors in the  $K^\pm$  section of the Particle Listings above.

In the form factor comments, the following symbols are used.

$f_+$  and  $f_-$  are form factors for the vector matrix element.

$f_S$  and  $f_T$  refer to the scalar and tensor term.

$$f_0 = f_+ + f_- t / (m_K^2 - m_\pi^2).$$

$\lambda_+$ ,  $\lambda_-$ , and  $\lambda_0$  are the linear expansion coefficients of  $f_+$ ,  $f_-$ , and  $f_0$ .

$\lambda_+$  refers to the  $K_{\mu 3}^0$  value except in the  $K_{e 3}^0$  sections.

$d\xi(0)/d\lambda_+$  is the correlation between  $\xi(0)$  and  $\lambda_+$  in  $K_{\mu 3}^0$ .

$d\lambda_0/d\lambda_+$  is the correlation between  $\lambda_0$  and  $\lambda_+$  in  $K_{\mu 3}^0$ .

$t$  = momentum transfer to the  $\pi$  in units of  $m_\pi^2$ .

DP = Dalitz plot analysis.

PI =  $\pi$  spectrum analysis.

MU =  $\mu$  spectrum analysis.

POL =  $\mu$  polarization analysis.

BR =  $K_{\mu 3}^0/K_{e 3}^0$  branching ratio analysis.

E = positron or electron spectrum analysis.

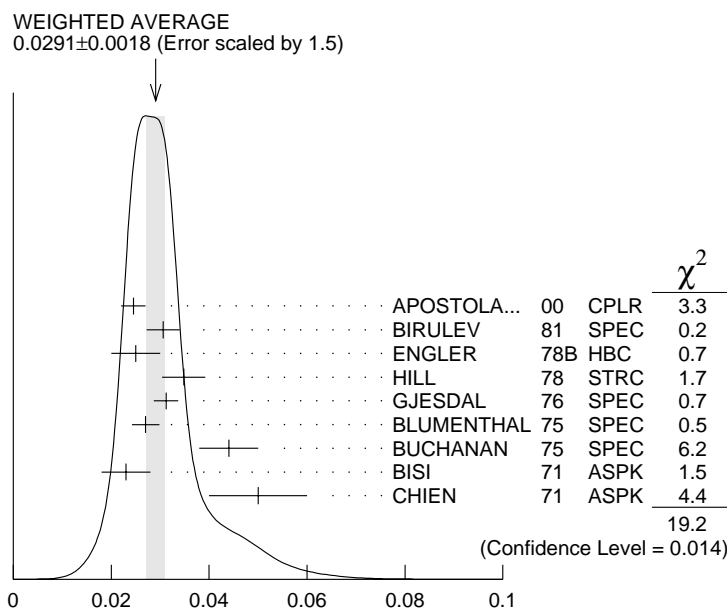
RC = radiative corrections.

### $\lambda_+$ (LINEAR ENERGY DEPENDENCE OF $f_+$ IN $K_{e 3}^0$ DECAY)

For radiative correction of  $K_{e 3}^0$  DP, see GINSBERG 67 and BECHERRAWY 70. Results labeled OUR FIT are discussed in the review " $K_{\ell 3}^\pm$  and  $K_{\ell 3}^0$  Form Factors" in the  $K^\pm$  Listings.

VALUE	EVTS	DOCUMENT ID	TECN	COMMENT
<b>0.0300 ± 0.0020 OUR FIT</b>	Error	includes scale factor of 2.0. Assumes $\mu$ -e universality.		
<b>0.0291 ± 0.0018 OUR AVERAGE</b>	Error	includes scale factor of 1.5. See the ideogram below.		
0.0245 ± 0.0012 ± 0.0022	366k	APOSTOLA...	00 CPLR	DP
0.0306 ± 0.0034	74k	BIRULEV	81 SPEC	DP
0.025 ± 0.005	12k	<sup>50</sup> ENGLER	78B HBC	DP
0.0348 ± 0.0044	18k	HILL	78 STRC	DP
0.0312 ± 0.0025	500k	GJESDAL	76 SPEC	DP
0.0270 ± 0.0028	25k	BLUMENTHAL75	SPEC	DP
0.044 ± 0.006	24k	BUCHANAN	75 SPEC	DP
0.023 ± 0.005	42k	BISI	71 ASPK	DP
0.05 ± 0.01	16k	CHIEN	71 ASPK	DP, no RC
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●				
0.029 ± 0.005	19k	<sup>50</sup> CHO	80 HBC	DP
0.040 ± 0.012	2171	WANG	74 OSPK	DP
0.045 ± 0.014	5600	ALBROW	73 ASPK	DP
0.019 ± 0.013	1871	BRANDENB...	73 HBC	PI transv.
0.022 ± 0.014	1910	NEUHOFER	72 ASPK	PI
0.02 ± 0.013	1000	ARONSON	68 OSPK	PI
+0.023 ± 0.012	4800	BASILE	68 OSPK	DP, no RC

<sup>50</sup> ENGLER 78B uses an unique  $K_{e3}$  subset of CHO 80 events and is less subject to systematic effects.



$\lambda_+$  (Linear energy dependence of  $f_+$ ,  $K_{e3}$  decay)

**$\xi_A = f_-/f_+$  (determined from  $K_{\mu 3}^0$  spectra)**

Results labeled OUR FIT are discussed in the review “ $K_{\ell 3}^\pm$  and  $K_{\ell 3}^0$  Form Factors” in the  $K^\pm$  Listings.  $\xi_A$  is  $\xi(0)$  determined by Method A of that review. The parameter  $\xi(0)$  is redundant with  $\lambda_0$  below and is not put into the Meson Summary Table.

VALUE	$d\xi(0)/d\lambda_+$	EVTS	DOCUMENT ID	TECN	COMMENT
<b>-0.01 ± 0.06 OUR FIT</b>					Error includes scale factor of 2.0. Correlation is $d\xi(0)/d\lambda_+ = -13.2$ . Assumes $\mu$ - $e$ universality.
<b>-0.08 ± 0.09 OUR FIT</b>					Error includes scale factor of 2.3. Correlation is $d\xi(0)/d\lambda_+ = -13.7$ .
-0.10 ± 0.09	-12	150k	51 BIRULEV	81 SPEC	DP
+0.26 ± 0.16	-13	14k	52 CHO	80 HBC	DP
+0.13 ± 0.23	-20	16k	52 HILL	79 STRC	DP
-0.25 ± 0.22	-5.9	32k	53 BUCHANAN	75 SPEC	DP
-0.11 ± 0.07	-17	1.6M	54 DONALDSON	74B SPEC	DP
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●					
-1.00 ± 0.45	-20	1385	55 PEACH	73 HLBC	DP
-1.5 ± 0.7	-28	9086	56 ALBROW	72 ASPK	DP
+0.50 ± 0.61	unknown	16k	57 DALLY	72 ASPK	DP
-3.9 ± 0.4		3140	58 BASILE	70 OSPK	DP, indep of $\lambda_+$
-0.68 <sup>+0.12</sup> / <sub>-0.20</sub>	-26	16k	57 CHIEN	70 ASPK	DP
+1.2 ± 0.8	-18	1341	59 CARPENTER	66 OSPK	DP

- 51 BIRULEV 81 error,  $d\xi(0)/d\lambda_+$  calculated by us from  $\lambda_0, \lambda_+$ .  $d\lambda_0/d\lambda_+ = 0$  used.
- 52 HILL 79 and CHO 80 calculated by us from  $\lambda_0, \lambda_+$ , and  $d\lambda_0/d\lambda_+$ .
- 53 BUCHANAN 75 is calculated by us from  $\lambda_0, \lambda_+$  and  $d\lambda_0/d\lambda_+$  because their appendix A value  $-0.20 \pm 22$  assumes  $\xi(t)$  constant, i.e.  $\lambda_- = \lambda_+$ .
- 54 DONALDSON 74B gives  $\xi = -0.11 \pm 0.02$  not including systematics. Above error and  $d\xi(0)/d\lambda_+$  were calculated by us from  $\lambda_0$  and  $\lambda_+$  errors (which include systematics) and  $d\lambda_0/d\lambda_+$ .
- 55 PEACH 73 gives  $\xi(0) = -0.95 \pm 0.45$  for  $\lambda_+ = \lambda_- = 0.025$ . The above value is for  $\lambda_- = 0$ . K.Peach, private communication (1974).
- 56 ALBROW 72 fit has  $\lambda_-$  free, gets  $\lambda_- = -0.030 \pm 0.060$  or  $\Lambda = +0.15^{+0.17}_{-0.11}$ .
- 57 CHIEN 70 errors are statistical only.  $d\xi(0)/d\lambda_+$  from figure 4. DALLY 72 is a reanalysis of CHIEN 70. The DALLY 72 result is not compatible with assumption  $\lambda_- = 0$  so not included in our fit. The nonzero  $\lambda_-$  value and the relatively large  $\lambda_+$  value found by DALLY 72 come mainly from a single low  $t$  bin (figures 1,2). The  $(f_+, \xi)$  correlation was ignored. We estimate from figure 2 that fixing  $\lambda_- = 0$  would give  $\xi(0) = -1.4 \pm 0.3$  and would add 10 to  $\chi^2$ .  $d\xi(0)/d\lambda_+$  is not given.
- 58 BASILE 70 is incompatible with all other results. Authors suggest that efficiency estimates might be responsible.
- 59 CARPENTER 66  $\xi(0)$  is for  $\lambda_+ = 0$ .  $d\xi(0)/d\lambda_+$  is from figure 9.

### $\xi_B = f_-/f_+$ (determined from $K_{\mu 3}^0/K_{e 3}^0$ )

The  $K_{\mu 3}^0/K_{e 3}^0$  branching ratio fixes a relationship between  $\xi(0)$  and  $\lambda_+$  if  $\mu$ - $e$  universality is assumed. We quote the author's  $\xi(0)$  and associated  $\lambda_+$  but do not average because the  $\lambda_+$  values differ. The result labeled OUR FIT below does not use these  $\xi_b$  values. Instead it uses the authors  $K_{\mu 3}^0/K_{e 3}^0$  branching ratios to obtain the fitted  $K_{\mu 3}^0/K_{e 3}^0$  ratio which is then converted to the KL3FIT value below, as discussed in the review " $K_{\ell 3}^\pm$  and  $K_{\ell 3}^0$  Form Factors" in the  $K^\pm$  Listings.  $\xi_B$  is  $\xi(0)$  determined by Method B of that review. The parameter  $\xi(0)$  is redundant with  $\lambda_0$  below and is not put into the Meson Summary Table.

VALUE	EVTS	DOCUMENT ID	TECN	COMMENT
<b><math>-0.01 \pm 0.06</math> OUR FIT</b>				Error includes scale factor of 2.0. Correlation is $d\xi/d\lambda_+ = -13.2$ . Assumes $\mu$ - $e$ universality.
$0.12 \pm 0.07$		<sup>60</sup> KL3FIT	02	RVUE $\lambda_+ = 0.030$
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●				
$0.5 \pm 0.4$	6700	BRANDENB...	73	HBC BR, $\lambda_+ = 0.019 \pm 0.013$
$-0.08 \pm 0.25$	1309	<sup>61</sup> EVANS	73	HLBC BR, $\lambda_+ = 0.02$
$-0.5 \pm 0.5$	3548	BASILE	70	OSPK BR, $\lambda_+ = 0.02$
$+0.45 \pm 0.28$	569	BEILLIERE	69	HLBC BR, $\lambda_+ = 0$
$-0.22 \pm 0.30$	1309	<sup>61</sup> EVANS	69	HLBC
$+0.2^{+0.8}_{-1.2}$		KULYUKINA	68	CC BR, $\lambda_+ = 0$
$+1.1 \pm 1.1$	389	ADAIR	64	HBC BR, $\lambda_+ = 0$
$+0.66^{+0.9}_{-1.3}$		LUERS	64	HBC BR, $\lambda_+ = 0$

<sup>60</sup> KL3FIT value is from fitted  $K_{\mu 3}^0/K_{e 3}^0$  branching ratio.  $d\xi(0)/d\lambda_+ = -10.2$ .

<sup>61</sup> EVANS 73 replaces EVANS 69.

### $\xi_C = f_-/f_+$ (determined from $\mu$ polarization in $K_{\mu 3}^0$ )

The  $\mu$  polarization is a measure of  $\xi(t)$ . No assumptions on  $\lambda_{+-}$  are necessary, but  $t$  (weighted by sensitivity to  $\xi(t)$ ) should be specified. In  $\lambda_+$ ,  $\xi(0)$  parametrization this is  $\xi(0)$  for  $\lambda_+ = 0$ .  $d\xi/d\lambda = \xi t$ . For radiative correction to  $\mu$  polarization in  $K_{\mu 3}^0$ , see GINSBERG 73. Results labeled OUR FIT are discussed in the review “ $K_{\ell 3}^{\pm}$  and  $K_{\ell 3}^0$  Form Factors” in the  $K^{\pm}$  Listings.  $\xi_C$  is  $\xi(0)$  determined by Method C of that review. The parameter  $\xi(0)$  is redundant with  $\lambda_0$  below and is not put into the Meson Summary Table.

VALUE	EVTS	DOCUMENT ID	TECN	COMMENT
<b>-0.01 ± 0.06 OUR FIT</b>				Error includes scale factor of 2.0. Correlation is $d\xi(0)/d\lambda_+ = -13.2$ . Assumes $\mu$ -e universality.
<b>-0.08 ± 0.09 OUR FIT</b>				Error includes scale factor of 2.3. Correlation is $d\xi(0)/d\lambda_+ = -13.7$ .
+0.178 ± 0.105	207k	<sup>62</sup> CLARK	77 SPEC	POL, $d\xi(0)/d\lambda_+ = +0.68$
-0.385 ± 0.105	2.2M	<sup>63</sup> SANDWEISS	73 CNTR	POL, $d\xi(0)/d\lambda_+ = -6$
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●				
-1.81 <sup>+0.50</sup> / <sub>-0.26</sub>		<sup>64</sup> LONGO	69 CNTR	POL, $t=3.3$
-1.6 ± 0.5	638	<sup>65</sup> ABRAMS	68B OSPK	Polarization
-1.2 ± 0.5	2608	<sup>65</sup> AUERBACH	66B OSPK	Polarization
<sup>62</sup> CLARK 77 $t = +3.80$ , $d\xi(0)/d\lambda_+ = \xi(t)t = 0.178 \times 3.80 = +0.68$ .				
<sup>63</sup> SANDWEISS 73 is for $\lambda_+ = 0$ and $t = 0$ .				
<sup>64</sup> LONGO 69 $t = 3.3$ calculated from $d\xi(0)/d\lambda_+ = -6.0$ (table 1) divided by $\xi = -1.81$ .				
<sup>65</sup> $t$ value not given.				

### Im( $\xi$ ) in $K_{\mu 3}^0$ DECAY (from transverse $\mu$ pol.)

Test of  $T$  reversal invariance.

VALUE	EVTS	DOCUMENT ID	TECN	COMMENT
<b>-0.007 ± 0.026 OUR AVERAGE</b>				
0.009 ± 0.030	12M	MORSE	80 CNTR	Polarization
0.35 ± 0.30	207k	<sup>66</sup> CLARK	77 SPEC	POL, $t=0$
-0.085 ± 0.064	2.2M	<sup>67</sup> SANDWEISS	73 CNTR	POL, $t=0$
-0.02 ± 0.08		LONGO	69 CNTR	POL, $t=3.3$
-0.2 ± 0.6		ABRAMS	68B OSPK	Polarization
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●				
0.012 ± 0.026		SCHMIDT	79 CNTR	Repl. by MORSE 80
<sup>66</sup> CLARK 77 value has additional $\xi(0)$ dependence $+0.21\text{Re}[\xi(0)]$ .				
<sup>67</sup> SANDWEISS 73 value corrected from value quoted in their paper due to new value of $\text{Re}(\xi)$ . See footnote 4 of SCHMIDT 79.				

### $\lambda_+$ (LINEAR ENERGY DEPENDENCE OF $f_+$ IN $K_{\mu 3}^0$ DECAY)

See also the corresponding entries and notes in section " $\xi_A = f_-/f_+$ " above and section " $\lambda_0$  (LINEAR ENERGY DEPENDENCE OF  $f_0$  IN  $K_{\mu 3}^0$  DECAY)" below. For radiative correction of  $K_{\mu 3}^0$  Dalitz plot see GINSBERG 70 and BECHERRAWY 70.

Results labeled OUR FIT are discussed in the review " $K_{\ell 3}^{\pm}$  and  $K_{\ell 3}^0$  Form Factors" in the  $K^{\pm}$  Listings.

VALUE	EVTS	DOCUMENT ID	TECN	COMMENT
<b>0.0300 ± 0.0020 OUR FIT</b>	Error includes scale factor of 2.0. Assumes $\mu$ -e universality.			
<b>0.033 ± 0.005 OUR FIT</b>	Error includes scale factor of 2.3.			
0.0427 ± 0.0044	150k	BIRULEV	81 SPEC	DP
0.028 ± 0.010	14k	CHO	80 HBC	DP
0.028 ± 0.011	16k	HILL	79 STRC	DP
0.046 ± 0.030	32k	BUCHANAN	75 SPEC	DP
0.030 ± 0.003	1.6M	DONALDSON	74B SPEC	DP
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●				
0.0337 ± 0.0033	129k	DZHORD...	77 SPEC	Repl. by BIRULEV 81
0.046 ± 0.008	82k	ALBRECHT	74 WIRE	Repl. by BIRULEV 81
0.085 ± 0.015	9086	ALBROW	72 ASPK	DP
0.11 ± 0.04	16k	DALLY	72 ASPK	DP
0.07 ± 0.02	16k	CHIEN	70 ASPK	Repl. by DALLY 72

### $\lambda_0$ (LINEAR ENERGY DEPENDENCE OF $f_0$ IN $K_{\mu 3}^0$ DECAY)

Wherever possible, we have converted the above values of  $\xi(0)$  into values of  $\lambda_0$  using the associated  $\lambda_+^{\mu}$  and  $d\xi(0)/d\lambda_+$ . Results labeled OUR FIT are discussed in the review " $K_{\ell 3}^{\pm}$  and  $K_{\ell 3}^0$  Form Factors" in the  $K^{\pm}$  Listings.

VALUE	$d\lambda_0/d\lambda_+$	EVTS	DOCUMENT ID	TECN	COMMENT
<b>0.030 ± 0.005 OUR FIT</b>	Error includes scale factor of 2.0. Correlation is $d\lambda_0/d\lambda_+ = -0.12$ . Assumes $\mu$ -e universality.				
<b>0.027 ± 0.006 OUR FIT</b>	Error includes scale factor of 2.3. Correlation is $d\lambda_0/d\lambda_+ = -0.17$ .				
0.040 ± 0.006	0.13		<sup>68</sup> KL3FIT	02 RVUE	$\lambda_+ = 0.030$
0.0341 ± 0.0067	unknown	150k	<sup>69</sup> BIRULEV	81 SPEC	DP
+0.050 ± 0.008	-0.11	14k	CHO	80 HBC	DP
+0.039 ± 0.010	-0.67	16k	HILL	79 STRC	DP
+0.047 ± 0.009	1.06	207k	<sup>70</sup> CLARK	77 SPEC	POL
+0.025 ± 0.019	+0.5	32k	<sup>71</sup> BUCHANAN	75 SPEC	DP
+0.019 ± 0.004	-0.47	1.6M	<sup>72</sup> DONALDSON	74B SPEC	DP
-0.018 ± 0.009	+0.49	2.2M	<sup>70</sup> SANDWEISS	73 CNTR	POL
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●					
0.041 ± 0.008		14k	<sup>73</sup> CHO	80 HBC	BR, $\lambda_+ = 0.028$
+0.0485 ± 0.0076		47k	DZHORD...	77 SPEC	In BIRULEV 81
+0.024 ± 0.011		82k	ALBRECHT	74 WIRE	In BIRULEV 81
+0.06 ± 0.03		6700	<sup>74</sup> BRANDENB...	73 HBC	BR, $\lambda_+ = 0.019 \pm 0.013$
-0.060 ± 0.038	-0.71	1385	<sup>75</sup> PEACH	73 HLBC	DP

$-0.043 \pm 0.052$	$-1.39$	9086	<sup>76</sup> ALBROW	72	ASPK	DP
$-0.067 \pm 0.227$	unknown	16k	<sup>77</sup> DALLY	72	ASPK	DP
$-0.333 \pm 0.034$	+1.	3140	<sup>78</sup> BASILE	70	OSPK	DP
$-0.140 \begin{smallmatrix} +0.043 \\ -0.022 \end{smallmatrix}$	+0.49		<sup>70</sup> LONGO	69	CNTR	POL
$+0.08 \pm 0.07$	$-0.54$	1371	<sup>70</sup> CARPENTER	66	OSPK	DP

<sup>68</sup> KL3FIT 02 value is from our fitted value of the  $K_{\mu 3}^{\pm}/K_{e 3}^{\pm}$  branching ratio. Assumes  $\mu - e$  universality.

<sup>69</sup> BIRULEV 81 gives  $d\lambda_0/d\lambda_+ = -1.5$ , giving an unreasonably narrow error ellipse which dominates all other results. We use  $d\lambda_0/d\lambda_+ = 0$ .

<sup>70</sup>  $\lambda_0$  value is for  $\lambda_+ = 0.03$  calculated by us from  $\xi(0)$  and  $d\xi(0)/d\lambda_+$ .

<sup>71</sup> BUCHANAN 75 value is from their appendix A and uses only  $K_{\mu 3}$  data.  $d\lambda_0/d\lambda_+$  was obtained by private communication, C.Buchanan, 1976.

<sup>72</sup> DONALDSON 74B  $d\lambda_0/d\lambda_+$  obtained from figure 18.

<sup>73</sup> CHO 80 BR result not independent of their Dalitz plot result.

<sup>74</sup> Fit for  $\lambda_0$  does not include this value but instead includes the  $K_{\mu 3}/K_{e 3}$  result from this experiment.

<sup>75</sup> PEACH 73 assumes  $\lambda_+ = 0.025$ . Calculated by us from  $\xi(0)$  and  $d\xi(0)/d\lambda_+$ .

<sup>76</sup> ALBROW 72  $\lambda_0$  is calculated by us from  $\xi_A$ ,  $\lambda_+$  and  $d\xi(0)/d\lambda_+$ . They give  $\lambda_0 = -0.043 \pm 0.039$  for  $\lambda_- = 0$ . We use our larger calculated error.

<sup>77</sup> DALLY 72 gives  $f_0 = 1.20 \pm 0.35$ ,  $\lambda_0 = -0.080 \pm 0.272$ ,  $\lambda_0' = -0.006 \pm 0.045$ , but with a different definition of  $\lambda_0$ . Our quoted  $\lambda_0$  is his  $\lambda_0/f_0$ . We cannot calculate true  $\lambda_0$  error without his  $(\lambda_0, f_0)$  correlations. See also note on DALLY 72 in section  $\xi_A$ .

<sup>78</sup> BASILE 70  $\lambda_0$  is for  $\lambda_+ = 0$ . Calculated by us from  $\xi_A$  with  $d\xi(0)/d\lambda_+ = 0$ . BASILE 70 is incompatible with all other results. Authors suggest that efficiency estimates might be responsible.

### $|f_S/f_+|$ FOR $K_{e 3}^0$ DECAY

Ratio of scalar to  $f_+$  couplings.

VALUE	CL%	EVTS	DOCUMENT ID	TECN	COMMENT
<b>&lt;0.04</b>	68	25k	BLUMENTHAL75	SPEC	
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●					
<0.095	95	18k	HILL	78	STRC
<0.07	68	48k	BIRULEV	76	SPEC See also BIRULEV 81
<0.19	95	5600	ALBROW	73	ASPK
<0.15	68		KULYUKINA	67	CC

### $|f_T/f_+|$ FOR $K_{e 3}^0$ DECAY

Ratio of tensor to  $f_+$  couplings.

VALUE	CL%	EVTS	DOCUMENT ID	TECN	COMMENT
<b>&lt;0.23</b>	68	25k	BLUMENTHAL75	SPEC	
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●					
<0.40	95	18k	HILL	78	STRC
<0.34	68	48k	BIRULEV	76	SPEC See also BIRULEV 81
<1.0	95	5600	ALBROW	73	ASPK
<1.0	68		KULYUKINA	67	CC



### $|f_T/f_+|$ FOR $K_{\mu 3}^0$ DECAY

Ratio of tensor to  $f_+$  couplings.

<u>VALUE</u>	<u>DOCUMENT ID</u>	<u>TECN</u>
<b>0.12±0.12</b>	BIRULEV	81 SPEC

### $\alpha_{K^*}$ DECAY FORM FACTOR FOR $K_L \rightarrow e^+ e^- \gamma$

$\alpha_{K^*}$  is the constant in the model of BERGSTROM 83 which measures the relative strength of the vector-vector transition  $K_L \rightarrow K^* \gamma$  with  $K^* \rightarrow \rho, \omega, \phi \rightarrow \gamma^*$  and the pseudoscalar-pseudoscalar transition  $K_L \rightarrow \pi, \eta, \eta' \rightarrow \gamma \gamma^*$ .

<u>VALUE</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>
<b>-0.33 ±0.05 OUR AVERAGE</b>			
-0.36 ±0.06 ±0.02	6864	FANTI	99B NA48
-0.28 ±0.13		BARR	90B NA31
-0.280 <sup>+0.099</sup> <sub>-0.090</sub>		OHL	90B B845

### $\alpha_{K^*}$ DECAY FORM FACTOR FOR $K_L \rightarrow \mu^+ \mu^- \gamma$

$\alpha_{K^*}$  is the constant in the model of BERGSTROM 83 described in the previous section.

<u>VALUE</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>
<b>-0.158±0.027 OUR AVERAGE</b>			
-0.160 <sup>+0.026</sup> <sub>-0.028</sub>	9100	ALAVI-HARATI01G	KTEV
-0.04 <sup>+0.24</sup> <sub>-0.21</sub>		FANTI	97 NA48

### $\alpha_{K^*}^{\text{eff}}$ DECAY FORM FACTOR FOR $K_L \rightarrow e^+ e^- e^+ e^-$

$\alpha_{K^*}^{\text{eff}}$  is the parameter describing the relative strength of an intermediate pseudoscalar decay amplitude and a vector meson decay amplitude in the model of BERGSTROM 83. It takes into account both the radiative effects and the form factor. Since there are two  $e^+ e^-$  pairs here compared with one in  $e^+ e^- \gamma$  decays, a factorized expression is used for the  $e^+ e^- e^+ e^-$  decay form factor.

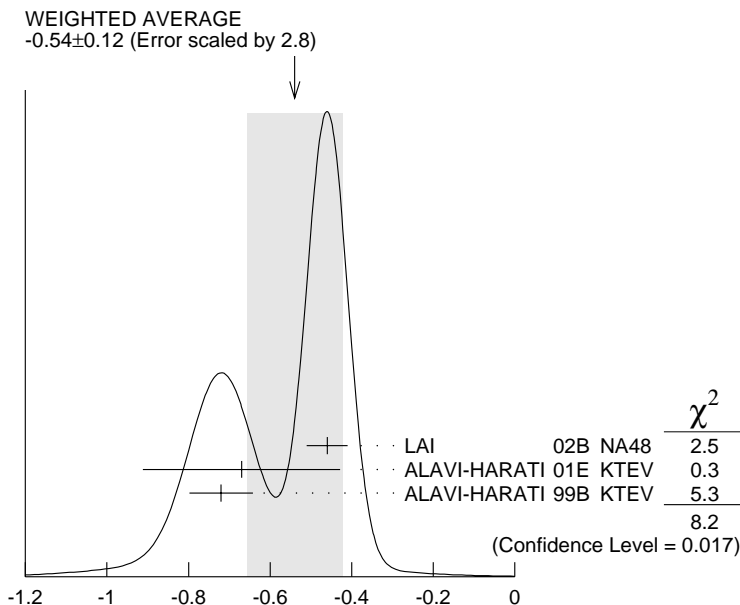
<u>VALUE</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>
<b>-0.14±0.16±0.15</b>	441	ALAVI-HARATI01D	KTEV

### DECAY FORM FACTORS FOR $K_L^0 \rightarrow \pi^\pm \pi^0 e^\mp \nu_e$

Given in MAKOFF 93.

### $a_V$ , VECTOR MESON EXCHANGE CONTRIBUTION

<u>VALUE</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
<b>-0.54±0.12 OUR AVERAGE</b>	Error includes scale factor of 2.8. See the ideogram below.		
-0.46±0.03±0.04	LAI	02B NA48	$K_L^0 \rightarrow \pi^0 2\gamma$
-0.67±0.21±0.12	ALAVI-HARATI01E	KTEV	$K_L^0 \rightarrow \pi^0 e^+ e^- \gamma$
-0.72±0.05±0.06	ALAVI-HARATI99B	KTEV	$K_L^0 \rightarrow \pi^0 2\gamma$



$a_V$

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### CP-VIOLATION PARAMETERS IN $K_L^0$ DECAYS

#### ———— CHARGE ASYMMETRY IN $K_{e3}^0$ DECAYS ————

Such asymmetry violates *CP*. It is related to  $\text{Re}(\epsilon)$ .

$\delta_L =$  weighted average of  $\delta_L(\mu)$  and  $\delta_L(e)$

VALUE (%)	EVTS	DOCUMENT ID	TECN	COMMENT
<b>0.327±0.012 OUR AVERAGE</b>		Includes data from the 2 datablocks that follow this one.		
0.333±0.050	33M	WILLIAMS	73 ASPK	$K_{\mu 3} + K_{e3}$

$\delta_L(\mu) = [\Gamma(\pi^- \mu^+ \nu_\mu) - \Gamma(\pi^+ \mu^- \bar{\nu}_\mu)]/\text{SUM}$

Only the combined value below is put into the Meson Summary Table.

VALUE (%)	EVTS	DOCUMENT ID	TECN
The data in this block is included in the average printed for a previous datablock.			

**0.304±0.025 OUR AVERAGE**

0.313±0.029	15M	GEWENIGER	74 ASPK
0.278±0.051	7.7M	PICCIONI	72 ASPK

• • • We do not use the following data for averages, fits, limits, etc. • • •

0.60 ±0.14	4.1M	MCCARTHY	73 CNTR
0.57 ±0.17	1M	<sup>79</sup> PACIOTTI	69 OSPK
0.403±0.134	1M	<sup>79</sup> DORFAN	67 OSPK

<sup>79</sup>PACIOTTI 69 is a reanalysis of DORFAN 67 and is corrected for  $\mu^+ \mu^-$  range difference in MCCARTHY 72.

$$\delta_L(\mathbf{e}) = [\Gamma(\pi^- e^+ \nu_e) - \Gamma(\pi^+ e^- \bar{\nu}_e)]/\text{SUM}$$

Only the combined value below is put into the Meson Summary Table.

VALUE (%)	EVTS	DOCUMENT ID	TECN
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The data in this block is included in the average printed for a previous datablock.

**0.333±0.014 OUR AVERAGE**

0.341±0.018	34M	GEWENIGER	74 ASPK
0.318±0.038	40M	FITCH	73 ASPK
0.346±0.033	10M	MARX	70 CNTR
0.246±0.059	10M	<sup>80</sup> SAAL	69 CNTR

• • • We do not use the following data for averages, fits, limits, etc. • • •

0.36 ±0.18	600k	ASHFORD	72 ASPK
0.224±0.036	10M	<sup>80</sup> BENNETT	67 CNTR

<sup>80</sup> SAAL 69 is a reanalysis of BENNETT 67.

———— **PARAMETERS FOR  $K_L^0 \rightarrow 2\pi$  DECAY** ————

$$\eta_{+-} = A(K_L^0 \rightarrow \pi^+ \pi^-) / A(K_S^0 \rightarrow \pi^+ \pi^-)$$

$$\eta_{00} = A(K_L^0 \rightarrow \pi^0 \pi^0) / A(K_S^0 \rightarrow \pi^0 \pi^0)$$

The fitted values of  $|\eta_{+-}|$  and  $|\eta_{00}|$  given below are the results of a fit to  $|\eta_{+-}|$ ,  $|\eta_{00}|$ ,  $|\eta_{00}/\eta_{+-}|$ , and  $\text{Re}(\epsilon'/\epsilon)$ . Independent information on  $|\eta_{+-}|$  and  $|\eta_{00}|$  can be obtained from the fitted values of the  $K_L^0 \rightarrow \pi\pi$  and  $K_S^0 \rightarrow \pi\pi$  branching ratios and the  $K_L^0$  and  $K_S^0$  lifetimes. This information is included as data in the  $|\eta_{+-}|$  and  $|\eta_{00}|$  sections with a Document ID "BRFIT." See the note "Fits for  $K_L^0$  CP-Violation Parameters" above for details.

$$|\eta_{00}| = |A(K_L^0 \rightarrow 2\pi^0) / A(K_S^0 \rightarrow 2\pi^0)|$$

VALUE (units $10^{-3}$ )	DOCUMENT ID	TECN	COMMENT
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**2.275±0.017 OUR FIT**

**2.23 ±0.11 OUR AVERAGE**

2.12 ±0.16	<sup>81</sup> BRFIT	02	
2.47 ±0.31 ±0.24	ANGELOPO...	98 CPLR	
2.33 ±0.18	CHRISTENS...	79 ASPK	

• • • We do not use the following data for averages, fits, limits, etc. • • •

2.49 ±0.40	<sup>82</sup> ADLER	96B CPLR	Sup. by ANGELOPOU-LOS 98
2.71 ±0.37	<sup>83</sup> WOLFF	71 OSPK	Cu reg., $4\gamma$ 's
2.95 ±0.63	<sup>83</sup> CHOLLET	70 OSPK	Cu reg., $4\gamma$ 's

<sup>81</sup> This BRFIT value is computed from fitted values of the  $K_L^0$  and  $K_S^0$  lifetimes and branching fractions to  $\pi\pi$ . See the discussion in the note "Fits for  $K_L^0$  CP-Violation Parameters."

<sup>82</sup> Error is statistical only.

<sup>83</sup> CHOLLET 70 gives  $|\eta_{00}| = (1.23 \pm 0.24) \times (\text{regeneration amplitude, } 2 \text{ GeV}/c \text{ Cu})/10000\text{mb}$ . WOLFF 71 gives  $|\eta_{00}| = (1.13 \pm 0.12) \times (\text{regeneration amplitude, } 2 \text{ GeV}/c \text{ Cu})/10000\text{mb}$ . We compute both  $|\eta_{00}|$  values for (regeneration amplitude,  $2 \text{ GeV}/c \text{ Cu}) = 24 \pm 2\text{mb}$ . This regeneration amplitude results from averaging over FAISSNER 69, extrapolated using optical-model calculations of Bohm et al., Physics Letters **27B** 594 (1968) and the data of BALATS 71. (From H. Faissner, private communication).

$$|\eta_{+-}| = |A(K_L^0 \rightarrow \pi^+ \pi^-) / A(K_S^0 \rightarrow \pi^+ \pi^-)|$$

VALUE (units $10^{-3}$ )	EVTS	DOCUMENT ID	TECN	COMMENT
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**2.286 ± 0.017 OUR FIT**

**2.287 ± 0.017 OUR AVERAGE**

2.292 ± 0.024		84 BRFIT	02	
2.264 ± 0.023 ± 0.027	70M	85 APOSTOLA...	99C CPLR	$K^0-\bar{K}^0$ asymmetry
2.30 ± 0.035		GEWENIGER	74B ASPK	

• • • We do not use the following data for averages, fits, limits, etc. • • •

2.310 ± 0.043 ± 0.031		86 ADLER	95B CPLR	$K^0-\bar{K}^0$ asymmetry
2.32 ± 0.14 ± 0.03	10 <sup>5</sup>	ADLER	92B CPLR	$K^0-\bar{K}^0$ asymmetry

<sup>84</sup> This BRFIT value is computed from fitted values of the  $K_L^0$  and  $K_S^0$  lifetimes and branching fractions to  $\pi\pi$ . See the discussion in the note "Fits for  $K_L^0$  CP-Violation Parameters."

<sup>85</sup> APOSTOLAKIS 99C report  $(2.264 \pm 0.023 \pm 0.026 + 9.1[\tau_S - 0.8934]) \times 10^{-3}$ . We evaluate for our 1998 best value  $\tau_S = (0.8934 \pm 0.0008) \times 10^{-10}$  s.

<sup>86</sup> ADLER 95B report  $(2.312 \pm 0.043 \pm 0.030 - 1[\Delta m - 0.5274] + 9.1[\tau_S - 0.8926]) \times 10^{-3}$ . We evaluate for our 1996 best values  $\Delta m = (0.5304 \pm 0.0014) \times 10^{-10} \text{ h}_S^{-1}$  and  $\tau_S = (0.8927 \pm 0.0009) \times 10^{-10}$  s. Superseded by APOSTOLAKIS 99C.

$$|\eta_{00}/\eta_{+-}|$$

VALUE	EVTS	DOCUMENT ID	TECN
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**0.9950 ± 0.0008 OUR FIT** Error includes scale factor of 1.6.

**0.9930 ± 0.0020 OUR AVERAGE**

0.9931 ± 0.0020		87,88 BARR	93D NA31
0.9904 ± 0.0084 ± 0.0036		89 WOODS	88 E731

• • • We do not use the following data for averages, fits, limits, etc. • • •

0.9939 ± 0.0013 ± 0.0015	1M	87 BARR	93D NA31
0.9899 ± 0.0020 ± 0.0025		87 BURKHARDT	88 NA31

<sup>87</sup> This is the square root of the ratio  $R$  given by BURKHARDT 88 and BARR 93D.

<sup>88</sup> This is the combined results from BARR 93D and BURKHARDT 88, taking into account a common systematic uncertainty of 0.0014.

<sup>89</sup> We calculate  $|\eta_{00}/\eta_{+-}| = 1 - 3(\epsilon'/\epsilon)$  from WOODS 88 ( $\epsilon'/\epsilon$ ) value.

$$\text{Re}(\epsilon'/\epsilon) = (1 - |\eta_{00}/\eta_{+-}|)/3$$

VALUE (units $10^{-3}$ )	DOCUMENT ID	TECN	COMMENT
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**1.67 ± 0.26 OUR FIT** Error includes scale factor of 1.6.

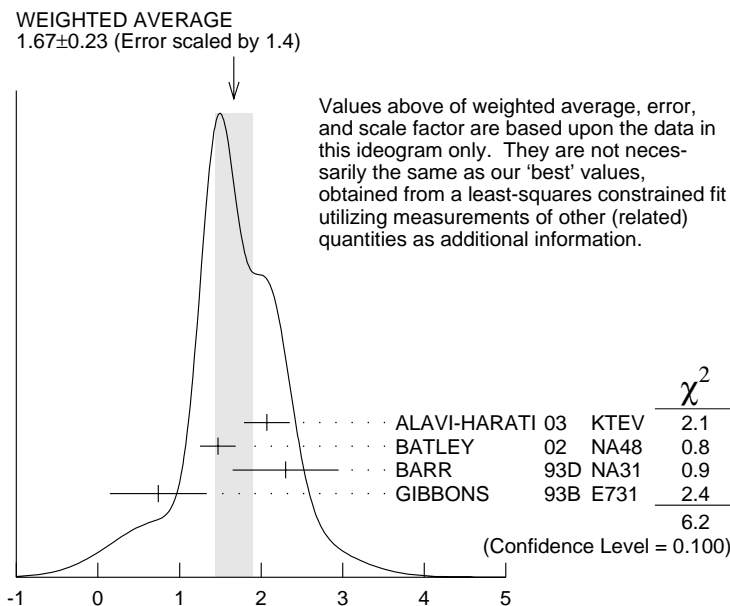
**1.67 ± 0.23 OUR AVERAGE** Error includes scale factor of 1.4. See the ideogram below.

2.07 ± 0.28	ALAVI-HARATI03	KTEV	
1.47 ± 0.22	BATLEY	02 NA48	
2.3 ± 0.65	90,91 BARR	93D NA31	
0.74 ± 0.52 ± 0.29	GIBBONS	93B E731	

• • • We do not use the following data for averages, fits, limits, etc. • • •

1.53 ± 0.26	LAI	01C NA48	Incl. in BATLEY 02
2.80 ± 0.30 ± 0.28	ALAVI-HARATI99D	KTEV	In ALAVI-HARATI 03
1.85 ± 0.45 ± 0.58	FANTI	99C NA48	In LAI 01C
2.0 ± 0.7	92 BARR	93D NA31	
-0.4 ± 1.4 ± 0.6	PATTERSON	90 E731	in GIBBONS 93B
3.3 ± 1.1	92 BURKHARDT	88 NA31	
3.2 ± 2.8 ± 1.2	90 WOODS	88 E731	

- 90 These values are derived from  $|\eta_{00}/\eta_{+-}|$  measurements. They enter the average in this section but enter the fit via the  $|\eta_{00}/\eta_{+-}|$  only.
- 91 This is the combined results from BARR 93D and BURKHARDT 88, taking into account their common systematic uncertainty.
- 92 These values are derived from  $|\eta_{00}/\eta_{+-}|$  measurements.



$$\text{Re}(\epsilon'/\epsilon) = (1 - |\eta_{00}/\eta_{+-}|)/3$$

### $\phi_{+-}$ , PHASE of $\eta_{+-}$

The dependence of the phase on  $\Delta m$  and  $\tau_S$  is given for each experiment in the comments below, where  $\Delta m$  is the  $K_L^0 - K_S^0$  mass difference in units  $10^{10} \text{ } \hbar\text{s}^{-1}$  and  $\tau_S$  is the  $K_S$  mean life in units  $10^{-10} \text{ s}$ . We also give the regeneration phase  $\phi_f$  in the comments below.

OUR FIT is described in the note on "Fits for  $K_L^0$  CP-Violation Parameters" in the  $K_L^0$  Particle Listings.

The FITS given below are from the 2002 edition and do NOT include the new data which are indicated by the change bars at the right.

<u>VALUE (°)</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
<b>43.51±0.06 OUR FIT</b>	Assuming <i>CPT</i>			
<b>43.4 ±0.7 OUR FIT</b>	Not assuming <i>CPT</i>			
<b>43.4 ±0.4 OUR AVERAGE</b>				
44.12±0.72±1.20	93	ALAVI-HARATI03	KTEV	Scintillator Pb regenera-
43.2 ±0.6 ±0.3	70M	94 APOSTOLA...	99C CPLR	$K^0$ - $\bar{K}^0$ asymmetry
43.6 ±0.8 ±0.3	95,96	SCHWINGEN...	95 E773	CH <sub>1,1</sub> regenerator
42.5 ±0.9 ±0.4	96,97	GIBBONS	93 E731	B <sub>4</sub> C regenerator

44.5 ± 1.6 ± 0.6	98 CAROSI	90 NA31	Vacuum regen.
44.5 ± 2.8 ± 0.2	99 CARITHERS	75 SPEC	C regenerator
43.9 ± 1.0 ± 0.5	100 GEWENIGER	74B ASPK	Vacuum regen.

• • • We do not use the following data for averages, fits, limits, etc. • • •

43.4 ± 0.4 ± 0.4	101,102 ADLER	96C RVUE	
43.6 ± 1.1 ± 0.3	103 ADLER	95B CPLR	$K^0-\bar{K}^0$ asymmetry
42.3 ± 4.4 ± 1.4	10 <sup>5</sup> 104 ADLER	92B CPLR	$K^0-\bar{K}^0$ asymmetry
47.7 ± 2.0 ± 0.9	96,105 KARLSSON	90 E731	

<sup>93</sup> ALAVI-HARATI 03  $\phi_{+-}$  is correlated with their  $\Delta m = m_{K_L^0} - m_{K_S^0}$  and  $\tau_{K_S}$  measurements in the  $K_L^0$  and  $K_S^0$  sections respectively. The correlation coefficients are  $\rho(\phi_{+-}, \Delta m) = +0.987$ ,  $\rho(\phi_{+-}, \tau_S) = -0.898$ , and  $\rho(\tau_S, \Delta m) = -0.874$ . *CPT* is not assumed.

<sup>94</sup> APOSTOLAKIS 99C measures  $\phi_{+-} = (43.19 \pm 0.53 \pm 0.28) + 300 [\Delta m - 0.5301] (^\circ)$ . We have adjusted the measurement to use our best values of ( $\Delta m = 0.5303 \pm 0.0009$ ) ( $10^{10} \hbar s^{-1}$ ). Our first error is their experiment's error and our second error is the systematic error from using our best values.

<sup>95</sup> SCHWINGENHEUER 95 measures  $\phi_{+-} = (43.53 \pm 0.76) + 173 [\Delta m - 0.5282] - 275 [\tau_S - 0.8926] (^\circ)$ . We have adjusted the measurement to use our best values of ( $\Delta m = 0.5303 \pm 0.0009$ ) ( $10^{10} \hbar s^{-1}$ ), ( $\tau_S = 0.8935 \pm 0.0008$ ) ( $10^{-10} s$ ). Our first error is their experiment's error and our second error is the systematic error from using our best values.

<sup>96</sup> These experiments measure  $\phi_{+-} - \phi_f$  and calculate the regeneration phase from the power law momentum dependence of the regeneration amplitude using analyticity and dispersion relations. SCHWINGENHEUER 95 [GIBBONS 93] includes a systematic error of  $0.35^\circ$  [ $0.5^\circ$ ] for uncertainties in their modeling of the regeneration amplitude. See the discussion of these systematic errors, including criticism that they could be underestimated, in the note on "*C* violation in  $K_L^0$  decay."

<sup>97</sup> GIBBONS 93 measures  $\phi_{+-} = (42.21 \pm 0.9) + 189 [\Delta m - 0.5257] - 460 [\tau_S - 0.8922] (^\circ)$ . We have adjusted the measurement to use our best values of ( $\Delta m = 0.5303 \pm 0.0009$ ) ( $10^{10} \hbar s^{-1}$ ), ( $\tau_S = 0.8935 \pm 0.0008$ ) ( $10^{-10} s$ ). Our first error is their experiment's error and our second error is the systematic error from using our best values. This is actually reported in SCHWINGENHEUER 95, footnote 8. GIBBONS 93 reports  $\phi_{+-}$  ( $42.2 \pm 1.4$ ) $^\circ$ . They measure  $\phi_{+-} - \phi_f$  and calculate the regeneration phase  $\phi_f$  from the power law momentum dependence of the regeneration amplitude using analyticity. An error of  $0.6^\circ$  is included for possible uncertainties in the regeneration phase.

<sup>98</sup> CAROSI 90 measures  $\phi_{+-} = (46.9 \pm 1.4 \pm 0.7) + 579 [\Delta m - 0.5351] + 303 [\tau_S - 0.8922] (^\circ)$ . We have adjusted the measurement to use our best values of ( $\Delta m = 0.5303 \pm 0.0009$ ) ( $10^{10} \hbar s^{-1}$ ), ( $\tau_S = 0.8935 \pm 0.0008$ ) ( $10^{-10} s$ ). Our first error is their experiment's error and our second error is the systematic error from using our best values.

<sup>99</sup> CARITHERS 75 measures  $\phi_{+-} = (45.5 \pm 2.8) + 224 [\Delta m - 0.5348] (^\circ)$ . We have adjusted the measurement to use our best values of ( $\Delta m = 0.5303 \pm 0.0009$ ) ( $10^{10} \hbar s^{-1}$ ). Our first error is their experiment's error and our second error is the systematic error from using our best values.  $\phi_f = -40.9 \pm 2.6^\circ$ .

<sup>100</sup> GEWENIGER 74B measures  $\phi_{+-} = (49.4 \pm 1.0) + 565 [\Delta m - 0.540] (^\circ)$ . We have adjusted the measurement to use our best values of ( $\Delta m = 0.5303 \pm 0.0009$ ) ( $10^{10} \hbar s^{-1}$ ). Our first error is their experiment's error and our second error is the systematic error from using our best values.

<sup>101</sup> ADLER 96C measures  $\phi_{+-} = (43.82 \pm 0.41) + 339 [\Delta m - 0.5307] - 252 [\tau_S - 0.8922] (^\circ)$ . We have adjusted the measurement to use our best values of ( $\Delta m =$

- 0.5303 ± 0.0009) (10<sup>10</sup> ħ s<sup>-1</sup>), (τ<sub>S</sub> = 0.8935 ± 0.0008) (10<sup>-10</sup> s). Our first error is their experiment's error and our second error is the systematic error from using our best values.
- 102 ADLER 96C is the result of a fit which includes nearly the same data as entered into the "OUR FIT" value in the 1996 edition of this Review (Physical Review **D54** 1 (1996)).
- 103 ADLER 95B measures φ<sub>+−</sub> = (42.7 ± 0.9 ± 0.6) + 316 [Δm − 0.5274] + 30 [τ<sub>S</sub> − 0.8926] (°). We have adjusted the measurement to use our best values of (Δm = 0.5303 ± 0.0009) (10<sup>10</sup> ħ s<sup>-1</sup>), (τ<sub>S</sub> = 0.8935 ± 0.0008) (10<sup>-10</sup> s). Our first error is their experiment's error and our second error is the systematic error from using our best values.
- 104 ADLER 92B quote separately two systematic errors: ±0.4 from their experiment and ±1.0 degrees due to the uncertainty in the value of Δm.
- 105 KARLSSON 90 systematic error does not include regeneration phase uncertainty.

### φ<sub>00</sub>, PHASE OF η<sub>00</sub>

See comment in φ<sub>+−</sub> header above for treatment of Δm and τ<sub>S</sub> dependence.

OUR FIT is described in the note on "Fits for K<sub>L</sub><sup>0</sup> CP-Violation Parameters" in the K<sub>L</sub><sup>0</sup> Particle Listings.

The FITS given below are from the 2002 edition and do NOT include the new data which are indicated by the change bars at the right.

VALUE (°)	DOCUMENT ID	TECN	COMMENT
<b>43.51 ± 0.06 OUR FIT</b>	Assuming CPT		
<b>43.2 ± 1.0 OUR FIT</b>	Not assuming CPT		
<b>44.3 ± 2.2 OUR AVERAGE</b>			
41.9 ± 5.9 ± 0.2	106 ANGELOPO...	98 CPLR	
44.6 ± 2.3 ± 0.6	107 CAROSI	90 NA31	
• • • We do not use the following data for averages, fits, limits, etc. • • •			
50.8 ± 7.1 ± 1.7	108 ADLER	96B CPLR	Sup. by ANGELOPOU- LOS 98
47.4 ± 1.4 ± 0.9	109 KARLSSON	90 E731	
106 ANGELOPOULOS 98 measures φ <sub>00</sub> = (42.0 ± 5.6 ± 1.9) + 240 [Δm − 0.5307] (°). We have adjusted the measurement to use our best values of (Δm = 0.5303 ± 0.0009) (10 <sup>10</sup> ħ s <sup>-1</sup> ). Our first error is their experiment's error and our second error is the systematic error from using our best values. The τ <sub>S</sub> dependence is negligible.			
107 CAROSI 90 measures φ <sub>00</sub> = (47.1 ± 2.1 ± 1.0) + 579 [Δm − 0.5351] + 252 [τ <sub>S</sub> − 0.8922] (°). We have adjusted the measurement to use our best values of (Δm = 0.5303 ± 0.0009) (10 <sup>10</sup> ħ s <sup>-1</sup> ), (τ <sub>S</sub> = 0.8935 ± 0.0008) (10 <sup>-10</sup> s). Our first error is their experiment's error and our second error is the systematic error from using our best values.			
108 ADLER 96B identified initial neutral kaon individually as being a K <sup>0</sup> or a K <sup>0</sup> . The systematic uncertainty is ±1.5° combined in quadrature with ±0.8° due to Δm.			
109 KARLSSON 90 systematic error does not include regeneration phase uncertainty.			

### ———— DECAY-PLANE ASYMMETRY IN π<sup>+</sup>π<sup>-</sup>e<sup>+</sup>e<sup>-</sup> DECAYS ————

This is the CP-violating asymmetry

$$A = \frac{N_{\sin\phi\cos\phi>0.0} - N_{\sin\phi\cos\phi<0.0}}{N_{\sin\phi\cos\phi>0.0} + N_{\sin\phi\cos\phi<0.0}}$$

where φ is the angle between the e<sup>+</sup>e<sup>-</sup> and π<sup>+</sup>π<sup>-</sup> planes in the K<sub>L</sub><sup>0</sup> rest frame.

### CP ASYMMETRY A in K<sub>L</sub> → π<sup>+</sup>π<sup>-</sup>e<sup>+</sup>e<sup>-</sup>

VALUE (%)	DOCUMENT ID	TECN
<b>13.6 ± 2.5 ± 1.2</b>	ALAVI-HARATI00B	KTEV

## PARAMETERS FOR $e^+ e^- e^+ e^-$ DECAYS

These are the  $CP$ -violating parameters in the  $\phi$  distribution, where  $\phi$  is the angle between the planes of the two  $e^+ e^-$  pairs in the kaon rest frame:

$$d\Gamma/d\phi \propto 1 + \beta_{CP} \cos(2\phi) + \gamma_{CP} \sin(2\phi)$$

### $\beta_{CP}$ from $K_L \rightarrow e^+ e^- e^+ e^-$

VALUE	EVTS	DOCUMENT ID	TECN	COMMENT
$-0.23 \pm 0.09 \pm 0.02$	441	ALAVI-HARATI01D	KTEV	$M_{ee} > 8 \text{ MeV}/c^2$

### $\gamma_{CP}$ from $K_L^0 \rightarrow e^+ e^- e^+ e^-$

VALUE	EVTS	DOCUMENT ID	TECN	COMMENT
$-0.09 \pm 0.09 \pm 0.02$	441	ALAVI-HARATI01D	KTEV	$M_{ee} > 8 \text{ MeV}/c^2$

## CHARGE ASYMMETRY IN $\pi^+ \pi^- \pi^0$ DECAYS

These are  $CP$ -violating charge-asymmetry parameters, defined at beginning of section "LINEAR COEFFICIENT  $g$  FOR  $K_L^0 \rightarrow \pi^+ \pi^- \pi^0$  above.

See also note on Dalitz plot parameters in  $K^\pm$  section and note on  $CP$  violation in  $K_L^0$  decay above.

### LINEAR COEFFICIENT $j$ FOR $K_L^0 \rightarrow \pi^+ \pi^- \pi^0$

VALUE	EVTS	DOCUMENT ID	TECN
<b>0.0011 <math>\pm</math> 0.0008 OUR AVERAGE</b>			
$0.0010 \pm 0.0024 \pm 0.0030$	500k	ANGELOPO...	98C CPLR
$0.001 \pm 0.011$	6499	CHO	77
$-0.001 \pm 0.003$	4709	PEACH	77
$0.0013 \pm 0.0009$	3M	SCRIBANO	70
$0.0 \pm 0.017$	4400	SMITH	70 OSPK
$0.001 \pm 0.004$	238k	BLANPIED	68

### QUADRATIC COEFFICIENT $f$ FOR $K_L^0 \rightarrow \pi^+ \pi^- \pi^0$

VALUE	EVTS	DOCUMENT ID	TECN
<b>0.0045 <math>\pm</math> 0.0024 <math>\pm</math> 0.0059</b>	500k	ANGELOPO...	98C CPLR

## PARAMETERS for $K_L^0 \rightarrow \pi^+ \pi^- \gamma$ DECAY

$$|\eta_{+-\gamma}| = |A(K_L^0 \rightarrow \pi^+ \pi^- \gamma, CP \text{ violating})/A(K_S^0 \rightarrow \pi^+ \pi^- \gamma)|$$

VALUE (units $10^{-3}$ )	EVTS	DOCUMENT ID	TECN
<b>2.35 <math>\pm</math> 0.07 OUR AVERAGE</b>			
$2.359 \pm 0.062 \pm 0.040$	9045	MATTHEWS	95 E773
$2.15 \pm 0.26 \pm 0.20$	3671	RAMBERG	93B E731

$$\phi_{+-\gamma} = \text{phase of } \eta_{+-\gamma}$$

VALUE ( $^\circ$ )	EVTS	DOCUMENT ID	TECN
<b>44 <math>\pm</math> 4 OUR AVERAGE</b>			
$43.8 \pm 3.5 \pm 1.9$	9045	MATTHEWS	95 E773
$72 \pm 23 \pm 17$	3671	RAMBERG	93B E731



### $|\epsilon'_{+-\gamma}|/\epsilon$ for $K_L^0 \rightarrow \pi^+\pi^-\gamma$

VALUE	CL%	EVTS	DOCUMENT ID	TECN
<b>&lt;0.3</b>	90	3671	110 RAMBERG	93B E731

<sup>110</sup> RAMBERG 93B limit on  $|\epsilon'_{+-\gamma}|/\epsilon$  assumes than any difference between  $\eta_{+-}$  and  $\eta_{+-\gamma}$  is due to direct CP violation.

## CPT-INVARIANCE TESTS IN $K_L^0$ DECAYS

### PHASE DIFFERENCE $\phi_{00} - \phi_{+-}$

Test of CPT.

OUR FIT is described in the note on "Fits for  $K_L^0$  CP-Violation Parameters" in the  $K_L^0$  Particle Listings.

The FITS given below are from the 2002 edition and do NOT include the new data which are indicated by the change bars at the right.

VALUE (°)	DOCUMENT ID	TECN	COMMENT
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- |   |                               |         |                     |
|---|-------------------------------|---------|---------------------|
| <b>0 OUR FIT</b>  | Assuming CPT                  |         |                     |
| <b>-0.1 ± 0.8 OUR FIT</b>   | Not assuming CPT              |         |                     |
| <b>0.2 ± 0.4 OUR AVERAGE</b>  |                               |         |                     |
| 0.39 ± 0.22 ± 0.45  | <sup>111</sup> ALAVI-HARATI03 | KTEV    |                     |
| -0.30 ± 0.88  | <sup>112</sup> SCHWINGEN...95 |         | Combined E731, E773 |
| 0.2 ± 2.6 ± 1.2   | <sup>113</sup> CAROSI         | 90 NA31 |                     |
| ● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ● |                               |         |                     |
| 0.62 ± 0.71 ± 0.75  | SCHWINGEN...95                | E773    |                     |
| -1.6 ± 1.2  | <sup>114</sup> GIBBONS        | 93 E731 |                     |
| -0.3 ± 2.4 ± 1.2  | KARLSSON                      | 90 E731 |                     |
- <sup>111</sup> ALAVI-HARATI 03 fit  $\text{Re}(\epsilon'/\epsilon)$ ,  $\text{Im}(\epsilon'/\epsilon)$ ,  $\Delta m$ ,  $\tau_S$ , and  $\phi_{+-}$  simultaneously, not assuming CPT. Phase difference is obtained from  $\phi_{00} - \phi_{+-} \approx -3\text{Im}(\epsilon'/\epsilon)$  for small  $|\epsilon'/\epsilon|$ .
- <sup>112</sup> This SCHWINGENHEUER 95 values is the combined result of SCHWINGENHEUER 95 and GIBBONS 93, accounting for correlated systematic errors.
- <sup>113</sup> CAROSI 90 is excluded from the fit because it it is not independent of  $\phi_{+-}$  and  $\phi_{00}$  values.
- <sup>114</sup> GIBBONS 93 give detailed dependence of systematic error on lifetime (see the section on the  $K_S^0$  mean life) and mass difference (see the section on  $m_{K_L^0} - m_{K_S^0}$ ).

### PHASE DIFFERENCE $\phi_{+-} - \phi_{SW}$

Test of CPT. The Superweak phase  $\phi_{SW} \equiv \tan^{-1}(2\Delta m/\Delta\Gamma)$  where  $\Delta m = m_{K_L^0} - m_{K_S^0}$  and  $\Delta\Gamma = \hbar(\tau_L - \tau_S)/(\tau_L\tau_S)$ .

VALUE	DOCUMENT ID	TECN
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<b>0.61 ± 0.62 ± 1.01</b>	<sup>115</sup> ALAVI-HARATI03	KTEV
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<sup>115</sup> ALAVI-HARATI 03 fit is the same as their  $\phi_{+-}$ ,  $\tau_{K_S}$ ,  $\Delta m$  fit, except that the parameter  $\phi_{+-} - \phi_{SW}$  is used in place of  $\phi$ .

$$\text{Re}\left(\frac{2}{3}\eta_{+-} + \frac{1}{3}\eta_{00}\right) - \frac{\delta_L}{2}$$

Test of *CPT*

VALUE (units $10^{-6}$ )	DOCUMENT ID	TECN	COMMENT
<b><math>-3 \pm 35</math></b>	116 ALAVI-HARATI02	E799	Uses $\delta_L$ from $K_{e3}$ decays

116 ALAVI-HARATI 02 uses PDG 00 values of  $\eta_{+-}$  and  $\eta_{00}$ .

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$$x = A(\bar{K}^0 \rightarrow \pi^- \ell^+ \nu) / A(K^0 \rightarrow \pi^- \ell^+ \nu) = A(\Delta S = -\Delta Q) / A(\Delta S = \Delta Q)$$

### REAL PART OF $x$

VALUE	EVTS	DOCUMENT ID	TECN	COMMENT
<b><math>-0.0018 \pm 0.0041 \pm 0.0045</math></b>		ANGELOPO...	98D CPLR	$K_{e3}$ from $K^0$
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●				
0.10 $\begin{smallmatrix} +0.18 \\ -0.19 \end{smallmatrix}$	79	SMITH	75B WIRE	$\pi^- p \rightarrow K^0 \Lambda$
0.04 $\pm 0.03$	4724	NIEBERGALL	74 ASPK	$K^+ p \rightarrow K^0 p \pi^+$
-0.008 $\pm 0.044$	1757	FACKLER	73 OSPK	$K_{e3}$ from $K^0$
-0.03 $\pm 0.07$	1367	HART	73 OSPK	$K_{e3}$ from $K^0 \Lambda$
-0.070 $\pm 0.036$	1079	MALLARY	73 OSPK	$K_{e3}$ from $K^0 \Lambda X$
0.03 $\pm 0.06$	410	117 BURGUN	72 HBC	$K^+ p \rightarrow K^0 p \pi^+$
0.04 $\begin{smallmatrix} +0.10 \\ -0.13 \end{smallmatrix}$	100	118 GRAHAM	72 OSPK	$K_{\mu 3}$ from $K^0 \Lambda$
-0.05 $\pm 0.09$	442	118 GRAHAM	72 OSPK	$\pi^- p \rightarrow K^0 \Lambda$
0.26 $\begin{smallmatrix} +0.10 \\ -0.14 \end{smallmatrix}$	126	MANN	72 HBC	$K^- p \rightarrow n \bar{K}^0$
-0.13 $\pm 0.11$	342	118 MANTSCH	72 OSPK	$K_{e3}$ from $K^0 \Lambda$
0.04 $\begin{smallmatrix} +0.07 \\ -0.08 \end{smallmatrix}$	222	117 BURGUN	71 HBC	$K^+ p \rightarrow K^0 p \pi^+$
0.25 $\begin{smallmatrix} +0.07 \\ -0.09 \end{smallmatrix}$	252	WEBBER	71 HBC	$K^- p \rightarrow n \bar{K}^0$
0.12 $\pm 0.09$	215	119 CHO	70 DBC	$K^+ d \rightarrow K^0 p p$
-0.020 $\pm 0.025$		120 BENNETT	69 CNTR	Charge asym+ Cu regen.
0.09 $\begin{smallmatrix} +0.14 \\ -0.16 \end{smallmatrix}$	686	LITTENBERG	69 OSPK	$K^+ n \rightarrow K^0 p$
0.03 $\pm 0.03$		120 BENNETT	68 CNTR	
0.09 $\begin{smallmatrix} +0.07 \\ -0.09 \end{smallmatrix}$	121	JAMES	68 HBC	$\bar{p} p$
0.17 $\begin{smallmatrix} +0.16 \\ -0.35 \end{smallmatrix}$	116	FELDMAN	67B OSPK	$\pi^- p \rightarrow K^0 \Lambda$
0.17 $\pm 0.10$	335	119 HILL	67 DBC	$K^+ d \rightarrow K^0 p p$
0.035 $\begin{smallmatrix} +0.11 \\ -0.13 \end{smallmatrix}$	196	AUBERT	65 HLBC	$K^+$ charge exchange
0.06 $\begin{smallmatrix} +0.18 \\ -0.44 \end{smallmatrix}$	152	121 BALDO-...	65 HLBC	$K^+$ charge exchange
-0.08 $\begin{smallmatrix} +0.16 \\ -0.28 \end{smallmatrix}$	109	122 FRANZINI	65 HBC	$\bar{p} p$

- 117 BURGUN 72 is a final result which includes BURGUN 71.  
 118 First GRAHAM 72 value is second GRAHAM 72 value combined with MANTSCH 72.  
 119 CHO 70 is analysis of unambiguous events in new data and HILL 67.  
 120 BENNETT 69 is a reanalysis of BENNETT 68.  
 121 BALDO-CEOLIN 65 gives  $x$  and  $\theta$  converted by us to  $\text{Re}(x)$  and  $\text{Im}(x)$ .  
 122 FRANZINI 65 gives  $x$  and  $\theta$  for  $\text{Re}(x)$  and  $\text{Im}(x)$ . See SCHMIDT 67.

### IMAGINARY PART OF $x$

Assumes  $m_{K_L^0} - m_{K_S^0}$  positive. See Listings above.

VALUE	EVTS	DOCUMENT ID	TECN	COMMENT
<b>0.0012±0.0019±0.0009</b>	640k	ANGELOPO...	01B CPLR	$K_{e3}$ from $K^0$
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●				
0.0012±0.0019	640k	<sup>123</sup> ANGELOPO...	98E CPLR	$K_{e3}$ from $K^0$
-0.10 <sup>+0.16</sup> <sub>-0.19</sub>	79	SMITH	75B WIRE	$\pi^- p \rightarrow K^0 \Lambda$
-0.06 ±0.05	4724	NIEBERGALL	74 ASPK	$K^+ p \rightarrow K^0 p \pi^+$
-0.017 ±0.060	1757	FACKLER	73 OSPK	$K_{e3}$ from $K^0$
0.09 ±0.07	1367	HART	73 OSPK	$K_{e3}$ from $K^0 \Lambda$
0.107 <sup>+0.092</sup> <sub>-0.074</sub>	1079	MALLARY	73 OSPK	$K_{e3}$ from $K^0 \Lambda X$
0.07 <sup>+0.06</sup> <sub>-0.07</sub>	410	<sup>124</sup> BURGUN	72 HBC	$K^+ p \rightarrow K^0 p \pi^+$
0.12 <sup>+0.17</sup> <sub>-0.16</sub>	100	<sup>125</sup> GRAHAM	72 OSPK	$K_{\mu 3}$ from $K^0 \Lambda$
0.05 ±0.13	442	<sup>125</sup> GRAHAM	72 OSPK	$\pi^- p \rightarrow K^0 \Lambda$
0.21 <sup>+0.15</sup> <sub>-0.12</sub>	126	MANN	72 HBC	$K^- p \rightarrow n \bar{K}^0$
-0.04 ±0.16	342	<sup>125</sup> MANTSCH	72 OSPK	$K_{e3}$ from $K^0 \Lambda$
0.12 <sup>+0.08</sup> <sub>-0.09</sub>	222	<sup>124</sup> BURGUN	71 HBC	$K^+ p \rightarrow K^0 p \pi^+$
0.0 ±0.08	252	WEBBER	71 HBC	$K^- p \rightarrow n \bar{K}^0$
-0.08 ±0.07	215	<sup>126</sup> CHO	70 DBC	$K^+ d \rightarrow K^0 p p$
-0.11 <sup>+0.10</sup> <sub>-0.11</sub>	686	LITTENBERG	69 OSPK	$K^+ n \rightarrow K^0 p$
+0.22 <sup>+0.37</sup> <sub>-0.29</sub>	121	JAMES	68 HBC	$\bar{p} p$
0.0 ±0.25	116	FELDMAN	67B OSPK	$\pi^- p \rightarrow K^0 \Lambda$
-0.20 ±0.10	335	<sup>126</sup> HILL	67 DBC	$K^+ d \rightarrow K^0 p p$
-0.21 <sup>+0.11</sup> <sub>-0.15</sub>	196	AUBERT	65 HLBC	$K^+$ charge exchange
-0.44 <sup>+0.32</sup> <sub>-0.19</sub>	152	<sup>127</sup> BALDO-...	65 HLBC	$K^+$ charge exchange
+0.24 <sup>+0.40</sup> <sub>-0.30</sub>	109	<sup>128</sup> FRANZINI	65 HBC	$\bar{p} p$

- <sup>123</sup> Superseded by ANGELOPOULOS 01B.  
<sup>124</sup> BURGUN 72 is a final result which includes BURGUN 71.  
<sup>125</sup> First GRAHAM 72 value is second GRAHAM 72 value combined with MANTSCH 72.  
<sup>126</sup> Footnote 10 of HILL 67 should read +0.58, not -0.58 (private communication) CHO 70 is analysis of unambiguous events in new data and HILL 67.  
<sup>127</sup> BALDO-CEOLIN 65 gives  $x$  and  $\theta$  converted by us to  $\text{Re}(x)$  and  $\text{Im}(x)$ .  
<sup>128</sup> FRANZINI 65 gives  $x$  and  $\theta$  for  $\text{Re}(x)$  and  $\text{Im}(x)$ . See SCHMIDT 67.

**$K_L^0$  REFERENCES**

ALAVI-HARATI	03	PR D67 012005	A. Alavi-Harati <i>et al.</i>	(FNAL KTeV Collab.)
LAI	03	PL B551 7	A. Lai <i>et al.</i>	(CERN NA48 Collab.)
ALAVI-HARATI	02	PRL 88 181601	A. Alavi-Harati <i>et al.</i>	(FNAL KTeV Collab.)
ALAVI-HARATI	02C	PRL 89 211801	A. Alavi-Harati <i>et al.</i>	(FNAL KTeV Collab.)
BATLEY	02	PL B544 97	J.R. Batley <i>et al.</i>	(CERN NA48 Collab.)
BRFIT	02	RPP 2002 edition	T.G. Trippe	(PDG Collab.)
Fits for $K_L^0$ CP-Violation Parameters				
ETAFIT	02	RPP 2002 edition	T.G. Trippe	(PDG Collab.)
Fits for $K_L^0$ CP-Violation Parameters				
KL3FIT	02	RPP 2002 edition	T.G. Trippe	(PDG Collab.)
$K_{\mu 3}^{\pm}$ and $K_{\mu 3}^0$ Form Factors review in $K^+$ Listings.				
LAI	02B	PL B536 229	A. Lai <i>et al.</i>	(CERN NA48 Collab.)
ALAVI-HARATI	01	PRL 86 397	A. Alavi-Harati <i>et al.</i>	(FNAL KTeV Collab.)
ALAVI-HARATI	01B	PRL 86 761	A. Alavi-Harati <i>et al.</i>	(FNAL KTeV Collab.)
ALAVI-HARATI	01D	PRL 86 5425	A. Alavi-Harati <i>et al.</i>	(FNAL KTeV Collab.)
ALAVI-HARATI	01E	PRL 87 021801	A. Alavi-Harati <i>et al.</i>	(FNAL KTeV Collab.)
ALAVI-HARATI	01F	PR D64 012003	A. Alavi-Harati <i>et al.</i>	(FNAL KTeV Collab.)
ALAVI-HARATI	01G	PRL 87 071801	A. Alavi-Harati <i>et al.</i>	(FNAL KTeV Collab.)
ALAVI-HARATI	01H	PRL 87 111802	A. Alavi-Harati <i>et al.</i>	(FNAL KTeV Collab.)
ALAVI-HARATI	01J	PR D64 112004	A. Alavi-Harati <i>et al.</i>	(FNAL KTeV Collab.)
ANGELOPO...	01	PL B503 49	A. Angelopoulos <i>et al.</i>	(CLEAR Collab.)
ANGELOPO...	01B	EPJ C22 55	A. Angelopoulos <i>et al.</i>	(CLEAR Collab.)
LAI	01B	PL B515 261	A. Lai <i>et al.</i>	(CERN NA48 Collab.)
LAI	01C	EPJ C22 231	A. Lai <i>et al.</i>	(CERN NA48 Collab.)
ALAVI-HARATI	00	PR D61 072006	A. Alavi-Harati <i>et al.</i>	(FNAL KTeV Collab.)
ALAVI-HARATI	00B	PRL 84 408	A. Alavi-Harati <i>et al.</i>	(FNAL KTeV Collab.)
ALAVI-HARATI	00D	PRL 84 5279	A. Alavi-Harati <i>et al.</i>	(FNAL KTeV Collab.)
ALAVI-HARATI	00E	PR D62 112001	A. Alavi-Harati <i>et al.</i>	(FNAL KTeV Collab.)
AMBROSE	00	PRL 84 1389	D. Ambrose <i>et al.</i>	(BNL E871 Collab.)
APOSTOLA...	00	PL B473 186	A. Apostolakis <i>et al.</i>	(CLEAR Collab.)
PDG	00	EPJ C15 1	D.E. Groom <i>et al.</i>	
ADAMS	99	PL B447 240	J. Adams <i>et al.</i>	(FNAL KTeV Collab.)
ALAVI-HARATI	99B	PRL 83 917	A. Alavi-Harati <i>et al.</i>	(FNAL KTeV Collab.)
ALAVI-HARATI	99D	PRL 83 22	A. Alavi-Harati <i>et al.</i>	(FNAL KTeV Collab.)
APOSTOLA...	99C	PL B458 545	A. Apostolakis <i>et al.</i>	(CLEAR Collab.)
Also	00B	EPJ C18 41	A. Apostolakis <i>et al.</i>	(CLEAR Collab.)
FANTI	99B	PL B458 553	V. Fanti <i>et al.</i>	(CERN NA48 Collab.)
FANTI	99C	PL B465 335	V. Fanti <i>et al.</i>	(CERN NA48 Collab.)
MURAKAMI	99	PL B463 333	K. Murakami <i>et al.</i>	(KEK E162 Collab.)
ADAMS	98	PRL 80 4123	J. Adams <i>et al.</i>	(FNAL KTeV Collab.)
AMBROSE	98	PRL 81 4309	D. Ambrose <i>et al.</i>	(BNL E871 Collab.)
AMBROSE	98B	PRL 81 5734	D. Ambrose <i>et al.</i>	(BNL E871 Collab.)
ANGELOPO...	98	PL B420 191	A. Angelopoulos <i>et al.</i>	(CLEAR Collab.)
ANGELOPO...	98C	EPJ C5 389	A. Angelopoulos <i>et al.</i>	(CLEAR Collab.)
ANGELOPO...	98D	PL B444 38	A. Angelopoulos <i>et al.</i>	(CLEAR Collab.)
Also	01B	EPJ C22 55	A. Angelopoulos <i>et al.</i>	(CLEAR Collab.)
ANGELOPO...	98E	PL B444 43	A. Angelopoulos <i>et al.</i>	(CLEAR Collab.)
ARISAKA	98	PL B432 230	K. Arisaka <i>et al.</i>	(FNAL E799 Collab.)
BENDER	98	PL B418 411	M. Bender <i>et al.</i>	(CERN NA48 Collab.)
SETZU	98	PL B420 205	M.G. Setzu <i>et al.</i>	
TAKEUCHI	98	PL B443 409	Y. Takeuchi <i>et al.</i>	(KYOT, KEK, HIRO)
FANTI	97	ZPHY C76 653	V. Fanti <i>et al.</i>	(CERN NA48 Collab.)
NOMURA	97	PL B408 445	T. Nomura <i>et al.</i>	(KYOT, KEK, HIRO)
ADLER	96B	ZPHY C70 211	R. Adler <i>et al.</i>	(CLEAR Collab.)
ADLER	96C	PL B369 367	R. Adler <i>et al.</i>	(CLEAR Collab.)
GU	96	PRL 76 4312	P. Gu <i>et al.</i>	(RUTG, UCLA, EFI, COLO+)
LEBER	96	PL B369 69	F. Leber <i>et al.</i>	(MANZ, CERN, EDIN, ORSAY+)
PDG	96	PR D54 1	R. M. Barnett <i>et al.</i>	
ADLER	95	PL B363 237	R. Adler <i>et al.</i>	(CLEAR Collab.)
ADLER	95B	PL B363 243	R. Adler <i>et al.</i>	(CLEAR Collab.)
AKAGI	95	PR D51 2061	T. Akagi <i>et al.</i>	(TOHOK, TOKY, KYOT, KEK)
BARR	95	ZPHY C65 361	G.D. Barr <i>et al.</i>	(CERN, EDIN, MANZ, LALO+)
BARR	95C	PL B358 399	G.D. Barr <i>et al.</i>	(CERN, EDIN, MANZ, LALO+)
HEINSON	95	PR D51 985	A.P. Heinson <i>et al.</i>	(BNL E791 Collab.)
KREUTZ	95	ZPHY C65 67	A. Kreutz <i>et al.</i>	(SIEG, EDIN, MANZ, ORSAY+)
MATTHEWS	95	PRL 75 2803	J.N. Matthews <i>et al.</i>	(RUTG, EFI, ELMT+)
SCHWINGEN...	95	PRL 74 4376	B. Schwingerheuer <i>et al.</i>	(EFI, CHIC+)

SPENCER	95	PRL 74 3323	M.B. Spencer <i>et al.</i>	(UCLA, EFI, COLO+)
BARR	94	PL B328 528	G.D. Barr <i>et al.</i>	(CERN, EDIN, MANZ, LALO+)
GU	94	PRL 72 3000	P. Gu <i>et al.</i>	(RUTG, UCLA, EFI, COLO+)
NAKAYA	94	PRL 73 2169	T. Nakaya <i>et al.</i>	(OSAK, UCLA, EFI, COLU+)
ROBERTS	94	PR D50 1874	D. Roberts <i>et al.</i>	(UCLA, EFI, COLU+)
WEAVER	94	PRL 72 3758	M. Weaver <i>et al.</i>	(UCLA, EFI, COLU, ELMT+)
AKAGI	93	PR D47 R2644	T. Akagi <i>et al.</i>	(TOHOK, TOKY, KYOT, KEK)
ARISAKA	93	PRL 70 1049	K. Arisaka <i>et al.</i>	(BNL E791 Collab.)
ARISAKA	93B	PRL 71 3910	K. Arisaka <i>et al.</i>	(BNL E791 Collab.)
BARR	93D	PL B317 233	G.D. Barr <i>et al.</i>	(CERN, EDIN, MANZ, LALO+)
GIBBONS	93	PRL 70 1199	L.K. Gibbons <i>et al.</i>	(FNAL E731 Collab.)
Also	97	PR D55 6625	L.K. Gibbons <i>et al.</i>	(FNAL E731 Collab.)
GIBBONS	93B	PRL 70 1203	L.K. Gibbons <i>et al.</i>	(FNAL E731 Collab.)
GIBBONS	93C	Thesis RX-1487	L.K. Gibbons	(CHIC)
Also	97	PR D55 6625	L.K. Gibbons <i>et al.</i>	(FNAL E731 Collab.)
HARRIS	93	PRL 71 3914	D.A. Harris <i>et al.</i>	(EFI, UCLA, COLO+)
HARRIS	93B	PRL 71 3918	D.A. Harris <i>et al.</i>	(EFI, UCLA, COLO+)
MAKOFF	93	PRL 70 1591	G. Makoff <i>et al.</i>	(FNAL E731 Collab.)
Also	95	PRL 75 2069 (erratum)	G. Makoff <i>et al.</i>	
RAMBERG	93	PRL 70 2525	E. Ramberg <i>et al.</i>	(FNAL E731 Collab.)
RAMBERG	93B	PRL 70 2529	E.J. Ramberg <i>et al.</i>	(FNAL E731 Collab.)
VAGINS	93	PRL 71 35	M.R. Vagins <i>et al.</i>	(BNL E845 Collab.)
ADLER	92B	PL B286 180	R. Adler <i>et al.</i>	(CPLEAR Collab.)
Also	92	SJNP 55 840	R. Adler <i>et al.</i>	(CPLEAR Collab.)
BARR	92	PL B284 440	G.D. Barr <i>et al.</i>	(CERN, EDIN, MANZ, LALO+)
GRAHAM	92	PL B295 169	G.E. Graham <i>et al.</i>	(FNAL E731 Collab.)
MORSE	92	PR D45 36	W.M. Morse <i>et al.</i>	(BNL, YALE, VASS)
PDG	92	PR D45, 1 June, Part II	K. Hikasa <i>et al.</i>	(KEK, LBL, BOST+)
SOMALWAR	92	PRL 68 2580	S.V. Somalwar <i>et al.</i>	(FNAL E731 Collab.)
AKAGI	91B	PRL 67 2618	T. Akagi <i>et al.</i>	(TOHOK, TOKY, KYOT, KEK)
BARR	91	PL B259 389	G.D. Barr <i>et al.</i>	(CERN, EDIN, MANZ, LALO+)
HEINSON	91	PR D44 R1	A.P. Heinson <i>et al.</i>	(UCI, UCLA, LANL+)
PAPADIMITR...	91	PR D44 R573	V. Papadimitriou <i>et al.</i>	(FNAL E731 Collab.)
BARKER	90	PR D41 3546	A.R. Barker <i>et al.</i>	(FNAL E731 Collab.)
Also	88	PRL 61 2661	L.K. Gibbons <i>et al.</i>	(FNAL E731 Collab.)
BARR	90B	PL B240 283	G.D. Barr <i>et al.</i>	(CERN, EDIN, MANZ, LALO+)
BARR	90C	PL B242 523	G.D. Barr <i>et al.</i>	(CERN, EDIN, MANZ, LALO+)
CAROSI	90	PL B237 303	R. Carosi <i>et al.</i>	(CERN, EDIN, MANZ, LALO+)
KARLSSON	90	PRL 64 2976	M. Karlsson <i>et al.</i>	(FNAL E731 Collab.)
OHL	90	PRL 64 2755	K.E. Ohl <i>et al.</i>	(BNL E845 Collab.)
OHL	90B	PRL 65 1407	K.E. Ohl <i>et al.</i>	(BNL E845 Collab.)
PATTERSON	90	PRL 64 1491	J.R. Patterson <i>et al.</i>	(FNAL E731 Collab.)
INAGAKI	89	PR D40 1712	T. Inagaki <i>et al.</i>	(KEK, TOKY, KYOT)
MATHIAZHA...	89	PRL 63 2181	C. Mathiazhagan <i>et al.</i>	(UCI, UCLA, LANL+)
MATHIAZHA...	89B	PRL 63 2185	C. Mathiazhagan <i>et al.</i>	(UCI, UCLA, LANL+)
WAHL	89	CERN-EP/89-86	H. Wahl	(CERN)
BARR	88	PL B214 303	G.D. Barr <i>et al.</i>	(CERN, EDIN, MANZ, LALO+)
BURKHARDT	88	PL B206 169	H. Burkhardt <i>et al.</i>	(CERN, EDIN, MANZ+)
JASTRZEM...	88	PRL 61 2300	E. Jastrzembski <i>et al.</i>	(BNL, YALE)
WOODS	88	PRL 60 1695	M. Woods <i>et al.</i>	(FNAL E731 Collab.)
BURKHARDT	87	PL B199 139	H. Burkhardt <i>et al.</i>	(CERN, EDIN, MANZ+)
ARONSON	86	PR D33 3180	S.H. Aronson <i>et al.</i>	(BNL, CHIC, STAN+)
Also	82	PRL 48 1078	S.H. Aronson <i>et al.</i>	(BNL, CHIC, STAN+)
PDG	86C	PL 170B 132	M. Aguilar-Benitez <i>et al.</i>	(CERN, CIT+)
COUPAL	85	PRL 55 566	D.P. Coupal <i>et al.</i>	(CHIC, SACL)
BALATS	83	SJNP 38 556	M.Y. Balats <i>et al.</i>	(ITEP)
BERGSTROM	83	PL 131B 229	L. Bergstrom, E. Masso, P. Singer	(CERN)
ARONSON	82	PRL 48 1078	S.H. Aronson <i>et al.</i>	(BNL, CHIC, STAN+)
ARONSON	82B	PRL 48 1306	S.H. Aronson <i>et al.</i>	(BNL, CHIC, PURD)
Also	82B	PL 116B 73	E. Fischbach <i>et al.</i>	(PURD, BNL, CHIC)
Also	83	PR D28 476	S.H. Aronson <i>et al.</i>	(BNL, CHIC, PURD)
Also	83B	PR D28 495	S.H. Aronson <i>et al.</i>	(BNL, CHIC, PURD)
PDG	82B	PL 111B 70	M. Roos <i>et al.</i>	(HELS, CIT, CERN)
BIRULEV	81	NP B182 1	V.K. Birulev <i>et al.</i>	(JINR)
Also	80	SJNP 31 622	V.K. Birulev <i>et al.</i>	(JINR)
CARROLL	80B	PRL 44 529	A.S. Carroll <i>et al.</i>	(BNL, ROCH)
CARROLL	80C	PL 96B 407	A.S. Carroll <i>et al.</i>	(BNL, ROCH)
CHO	80	PR D22 2688	Y. Cho <i>et al.</i>	(ANL, CMU)
MORSE	80	PR D21 1750	W.M. Morse <i>et al.</i>	(BNL, YALE)

CHRISTENS...	79	PRL 43 1209	J.H. Christenson <i>et al.</i>	(NYU)
HILL	79	NP B153 39	D.G. Hill <i>et al.</i>	(BNL, SLAC, SBER)
SCHMIDT	79	PRL 43 556	M.P. Schmidt <i>et al.</i>	(YALE, BNL)
ENGLER	78B	PR D18 623	A. Engler <i>et al.</i>	(CMU, ANL)
HILL	78	PL 73B 483	D.G. Hill <i>et al.</i>	(BNL, SLAC, SBER)
CHO	77	PR D15 587	Y. Cho <i>et al.</i>	(ANL, CMU)
CLARK	77	PR D15 553	A.R. Clark <i>et al.</i>	(LBL)
Also	75	Thesis LBL-4275	G. Shen	(LBL)
DEVOE	77	PR D16 565	R. Devoe <i>et al.</i>	(EFI, ANL)
DZHORD...	77	SJNP 26 478	V.P. Dzhorzhadze <i>et al.</i>	(JINR)
		Translated from YAF 26	910.	
PEACH	77	NP B127 399	K.J. Peach <i>et al.</i>	(BGNA, EDIN, GLAS+)
BIRULEV	76	SJNP 24 178	V.K. Birulev <i>et al.</i>	(JINR)
		Translated from YAF 24	340.	
COOMBES	76	PRL 37 249	R.W. Coombes <i>et al.</i>	(STAN, NYU)
GJESDAL	76	NP B109 118	G. Gjesdal <i>et al.</i>	(CERN, HEIDH)
BALDO-...	75	NC 25A 688	M. Baldo-Ceolin <i>et al.</i>	(PADO, WISC)
BLUMENTHAL	75	PRL 34 164	R.B. Blumenthal <i>et al.</i>	(PENN, CHIC, TEMP)
BUCHANAN	75	PR D11 457	C.D. Buchanan <i>et al.</i>	(UCLA, SLAC, JHU)
CARITHERS	75	PRL 34 1244	W.C.J. Carithers <i>et al.</i>	(COLU, NYU)
SMITH	75B	Thesis UCSD unpub.	J.G. Smith	(UCSD)
ALBRECHT	74	PL 48B 393	K.F. Albrecht	(JINR, BERL, BUDA, PRAG, SERP+)
BISI	74	PL 50B 504	V. Bisi, M.I. Ferrero	(TORI)
DONALDSON	74	Thesis SLAC-0184	G. Donaldson	(SLAC)
Also	76	PR D14 2839	G. Donaldson <i>et al.</i>	(SLAC)
DONALDSON	74B	PR D9 2960	G. Donaldson <i>et al.</i>	(SLAC, UCSC)
Also	73B	PRL 31 337	G. Donaldson <i>et al.</i>	(SLAC, UCSC)
GEWENIGER	74	PL 48B 483	C. Geweniger <i>et al.</i>	(CERN, HEIDH)
Also	74	Thesis CERN Int. 74-4	V. Luth	(CERN)
GEWENIGER	74B	PL 48B 487	C. Geweniger <i>et al.</i>	(CERN, HEIDH)
Also	74B	PL 52B 119	S. Gjesdal <i>et al.</i>	(CERN, HEIDH)
GEWENIGER	74C	PL 52B 108	C. Geweniger <i>et al.</i>	(CERN, HEIDH)
GJESDAL	74	PL 52B 113	S. Gjesdal <i>et al.</i>	(CERN, HEIDH)
MESSNER	74	PRL 33 1458	R. Messner <i>et al.</i>	(COLO, SLAC, UCSC)
NIEBERGALL	74	PL 49B 103	F. Niebergall <i>et al.</i>	(CERN, ORSAY, VIEN)
WANG	74	PR D9 540	L. Wang <i>et al.</i>	(UMD, BNL)
WILLIAMS	74	PRL 33 240	H.H. Williams <i>et al.</i>	(BNL, YALE)
ALBROW	73	NP B58 22	M.G. Albrow <i>et al.</i>	(MCHS, DARE)
ALEXANDER	73B	NP B65 301	G. Alexander <i>et al.</i>	(TELA, HEID)
BRANDENB...	73	PR D8 1978	G.W. Brandenburg <i>et al.</i>	(SLAC)
EVANS	73	PR D7 36	G.R. Evans <i>et al.</i>	(EDIN, CERN)
Also	69	PRL 23 427	G.R. Evans <i>et al.</i>	(EDIN, CERN)
FACKLER	73	PRL 31 847	O. Fackler <i>et al.</i>	(MIT)
FITCH	73	PRL 31 1524	V.L. Fitch <i>et al.</i>	(PRIN)
Also	72	Thesis COO-3072-13	R.C. Webb	(PRIN)
GINSBERG	73	PR D8 3887	E.S. Ginsberg, J. Smith	(MIT, STON)
HART	73	NP B66 317	J.C. Hart <i>et al.</i>	(CAVE, RHEL)
MALLARY	73	PR D7 1953	M.L. Mallary <i>et al.</i>	(CIT)
Also	70	PRL 25 1214	F.J. Sciulli <i>et al.</i>	(CIT)
MCCARTHY	73	PR D7 687	R.L. McCarthy <i>et al.</i>	(LBL)
Also	72	PL 42B 291	R.L. McCarthy <i>et al.</i>	(LBL)
Also	71	Thesis LBL-550	R.L. McCarthy	(LBL)
MESSNER	73	PRL 30 876	R. Messner <i>et al.</i>	(COLO, SLAC, UCSC)
PEACH	73	PL 43B 441	K.J. Peach <i>et al.</i>	(EDIN, CERN, AACH)
SANDWEISS	73	PRL 30 1002	J. Sandweiss <i>et al.</i>	(YALE, ANL)
WILLIAMS	73	PRL 31 1521	H.H. Williams <i>et al.</i>	(BNL, YALE)
ALBROW	72	NP B44 1	M.G. Albrow <i>et al.</i>	(MCHS, DARE)
ASHFORD	72	PL 38B 47	V.A. Ashford <i>et al.</i>	(UCSD)
BANNER	72B	PRL 29 237	M. Banner <i>et al.</i>	(PRIN)
BARMIN	72B	SJNP 15 638	V.V. Barmin <i>et al.</i>	(ITEP)
		Translated from YAF 15	1152.	
BURGUN	72	NP B50 194	G. Burgun <i>et al.</i>	(SACL, CERN, OSLO)
DALLY	72	PL 41B 647	E.B. Dally <i>et al.</i>	(SLAC, JHU, UCLA)
Also	70	PL 33B 627	C.Y. Chien <i>et al.</i>	(JHU, SLAC, UCLA)
Also	71	PL 35B 261	C.Y. Chien <i>et al.</i>	(JHU, SLAC, UCLA)
GRAHAM	72	NC 9A 166	M.F. Graham <i>et al.</i>	(ILL, NEAS)
JAMES	72	NP B49 1	F. James <i>et al.</i>	(CERN, SACL, OSLO)
KRENZ	72	LNC 4 213	W. Krenz <i>et al.</i>	(AACH, CERN, EDIN)
MANN	72	PR D6 137	W.A. Mann <i>et al.</i>	(MASA, BNL, YALE)
MANTSCH	72	NC 9A 160	P.M. Mantsch <i>et al.</i>	(ILL, NEAS)
MCCARTHY	72	PL 42B 291	R.L. McCarthy <i>et al.</i>	(LBL)
NEUHOFER	72	PL 41B 642	G. Neuhofer <i>et al.</i>	(CERN, ORSAY, VIEN)

PICCIONI	72	PRL 29 1412	R. Piccioni <i>et al.</i>	(SLAC)
Also	74	PR D9 2939	R. Piccioni <i>et al.</i>	(SLAC, UCSC, COLO)
VOSBURGH	72	PR D6 1834	K.G. Vosburgh <i>et al.</i>	(RUTG, MASA)
Also	71	PRL 26 866	K.G. Vosburgh <i>et al.</i>	(RUTG, MASA)
BALATS	71	SJNP 13 53	M.Y. Balats <i>et al.</i>	(ITEP)
		Translated from YAF 13	93.	
BARMIN	71	PL 35B 604	V.V. Barmin <i>et al.</i>	(ITEP)
BISI	71	PL 36B 533	V. Bisi <i>et al.</i>	(AACH, CERN, TORI)
BURGUN	71	LNC 2 1169	G. Burgun <i>et al.</i>	(SACL, CERN, OSLO)
CARNEGIE	71	PR D4 1	R.K. Carnegie <i>et al.</i>	(PRIN)
CHAN	71	Thesis LBL-350	J.H.S. Chan	(LBL)
CHIEN	71	PL 35B 261	C.Y. Chien <i>et al.</i>	(JHU, SLAC, UCLA)
Also	72	PL 41B 647	E.B. Dally <i>et al.</i>	(SLAC, JHU, UCLA)
CHO	71	PR D3 1557	Y. Cho <i>et al.</i>	(CMU, BNL, CASE)
ENSTROM	71	PR D4 2629	J. Enstrom <i>et al.</i>	(SLAC, STAN)
Also	70	Thesis SLAC-0125	J.E. Enstrom	(STAN)
JAMES	71	PL 35B 265	F. James <i>et al.</i>	(CERN, SACL, OSLO)
MEISNER	71	PR D3 59	G.W. Meisner <i>et al.</i>	(MASA, BNL, YALE)
REPELLIN	71	PL 36B 603	J.P. Repellin <i>et al.</i>	(ORSAY, CERN)
WEBBER	71	PR D3 64	B.R. Webber <i>et al.</i>	(LRL)
Also	68	PRL 21 498	B.R. Webber <i>et al.</i>	(LRL)
Also	69	Thesis UCRL 19226	B.R. Webber	(LRL)
WOLFF	71	PL 36B 517	B. Wolff <i>et al.</i>	(ORSAY, CERN)
ALBROW	70	PL 33B 516	M.G. Albrow <i>et al.</i>	(MCHS, DARE)
ARONSON	70	PRL 25 1057	S.H. Aronson <i>et al.</i>	(EFI, ILLC, SLAC)
BARMIN	70	PL 33B 377	V.V. Barmin <i>et al.</i>	(ITEP, JINR)
BASILE	70	PR D2 78	P. Basile <i>et al.</i>	(SACL)
BECHERRAWY	70	PR D1 1452	T. Becherrawy	(ROCH)
BUCHANAN	70	PL 33B 623	C.D. Buchanan <i>et al.</i>	(SLAC, JHU, UCLA)
Also	71	Private Comm.	A.J. Cox	
BUDAGOV	70	PR D2 815	I.A. Budagov <i>et al.</i>	(CERN, ORSAY, EPOL)
Also	68B	PL 28B 215	I.A. Budagov <i>et al.</i>	(CERN, ORSAY, EPOL)
CHIEN	70	PL 33B 627	C.Y. Chien <i>et al.</i>	(JHU, SLAC, UCLA)
Also	71	Private Comm.	A.J. Cox	
CHO	70	PR D1 3031	Y. Cho <i>et al.</i>	(CMU, BNL, CASE)
Also	67	PRL 19 668	D.G. Hill <i>et al.</i>	(BNL, CMU)
CHOLLET	70	PL 31B 658	J.C. Chollet <i>et al.</i>	(CERN)
CULLEN	70	PL 32B 523	M. Cullen <i>et al.</i>	(AACH, CERN, TORI)
GINSBERG	70	PR D1 229	E.S. Ginsberg	(HAIF)
MARX	70	PL 32B 219	J. Marx <i>et al.</i>	(COLU, HARV, CERN)
Also	70B	Thesis Nevis 179	J. Marx	(COLU)
SCRIBANO	70	PL 32B 224	A. Scribano <i>et al.</i>	(PISA, COLU, HARV)
SMITH	70	PL 32B 133	R.C. Smith <i>et al.</i>	(UMD, BNL)
WEBBER	70	PR D1 1967	B.R. Webber <i>et al.</i>	(LRL)
Also	69	Thesis UCRL 19226	B.R. Webber	(LRL)
BANNER	69	PR 188 2033	M. Banner <i>et al.</i>	(PRIN)
Also	68	PRL 21 1103	M. Banner <i>et al.</i>	(PRIN)
Also	68	PRL 21 1107	J.W. Cronin, J.K. Liu, J.E. Pilcher	(PRIN)
BEILLIERE	69	PL 30B 202	P. Beilliere, G. Boutang, J. Limon	(EPOL)
BENNETT	69	PL 29B 317	S. Bennett <i>et al.</i>	(COLU, BNL)
EVANS	69	PRL 23 427	G.R. Evans <i>et al.</i>	(EDIN, CERN)
FAISSNER	69	PL 30B 204	H. Faissner <i>et al.</i>	(AACH3, CERN, TORI)
LITTENBERG	69	PRL 22 654	L.S. Littenberg <i>et al.</i>	(UCSD)
LONGO	69	PR 181 1808	M.J. Longo, K.K. Young, J.A. Helland	(MICH, UCLA)
PACIOTTI	69	Thesis UCRL 19446	M.A. Paciotti	(LRL)
SAAL	69	Thesis	H.J. Saal	(COLU)
ABRAMS	68B	PR 176 1603	R.J. Abrams <i>et al.</i>	(ILL)
ARNOLD	68B	PL 28B 56	R.G. Arnold <i>et al.</i>	(CERN, ORSAY)
ARONSON	68	PRL 20 287	S.H. Aronson, K.W. Chen	(PRIN)
Also	69	PR 175 1708	S.H. Aronson, K.W. Chen	(PRIN)
BASILE	68	PL 26B 542	P. Basile <i>et al.</i>	(SACL)
BASILE	68B	PL 28B 58	P. Basile <i>et al.</i>	(SACL)
BENNETT	68	PL 27B 244	S. Bennett <i>et al.</i>	(COLU, CERN)
BLANPIED	68	PRL 21 1650	W.A. Blanpied <i>et al.</i>	(CASE, HARV, MCGI)
BOHM	68B	PL 27B 594	A. Bohm <i>et al.</i>	
BUDAGOV	68	NC 57A 182	I.A. Budagov <i>et al.</i>	(CERN, ORSAY, IPNP)
Also	68B	PL 28B 215	I.A. Budagov <i>et al.</i>	(CERN, ORSAY, EPOL)
JAMES	68	NP B8 365	F. James, H. Briand	(IPNP, CERN)
Also	68	PRL 21 257	J.A. Helland, M.J. Longo, K.K. Young	(UCLA, MICH)
KULYUKINA	68	JETP 26 20	L.A. Kulyukina <i>et al.</i>	(JINR)
		Translated from ZETF 53	29.	

KUNZ	68	Thesis PU-68-46	P.F. Kunz	(PRIN)
BENNETT	67	PRL 19 993	S. Bennett <i>et al.</i>	(COLU)
DEBOUARD	67	NC 52A 662	X. de Bouard <i>et al.</i>	(CERN)
Also	65	PL 15 58	X. de Bouard <i>et al.</i>	(CERN, ORSAY, MPIM)
DEVLIN	67	PRL 18 54	T.J. Devlin <i>et al.</i>	(PRIN, UMD)
Also	68	PR 169 1045	G.A. Sayer <i>et al.</i>	(UMD, PPA, PRIN)
DORFAN	67	PRL 19 987	D.E. Dorfan <i>et al.</i>	(SLAC, LRL)
FELDMAN	67B	PR 155 1611	L. Feldman <i>et al.</i>	(PENN)
FITCH	67	PR 164 1711	V.L. Fitch <i>et al.</i>	(PRIN)
GINSBERG	67	PR 162 1570	E.S. Ginsberg	(MASB)
HILL	67	PRL 19 668	D.G. Hill <i>et al.</i>	(BNL, CMU)
HOPKINS	67	PRL 19 185	H.W.K. Hopkins, T.C. Bacon, F.R. Eisler	(BNL)
KULYUKINA	67	Preprint	L.A. Kulyukina <i>et al.</i>	(JINR)
LOWYS	67	PL 24B 75	J.P. Lowys <i>et al.</i>	(EPOL, ORSAY)
NEFKENS	67	PR 157 1233	B.M.K. Nefkens <i>et al.</i>	(ILL)
SCHMIDT	67	Thesis Nevis 160	P. Schmidt	(COLU)
AUERBACH	66B	PRL 17 980	L.B. Auerbach <i>et al.</i>	(PENN)
BEHR	66	PL 22 540	L. Behr <i>et al.</i>	(EPOL, MILA, PADO, ORSAY)
CARPENTER	66	PR 142 871	D.W. Carpenter <i>et al.</i>	(ILL)
HAWKINS	66	PL 21 238	C.J.B. Hawkins	(YALE)
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