



$$I(J^P) = \frac{1}{2}(0^-)$$

$m_{K_L^0} - m_{K_S^0}$

For earlier measurements, beginning with GOOD 61 and FITCH 61, see our 1986 edition, Physics Letters **170B** 132 (1986).

OUR FIT is described in the note on "Fits for K_L^0 CP-Violation Parameters" in the K_L^0 Particle Listings.

VALUE ($10^{10} \hbar s^{-1}$)	DOCUMENT ID	TECN	COMMENT
0.5300 ± 0.0012	OUR FIT		
0.5307 ± 0.0015	OUR AVERAGE Error includes scale factor of 1.1.		
0.5240 ± 0.0044 ± 0.0033	APOSTOLA...	99C CPLR	$K^0 - \bar{K}^0$ to $\pi^+ \pi^-$
0.5295 ± 0.0020 ± 0.0003	¹ ANGELOPO...	98D CPLR	
0.5297 ± 0.0030 ± 0.0022	² SCHWINGEN...	95 E773	20–160 GeV <i>K</i> beams
0.5257 ± 0.0049 ± 0.0021	² GIBBONS	93C E731	20–160 GeV <i>K</i> beams
0.5340 ± 0.00255 ± 0.0015	³ GEWENIGER	74C SPEC	Gap method
0.5334 ± 0.0040 ± 0.0015	³ GJESDAL	74 SPEC	Charge asymmetry in $K_{\ell 3}^0$
0.542 ± 0.006	CULLEN	70 CNTR	
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●			
0.5307 ± 0.0013	⁴ ADLER	96C RVUE	
0.5274 ± 0.0029 ± 0.0005	¹ ADLER	95 CPLR	Sup. by ANGELOPOULOS 98D
0.5286 ± 0.0028	⁵ GIBBONS	93 E731	20–160 GeV <i>K</i> beams
0.482 ± 0.014	⁶ ARONSON	82B SPEC	$E=30-110$ GeV
0.534 ± 0.007	⁷ CARNEGIE	71 ASPK	Gap method
0.542 ± 0.006	⁷ ARONSON	70 ASPK	Gap method

- ¹ Uses \bar{K}_{e3}^0 and K_{e3}^0 strangeness tagging at production and decay.
- ² Fits Δm and ϕ_{+-} simultaneously. GIBBONS 93C systematic error is from B. Winstein via private communication.
- ³ These two experiments have a common systematic error due to the uncertainty in the momentum scale, as pointed out in WAHL 89.
- ⁴ ADLER 96C is the result of a fit which includes nearly the same data as entered into the "OUR FIT" value above.
- ⁵ GIBBONS 93 value assume $\phi_{+-} = \phi_{00} = \phi_{SW} = (43.7 \pm 0.2)^\circ$.
- ⁶ ARONSON 82 find that Δm may depend on the kaon energy.
- ⁷ ARONSON 70 and CARNEGIE 71 use K_S^0 mean life = $(0.862 \pm 0.006) \times 10^{-10}$ s. We have not attempted to adjust these values for the subsequent change in the K_S^0 mean life or in η_{+-} .

K_L^0 MEAN LIFE

VALUE (10^{-8} s)	EVTS	DOCUMENT ID	TECN
5.17 ± 0.04	OUR FIT Error includes scale factor of 1.1.		
5.15 ± 0.04	OUR AVERAGE		
5.154 ± 0.044	0.4M	VOSBURGH	72 CNTR
5.15 ± 0.14		DEVLIN	67 CNTR

• • • We do not use the following data for averages, fits, limits, etc. • • •

5.0	± 0.5		⁸ LOWYS	67	HLBC
6.1	$+1.5$ -1.2	1700	ASTBURY	65C	CNTR
5.3	± 0.6		FUJII	64	OSPK
5.1	$+2.4$ -1.3	15	DARMON	62	FBC
8.1	$+3.2$ -2.4	34	BARDON	58	CNTR

⁸Sum of partial decay rates.

K_L^0 DECAY MODES

	Mode	Fraction (Γ_i/Γ)	Scale factor/ Confidence level
Γ_1	$3\pi^0$	(21.13 \pm 0.27) %	S=1.1
Γ_2	$\pi^+\pi^-\pi^0$	(12.55 \pm 0.20) %	S=1.7
Γ_3	$\pi^\pm\mu^\mp\nu_\mu$ Called $K_{\mu 3}^0$.	[a] (27.18 \pm 0.25) %	S=1.1
Γ_4	$\pi^-\mu^+\nu_\mu$		
Γ_5	$\pi^+\mu^-\bar{\nu}_\mu$		
Γ_6	$\pi^\pm e^\mp\nu_e$ Called $K_{e 3}^0$.	[a] (38.78 \pm 0.28) %	S=1.1
Γ_7	$\pi^-e^+\nu_e$		
Γ_8	$\pi^+e^-\bar{\nu}_e$		
Γ_9	2γ	(5.86 \pm 0.15) $\times 10^{-4}$	
Γ_{10}	3γ	< 2.4 $\times 10^{-7}$	CL=90%
Γ_{11}	$\pi^0 2\gamma$	[b] (1.68 \pm 0.10) $\times 10^{-6}$	
Γ_{12}	$\pi^0\pi^\pm e^\mp\nu$	[a] (5.18 \pm 0.29) $\times 10^{-5}$	
Γ_{13}	$(\pi\mu\text{atom})\nu$	(1.06 \pm 0.11) $\times 10^{-7}$	
Γ_{14}	$\pi^\pm e^\mp\nu_e\gamma$	[a,b,c] (3.62 $^{+0.26}_{-0.21}$) $\times 10^{-3}$	
Γ_{15}	$\pi^\pm\mu^\mp\nu_\mu\gamma$	(5.7 $^{+0.6}_{-0.7}$) $\times 10^{-4}$	
Γ_{16}	$\pi^+\pi^-\gamma$	[b,c] (4.61 \pm 0.14) $\times 10^{-5}$	
Γ_{17}	$\pi^0\pi^0\gamma$	< 5.6 $\times 10^{-6}$	
Γ_{18}	$\mu^+\mu^-\gamma$	(3.25 \pm 0.28) $\times 10^{-7}$	
Γ_{19}	$e^+e^-\gamma$	(10.0 \pm 0.5) $\times 10^{-6}$	S=1.5
Γ_{20}	$e^+e^-\gamma\gamma$	[b] (6.9 \pm 1.0) $\times 10^{-7}$	
Γ_{21}	$\pi^0\gamma e^+e^-$	< 7.1 $\times 10^{-7}$	CL=90%

**Charge conjugation \times Parity (CP , CPV) or Lepton Family number (LF)
violating modes, or $\Delta S = 1$ weak neutral current ($S1$) modes**

Γ_{22}	$\pi^+ \pi^-$	CPV	$(2.056 \pm 0.033) \times 10^{-3}$	
Γ_{23}	$\pi^0 \pi^0$	CPV	$(9.27 \pm 0.19) \times 10^{-4}$	
Γ_{24}	$\mu^+ \mu^-$	$S1$	$(7.15 \pm 0.16) \times 10^{-9}$	
Γ_{25}	$e^+ e^-$	$S1$	$(9 \quad \begin{smallmatrix} +6 \\ -4 \end{smallmatrix}) \times 10^{-12}$	
Γ_{26}	$\pi^+ \pi^- e^+ e^-$	$S1$ [b]	$(3.5 \pm 0.6) \times 10^{-7}$	
Γ_{27}	$\mu^+ \mu^- e^+ e^-$	$S1$	$(2.9 \quad \begin{smallmatrix} +6.7 \\ -2.4 \end{smallmatrix}) \times 10^{-9}$	
Γ_{28}	$e^+ e^- e^+ e^-$	$S1$	$(4.1 \pm 0.8) \times 10^{-8}$	$S=1.2$
Γ_{29}	$\pi^0 \mu^+ \mu^-$	$CP, S1$ [d]	$< 5.1 \times 10^{-9}$	$CL=90\%$
Γ_{30}	$\pi^0 e^+ e^-$	$CP, S1$ [d]	$< 4.3 \times 10^{-9}$	$CL=90\%$
Γ_{31}	$\pi^0 \nu \bar{\nu}$	$CP, S1$ [e]	$< 5.9 \times 10^{-7}$	$CL=90\%$
Γ_{32}	$e^\pm \mu^\mp$	LF [a]	$< 4.7 \times 10^{-12}$	$CL=90\%$
Γ_{33}	$e^\pm e^\pm \mu^\mp \mu^\mp$	LF [a]	$< 6.1 \times 10^{-9}$	$CL=90\%$
Γ_{34}	$\pi^0 \mu^\pm e^\mp$	LF [a]	$< 6.2 \times 10^{-9}$	$CL=90\%$

[a] The value is for the sum of the charge states or particle/antiparticle states indicated.

[b] See the Particle Listings below for the energy limits used in this measurement.

[c] Most of this radiative mode, the low-momentum γ part, is also included in the parent mode listed without γ 's.

[d] Allowed by higher-order electroweak interactions.

[e] Violates CP in leading order. Test of direct CP violation since the indirect CP -violating and CP -conserving contributions are expected to be suppressed.

CONSTRAINED FIT INFORMATION

An overall fit to the mean life, 4 decay rate, and 12 branching ratios uses 46 measurements and one constraint to determine 8 parameters. The overall fit has a $\chi^2 = 40.5$ for 39 degrees of freedom.

The following *off-diagonal* array elements are the correlation coefficients $\langle \delta p_i \delta p_j \rangle / (\delta p_i \cdot \delta p_j)$, in percent, from the fit to parameters p_i , including the branching fractions, $x_i \equiv \Gamma_i / \Gamma_{\text{total}}$. The fit constrains the x_i whose labels appear in this array to sum to one.

x_2	-19						
x_3	-37	-28					
x_6	-49	-28	-36				
x_9	-7	21	-5	-5			
x_{22}	-12	34	-8	-7	63		
x_{23}	-9	26	-6	-6	83	77	
Γ	0	0	0	0	0	0	0
	x_1	x_2	x_3	x_6	x_9	x_{22}	x_{23}

	Mode	Rate (10^8 s^{-1})	Scale factor
Γ_1	$3\pi^0$	0.0408 ± 0.0006	
Γ_2	$\pi^+ \pi^- \pi^0$	0.0243 ± 0.0004	1.5
Γ_3	$\pi^\pm \mu^\mp \nu_\mu$ Called $K_{\mu 3}^0$.	[a] 0.0525 ± 0.0007	1.1
Γ_6	$\pi^\pm e^\mp \nu_e$ Called $K_{e 3}^0$.	[a] 0.0750 ± 0.0008	1.1
Γ_9	2γ	$(1.133 \pm 0.030) \times 10^{-4}$	
Γ_{22}	$\pi^+ \pi^-$	$(3.97 \pm 0.07) \times 10^{-4}$	1.1
Γ_{23}	$\pi^0 \pi^0$	$(1.79 \pm 0.04) \times 10^{-4}$	

K_L^0 DECAY RATES

$\Gamma(3\pi^0)$						Γ_1
VALUE (10^6 s^{-1})	EVTS	DOCUMENT ID	TECN	COMMENT		
4.08 ± 0.06 OUR FIT						
$5.22^{+1.03}_{-0.84}$	54	BEHR	66 HLBC	Assumes CP		

$\Gamma(\pi^+\pi^-\pi^0)$

Γ_2

<u>VALUE (10^6 s^{-1})</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
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2.43±0.04 OUR FIT Error includes scale factor of 1.5.

2.38±0.09 OUR AVERAGE

2.32 ^{+0.13} _{-0.15}	192	BALDO-...	75	HLBC	Assumes <i>CP</i>
2.35±0.20	180	⁹ JAMES	72	HBC	Assumes <i>CP</i>
2.71±0.28	99	CHO	71	DBC	Assumes <i>CP</i>
2.12±0.33	50	MEISNER	71	HBC	Assumes <i>CP</i>
2.20±0.35	53	WEBBER	70	HBC	Assumes <i>CP</i>
2.62 ^{+0.28} _{-0.27}	136	BEHR	66	HLBC	Assumes <i>CP</i>

• • • We do not use the following data for averages, fits, limits, etc. • • •

2.5 ±0.3	98	⁹ JAMES	71	HBC	Assumes <i>CP</i>
3.26±0.77	18	ANDERSON	65	HBC	
1.4 ±0.4	14	FRANZINI	65	HBC	

In the fit this rate is well determined by the mean life and the branching ratio $\Gamma(\pi^+\pi^-\pi^0)/[\Gamma(\pi^+\pi^-\pi^0) + \Gamma(\pi^\pm\mu^\mp\nu_\mu) + \Gamma(\pi^\pm e^\mp\nu_e)]$. For this reason the discrepancy between the $\Gamma(\pi^+\pi^-\pi^0)$ measurements does not affect the scale factor of the overall fit.

⁹JAMES 72 is a final measurement and includes JAMES 71.

$\Gamma(\pi^\pm\mu^\mp\nu_\mu)$

Γ_3

<u>VALUE (10^6 s^{-1})</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
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5.25±0.07 OUR FIT Error includes scale factor of 1.1.

• • • We do not use the following data for averages, fits, limits, etc. • • •

4.54 ^{+1.24} _{-1.08}	19	LOWYS	67	HLBC	
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$\Gamma(\pi^\pm e^\mp\nu_e)$

Γ_6

<u>VALUE (10^6 s^{-1})</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
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7.50±0.08 OUR FIT Error includes scale factor of 1.1.

7.7 ±0.5 OUR AVERAGE

7.81±0.56	620	CHAN	71	HBC	
7.52 ^{+0.85} _{-0.72}		AUBERT	65	HLBC	$\Delta S=\Delta Q, CP$ assumed

$\Gamma(\pi^+\pi^-\pi^0) + \Gamma(\pi^\pm\mu^\mp\nu_\mu) + \Gamma(\pi^\pm e^\mp\nu_e)$ ($\Gamma_2+\Gamma_3+\Gamma_6$)

$K_L^0 \rightarrow$ charged.

<u>VALUE (10^6 s^{-1})</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
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15.18±0.14 OUR FIT Error includes scale factor of 1.1.

• • • We do not use the following data for averages, fits, limits, etc. • • •

15.1 ±1.9	98	AUERBACH	66B	OSPK	
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$\Gamma(\pi^\pm \mu^\mp \nu_\mu) + \Gamma(\pi^\pm e^\mp \nu_e)$ ($\Gamma_3 + \Gamma_6$)

VALUE (10^6 s^{-1})	EVTS	DOCUMENT ID	TECN	COMMENT
12.75 ± 0.12 OUR FIT	Error includes scale factor of 1.1.			
11.9 ± 0.6 OUR AVERAGE	Error includes scale factor of 1.2.			
12.4 ± 0.7	410	¹⁰ BURGUN	72 HBC	$K^+ p \rightarrow K^0 p \pi^+$
13.1 ± 1.3	252	¹⁰ WEBBER	71 HBC	$K^- p \rightarrow n \bar{K}^0$
11.6 ± 0.9	393	^{10,11} CHO	70 DBC	$K^+ n \rightarrow K^0 p$
9.85 ^{+1.15} _{-1.05}	109	¹⁰ FRANZINI	65 HBC	
• • • We do not use the following data for averages, fits, limits, etc. • • •				
8.47 ± 1.69	126	¹⁰ MANN	72 HBC	$K^- p \rightarrow n \bar{K}^0$
10.3 ± 0.8	335	¹¹ HILL	67 DBC	$K^+ n \rightarrow K^0 p$
¹⁰ Assumes $\Delta S = \Delta Q$ rule.				
¹¹ CHO 70 includes events of HILL 67.				

K_L^0 BRANCHING RATIOS

$\Gamma(3\pi^0)/\Gamma_{\text{total}}$ Γ_1/Γ

VALUE	EVTS	DOCUMENT ID	TECN	COMMENT
0.2113 ± 0.0027 OUR FIT	Error includes scale factor of 1.1.			
0.2105 ± 0.0028	38k	¹² KREUTZ	95 NA31	
¹² KREUTZ 95 measure $3\pi^0$, $\pi^+ \pi^- \pi^0$, and $\pi e \nu_e$ modes. They assume PDG 1992 values for $\pi \mu \nu_\mu$, 2π , and 2γ modes.				

$\Gamma(3\pi^0)/\Gamma(\pi^+ \pi^- \pi^0)$ Γ_1/Γ_2

VALUE	EVTS	DOCUMENT ID	TECN	COMMENT
1.68 ± 0.04 OUR FIT	Error includes scale factor of 1.3.			
1.63 ± 0.05 OUR AVERAGE	Error includes scale factor of 1.4.			
1.611 ± 0.014 ± 0.034	38k	¹³ KREUTZ	95 NA31	
1.80 ± 0.13	1010	BUDAGOV	68 HLBC	
2.0 ± 0.6	188	ALEKSANYAN	64B FBC	
• • • We do not use the following data for averages, fits, limits, etc. • • •				
1.65 ± 0.07	883	BARMIN	72B HLBC	Error statistical only
¹³ KREUTZ 95 excluded from fit because it is not independent of their $\Gamma(3\pi^0)/\Gamma_{\text{total}}$ measurement, which is in the fit.				

$\Gamma(3\pi^0)/\Gamma(\pi^\pm e^\mp \nu_e)$ Γ_1/Γ_6

VALUE	EVTS	DOCUMENT ID	TECN	COMMENT
0.545 ± 0.009 OUR FIT	Error includes scale factor of 1.1.			
0.545 ± 0.004 ± 0.009	38k	¹⁴ KREUTZ	95 NA31	
¹⁴ KREUTZ 95 measurement excluded from fit because it is not independent of their $\Gamma(3\pi^0)/\Gamma_{\text{total}}$ measurement, which is in the fit.				

$$\frac{\Gamma(3\pi^0)}{[\Gamma(\pi^+\pi^-\pi^0) + \Gamma(\pi^\pm\mu^\mp\nu_\mu) + \Gamma(\pi^\pm e^\mp\nu_e)]} \quad \Gamma_1/(\Gamma_2+\Gamma_3+\Gamma_6)$$

VALUE	EVTS	DOCUMENT ID	TECN	COMMENT
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0.269±0.004 OUR FIT Error includes scale factor of 1.1.

0.260±0.011 OUR AVERAGE

0.251±0.014	549	BUDAGOV	68	HLBC	ORSAY measur.
0.277±0.021	444	BUDAGOV	68	HLBC	Ecole polytec.meas
0.31 ^{+0.07} _{-0.06}	29	KULYUKINA	68	CC	
0.24 ±0.08	24	ANIKINA	64	CC	

$$\frac{\Gamma(\pi^+\pi^-\pi^0)}{\Gamma_{\text{total}}} \quad \Gamma_2/\Gamma$$

VALUE	DOCUMENT ID
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0.1255±0.0020 OUR FIT Error includes scale factor of 1.7.

$$\frac{\Gamma(\pi^+\pi^-\pi^0)}{[\Gamma(\pi^+\pi^-\pi^0) + \Gamma(\pi^\pm\mu^\mp\nu_\mu) + \Gamma(\pi^\pm e^\mp\nu_e)]} \quad \Gamma_2/(\Gamma_2+\Gamma_3+\Gamma_6)$$

VALUE	EVTS	DOCUMENT ID	TECN	COMMENT
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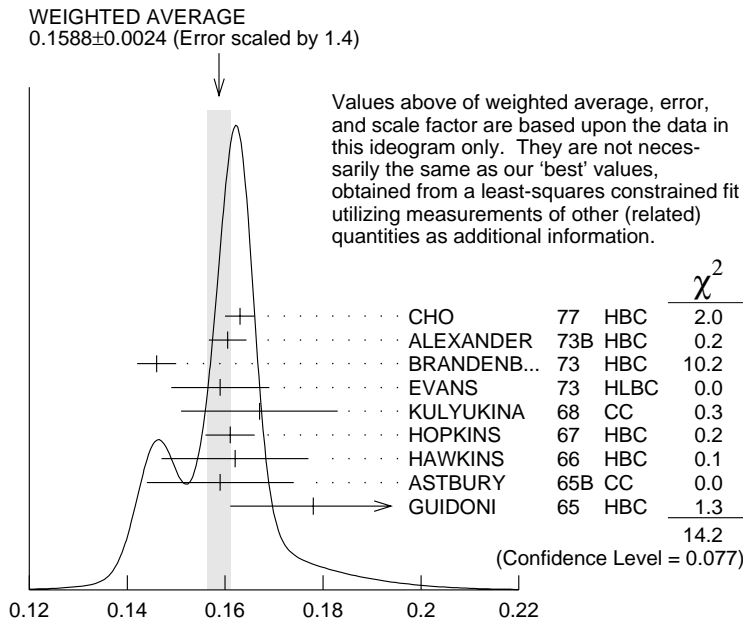
0.1599±0.0025 OUR FIT Error includes scale factor of 1.7.

0.1588±0.0024 OUR AVERAGE Error includes scale factor of 1.4. See the ideogram below.

0.163 ±0.003	6499	CHO	77	HBC	
0.1605±0.0038	1590	ALEXANDER	73B	HBC	
0.146 ±0.004	3200	BRANDENB...	73	HBC	
0.159 ±0.010	558	EVANS	73	HLBC	
0.167 ±0.016	1402	KULYUKINA	68	CC	
0.161 ±0.005		HOPKINS	67	HBC	
0.162 ±0.015	126	HAWKINS	66	HBC	
0.159 ±0.015	326	ASTBURY	65B	CC	
0.178 ±0.017	566	GUIDONI	65	HBC	

• • • We do not use the following data for averages, fits, limits, etc. • • •

0.15 ^{+0.03} _{-0.04}	66	ASTBURY	65	CC	
0.144 ±0.004	1729	HOPKINS	65	HBC	See HOPKINS 67
0.151 ±0.020	79	ADAIR	64	HBC	
0.157 ^{+0.03} _{-0.04}	75	LUERS	64	HBC	
0.185 ±0.038	59	ASTIER	61	CC	



$$\Gamma(\pi^+ \pi^- \pi^0) / [\Gamma(\pi^+ \pi^- \pi^0) + \Gamma(\pi^\pm \mu^\mp \nu_\mu) + \Gamma(\pi^\pm e^\mp \nu_e)]$$

$$\Gamma(\pi^+ \pi^- \pi^0) / \Gamma(\pi^\pm e^\mp \nu_e)$$

Γ_2/Γ_6

VALUE	EVTS	DOCUMENT ID	TECN
0.324±0.006 OUR FIT	Error includes scale factor of 1.6.		
0.336±0.003±0.007	28k	KREUTZ	95 NA31

$$\Gamma(\pi^\pm \mu^\mp \nu_\mu) / \Gamma(\pi^\pm e^\mp \nu_e)$$

Γ_3/Γ_6

VALUE	EVTS	DOCUMENT ID	TECN	COMMENT
0.701±0.009 OUR FIT				
0.697^{+0.010}_{-0.009} OUR AVERAGE				

0.702±0.011	33k	CHO	80	HBC
0.662±0.037	10k	WILLIAMS	74	ASPK
0.741±0.044	6700	BRANDENB...	73	HBC
0.662±0.030	1309	EVANS	73	HLBC
0.71 ±0.05	770	BUDAGOV	68	HLBC

• • • We do not use the following data for averages, fits, limits, etc. • • •

0.68 ±0.08	3548	BASILE	70	OSPK
0.71 ±0.04	569	¹⁵ BEILLIERE	69	HLBC
0.648±0.030	1309	EVANS	69	HLBC Repl. by EVANS 73
0.67 ±0.13		¹⁶ KULYUKINA	68	CC
0.82 ±0.10		DEBOUARD	67	OSPK
0.7 ±0.2	273	HAWKINS	67	HBC
0.81 ±0.08		HOPKINS	67	HBC
0.81 ±0.19		ADAIR	64	HBC

¹⁵BEILLIERE 69 is a scanning experiment using same exposure as BUDAGOV 68.

¹⁶ KULYUKINA 68 $\Gamma(\pi^\pm \mu^\mp \nu_\mu)/\Gamma(\pi^\pm e^\mp \nu_e)$ is not measured independently from $\Gamma(\pi^+ \pi^- \pi^0)/[\Gamma(\pi^+ \pi^- \pi^0) + \Gamma(\pi^\pm \mu^\mp \nu_\mu) + \Gamma(\pi^\pm e^\mp \nu_e)]$ and $\Gamma(\pi^\pm e^\mp \nu_e)/[\Gamma(\pi^+ \pi^- \pi^0) + \Gamma(\pi^\pm \mu^\mp \nu_\mu) + \Gamma(\pi^\pm e^\mp \nu_e)]$.

$$\Gamma(\pi^\pm \mu^\mp \nu_\mu)/[\Gamma(\pi^+ \pi^- \pi^0) + \Gamma(\pi^\pm \mu^\mp \nu_\mu) + \Gamma(\pi^\pm e^\mp \nu_e)] \quad \Gamma_3/(\Gamma_2+\Gamma_3+\Gamma_6)$$

VALUE EVTS DOCUMENT ID TECN

0.3461±0.0030 OUR FIT Error includes scale factor of 1.1.

• • • We do not use the following data for averages, fits, limits, etc. • • •

0.335 ±0.055	330	¹⁷ KULYUKINA	68	CC
0.39 ^{+0.08} _{-0.10}	172	¹⁷ ASTBURY	65	CC
0.356 ±0.07	251	¹⁷ LUERS	64	HBC

¹⁷ This mode not measured independently from $\Gamma(\pi^+ \pi^- \pi^0)/[\Gamma(\pi^+ \pi^- \pi^0) + \Gamma(\pi^\pm \mu^\mp \nu_\mu) + \Gamma(\pi^\pm e^\mp \nu_e)]$ and $\Gamma(\pi^\pm e^\mp \nu_e)/[\Gamma(\pi^+ \pi^- \pi^0) + \Gamma(\pi^\pm \mu^\mp \nu_\mu) + \Gamma(\pi^\pm e^\mp \nu_e)]$.

$$\Gamma(\pi^\pm e^\mp \nu_e)/[\Gamma(\pi^+ \pi^- \pi^0) + \Gamma(\pi^\pm \mu^\mp \nu_\mu) + \Gamma(\pi^\pm e^\mp \nu_e)] \quad \Gamma_6/(\Gamma_2+\Gamma_3+\Gamma_6)$$

VALUE EVTS DOCUMENT ID TECN

0.4940±0.0030 OUR FIT Error includes scale factor of 1.1.

• • • We do not use the following data for averages, fits, limits, etc. • • •

0.498 ±0.052	500	KULYUKINA	68	CC
0.46 ^{+0.08} _{-0.10}	202	ASTBURY	65	CC
0.487 ±0.05	153	LUERS	64	HBC
0.46 ±0.11	24	NYAGU	61	CC

$$\Gamma(\pi^\pm e^\mp \nu_e)/[\Gamma(\pi^\pm \mu^\mp \nu_\mu) + \Gamma(\pi^\pm e^\mp \nu_e)] \quad \Gamma_6/(\Gamma_3+\Gamma_6)$$

VALUE EVTS DOCUMENT ID TECN

0.5880±0.0033 OUR FIT

• • • We do not use the following data for averages, fits, limits, etc. • • •

0.415 ±0.120	320	ASTIER	61	CC
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$$[\Gamma(\pi^\pm \mu^\mp \nu_\mu) + \Gamma(\pi^\pm e^\mp \nu_e)]/\Gamma_{\text{total}} \quad (\Gamma_3+\Gamma_6)/\Gamma$$

VALUE DOCUMENT ID

0.6596±0.0030 OUR FIT Error includes scale factor of 1.2.

$$\Gamma(2\gamma)/\Gamma_{\text{total}} \quad \Gamma_9/\Gamma$$

VALUE (units 10⁻⁴) EVTS DOCUMENT ID TECN COMMENT

5.86±0.15 OUR FIT

• • • We do not use the following data for averages, fits, limits, etc. • • •

4.54±0.84		¹⁸ BANNER	72B	OSPK	
4.5 ±1.0	23	ENSTROM	71	OSPK	K_L^0 1.5–9 GeV/c
5.0 ±1.0		¹⁹ REPELLIN	71	OSPK	
5.5 ±1.1	90	KUNZ	68	OSPK	Norm.to 3 π (C+N)
7.4 ±1.6	33	²⁰ CRONIN	67	OSPK	
6.7 ±2.2	32	TODOROFF	67	OSPK	Repl. CRIEGEE 66
1.3 ±0.6		²¹ CRIEGEE	66	OSPK	

¹⁸ This value uses $(\eta_{00}/\eta_{+-})^2 = 1.05 \pm 0.14$. In general, $\Gamma(2\gamma)/\Gamma_{\text{total}} = [(4.32 \pm 0.55) \times 10^{-4}] [(\eta_{00}/\eta_{+-})^2]$.

¹⁹ Assumes regeneration amplitude in copper at 2 GeV is 22 mb. To evaluate for a given regeneration amplitude and error, multiply by $(\text{regeneration amplitude}/22\text{mb})^2$.

²⁰ CRONIN 67 replaced by KUNZ 68.

²¹ CRIEGEE 66 replaced by TODOROFF 67.

$\Gamma(2\gamma)/\Gamma(3\pi^0)$

Γ_9/Γ_1

VALUE (units 10^{-3})	EVTS	DOCUMENT ID	TECN	COMMENT
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2.77 ± 0.08 OUR FIT Error includes scale factor of 1.1.

• • • We do not use the following data for averages, fits, limits, etc. • • •

2.13 ± 0.43	28	BARMIN	71	HLBC
2.24 ± 0.28	115	BANNER	69	OSPK
2.5 ± 0.7	16	ARNOLD	68B	HLBC Vacuum decay

$\Gamma(2\gamma)/\Gamma(\pi^0\pi^0)$

Γ_9/Γ_{23}

VALUE	EVTS	DOCUMENT ID	TECN
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0.632 ± 0.009 OUR FIT

0.632 ± 0.004 ± 0.008 110k BURKHARDT 87 NA31

$\Gamma(3\gamma)/\Gamma_{\text{total}}$

Γ_{10}/Γ

VALUE	CL%	DOCUMENT ID	TECN
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< 2.4 × 10⁻⁷ 90 ²² BARR 95C NA31

²² Assumes a phase-space decay distribution.

$\Gamma(\pi^0 2\gamma)/\Gamma_{\text{total}}$

Γ_{11}/Γ

VALUE (units 10^{-6})	CL%	EVTS	DOCUMENT ID	TECN	COMMENT
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1.68 ± 0.10 OUR AVERAGE

1.68 ± 0.07 ± 0.08 884 ALAVI-HARATI 99B KTEV

1.7 ± 0.2 ± 0.2 63 ²³ BARR 92 SPEC

• • • We do not use the following data for averages, fits, limits, etc. • • •

1.86 ± 0.60 ± 0.60	60	PAPADIMITR...91	E731	$m_{\gamma\gamma} > 280$ MeV
< 5.1	90	PAPADIMITR...91	E731	$m_{\gamma\gamma} < 264$ MeV
2.1 ± 0.6	14	²⁴ BARR	90C NA31	$m_{\gamma\gamma} > 280$ MeV
< 2.7	90	PAPADIMITR...89	E731	In PAPADI...91
< 230	90	0	BANNER	69 OSPK

²³ BARR 92 find that $\Gamma(\pi^0 2\gamma, m_{\gamma\gamma} < 240 \text{ MeV})/\Gamma(\pi^0 2\gamma) < 0.09$ (90% CL).

²⁴ BARR 90C superseded by BARR 92.

$\Gamma(\pi^0\pi^\pm e^\mp\nu)/\Gamma_{\text{total}}$

Γ_{12}/Γ

VALUE (units 10^{-5})	CL%	EVTS	DOCUMENT ID	TECN
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5.18 ± 0.29 OUR AVERAGE

5.16 ± 0.20 ± 0.22 729 MAKOFF 93 E731

6.2 ± 2.0 16 CARROLL 80C SPEC

• • • We do not use the following data for averages, fits, limits, etc. • • •

< 220 90 ²⁵ DONALDSON 74 SPEC

²⁵ DONALDSON 74 uses $K_L^0 \rightarrow \pi^+\pi^-\pi^0$ /(all K_L^0) decays = 0.126.

$\Gamma((\pi\mu\text{atom})\nu)/\Gamma(\pi^\pm\mu^\mp\nu_\mu)$

Γ_{13}/Γ_3

VALUE (units 10^{-7})	EVTS	DOCUMENT ID	TECN
3.90±0.39	155	²⁶ ARONSON	86 SPEC

• • • We do not use the following data for averages, fits, limits, etc. • • •

seen	18	COOMBES	76 WIRE
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²⁶ ARONSON 86 quote theoretical value of $(4.31 \pm 0.08) \times 10^{-7}$.

$\Gamma(\pi^\pm e^\mp\nu_e\gamma)/\Gamma(\pi^\pm e^\mp\nu_e)$

Γ_{14}/Γ_6

VALUE (units 10^{-2})	EVTS	DOCUMENT ID	TECN	COMMENT
0.934±0.036^{+0.055}_{-0.039}	1384	LEBER	96 NA31	$E_\gamma^* \geq 30$ MeV, $\theta_{e\gamma}^* \geq 20^\circ$

• • • We do not use the following data for averages, fits, limits, etc. • • •

3.3 ±2.0	10	PEACH	71 HLBC	γ KE >15 MeV
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$\Gamma(\pi^\pm\mu^\mp\nu_\mu\gamma)/\Gamma(\pi^\pm\mu^\mp\nu_\mu)$

Γ_{15}/Γ_3

VALUE (units 10^{-3})	EVTS	DOCUMENT ID	TECN	COMMENT
2.08±0.17^{+0.16}_{-0.21}	4261	BENDER	98 NA48	$E_\gamma^* \geq 30$ MeV

$\Gamma(\pi^+\pi^-\gamma)/\Gamma_{\text{total}}$

Γ_{16}/Γ

For earlier limits see our 1992 edition Physical Review **D45**, 1 June, Part II (1992).

VALUE (units 10^{-5})	EVTS	DOCUMENT ID	TECN	COMMENT
4.61±0.14 OUR AVERAGE				
4.66±0.15	3136	²⁷ RAMBERG	93 E731	$E_\gamma > 20$ MeV
4.41±0.32	1062	²⁸ CARROLL	80B SPEC	$E_\gamma > 20$ MeV

• • • We do not use the following data for averages, fits, limits, etc. • • •

1.52±0.16	516	²⁹ CARROLL	80B SPEC	$E_\gamma > 20$ MeV
2.89±0.28	546	³⁰ CARROLL	80B SPEC	
6.2 ±2.1	24	³¹ DONALDSON	74C SPEC	

²⁷ RAMBERG 93 finds that fraction of Direct Emission (DE) decays with $E_\gamma > 20$ MeV is 0.685 ± 0.041 .

²⁸ Both components. Uses $K_L^0 \rightarrow \pi^+\pi^-\pi^0$ /(all K_L^0) decays = 0.1239.

²⁹ Internal Bremsstrahlung component only.

³⁰ Direct γ emission component only.

³¹ Uses $K_L^0 \rightarrow \pi^+\pi^-\pi^0$ /(all K_L^0) decays = 0.126.

$\Gamma(\pi^0\pi^0\gamma)/\Gamma_{\text{total}}$

Γ_{17}/Γ

VALUE (units 10^{-6})	CL%	EVTS	DOCUMENT ID	TECN
< 5.6			BARR	94 NA31

• • • We do not use the following data for averages, fits, limits, etc. • • •

<230	90	0	ROBERTS	94 E799
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$\Gamma(\mu^+ \mu^- \gamma)/\Gamma_{\text{total}}$

Γ_{18}/Γ

VALUE (units 10^{-7}) CL% EVTS DOCUMENT ID TECN

3.25 ± 0.28 OUR AVERAGE

3.4 ± 0.6 ± 0.4 45 FANTI 97 NA48

3.23 ± 0.23 ± 0.19 197 SPENCER 95 E799

• • • We do not use the following data for averages, fits, limits, etc. • • •

2.8 ± 2.8 1 ³² CARROLL 80D SPEC

<78.1 90 ³³ DONALDSON 74 SPEC

³² Uses $K_L^0 \rightarrow \pi^+ \pi^- \pi^0$ / (all K_L^0) decays = 0.1239.

³³ Uses $K_L^0 \rightarrow \pi^+ \pi^- \pi^0$ / (all K_L^0) decays = 0.126.

$\Gamma(e^+ e^- \gamma)/\Gamma_{\text{total}}$

Γ_{19}/Γ

VALUE (units 10^{-6}) CL% EVTS DOCUMENT ID TECN

10.0 ± 0.5 OUR AVERAGE

Error includes scale factor of 1.5. See the ideogram below.

10.6 ± 0.2 ± 0.4 6864 ³⁴ FANTI 99B NA48

9.2 ± 0.5 ± 0.5 1053 BARR 90B NA31

9.1 ± 0.4 ^{+0.6}_{-0.5} 919 OHL 90B B845

• • • We do not use the following data for averages, fits, limits, etc. • • •

17.4 ± 8.7 4 ³⁵ CARROLL 80D SPEC

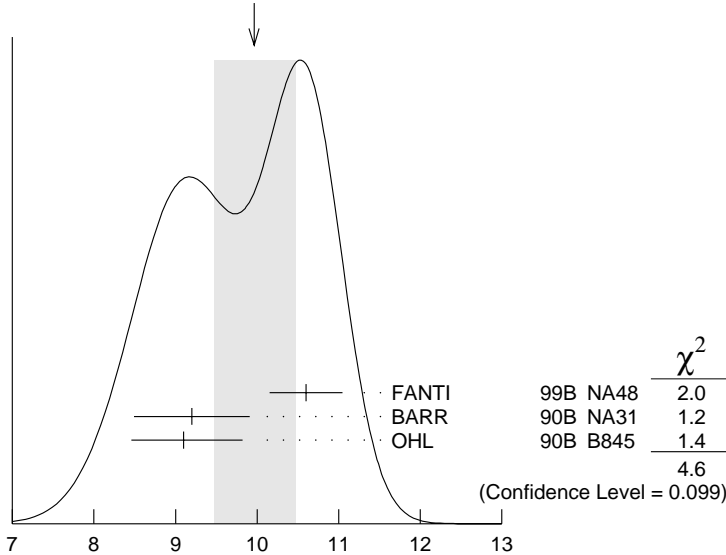
<27 90 0 ³⁶ BARMIN 72 HLBC

³⁴ For FANTI 99B, the ±0.4 systematic error includes for uncertainties in the calculation, primarily uncertainties in the $\pi^0 \rightarrow e^+ e^- \gamma$ and $K_L^0 \rightarrow \pi^0 \pi^0$ branching ratios, evaluated using our 1999 Web edition values.

³⁵ Uses $K_L^0 \rightarrow \pi^+ \pi^- \pi^0$ / (all K_L^0) decays = 0.1239.

³⁶ Uses $K_L^0 \rightarrow 3\pi^0$ / total = 0.214.

WEIGHTED AVERAGE
10.0 ± 0.5 (Error scaled by 1.5)



$\Gamma(e^+ e^- \gamma)/\Gamma_{\text{total}}$ (units 10^{-6})

$\Gamma(e^+ e^- \gamma \gamma) / \Gamma_{\text{total}}$					Γ_{20} / Γ
<u>VALUE (units 10^{-7})</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>	
6.9 ± 1.0 OUR AVERAGE					
$8.0 \pm 1.5^{+1.4}_{-1.2}$	40	SETZU	98 NA31	$E_\gamma > 5 \text{ MeV}$	
$6.5 \pm 1.2 \pm 0.6$	58	NAKAYA	94 E799	$E_\gamma > 5 \text{ MeV}$	
6.6 ± 3.2		MORSE	92 B845	$E_\gamma > 5 \text{ MeV}$	

$\Gamma(\pi^0 \gamma e^+ e^-) / \Gamma_{\text{total}}$			Γ_{21} / Γ	
<u>VALUE (units 10^{-7})</u>	<u>CL%</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>
<7.1	90	0	MURAKAMI	99 SPEC

$\Gamma(\pi^+ \pi^-) / \Gamma_{\text{total}}$		Γ_{22} / Γ
Violates CP conservation.		
<u>VALUE (units 10^{-3})</u>	<u>DOCUMENT ID</u>	
2.056 ± 0.033 OUR FIT		
2.07 ± 0.05 OUR AVERAGE		
2.071 ± 0.049	³⁷ ETAFIT	00

³⁷ This ETAFIT value is computed from fitted values of $|\eta_{+-}|$, the K_L^0 and K_S^0 lifetimes, and the $K_S^0 \rightarrow \pi^+ \pi^-$ branching fraction. See the discussion in the note "Fits for K_L^0 CP -Violation Parameters."

$\Gamma(\pi^+ \pi^-) / \Gamma(\pi^+ \pi^- \pi^0)$					Γ_{22} / Γ_2
Violates CP conservation.					
<u>VALUE (units 10^{-2})</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>	
1.637 ± 0.030 OUR FIT Error includes scale factor of 1.1.					
1.64 ± 0.04	4200	MESSNER	73 ASPK	$\eta_{+-} = 2.23$	

$\Gamma(\pi^+ \pi^-) / [\Gamma(\pi^\pm \mu^\mp \nu_\mu) + \Gamma(\pi^\pm e^\mp \nu_e)]$					$\Gamma_{22} / (\Gamma_3 + \Gamma_6)$
Violates CP conservation.					
<u>VALUE (units 10^{-3})</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>	
3.12 ± 0.05 OUR FIT Error includes scale factor of 1.1.					
3.08 ± 0.10 OUR AVERAGE					
3.13 ± 0.14	1687	COUPAL	85 SPEC	$\eta_{+-} = 2.28 \pm 0.06$	
3.04 ± 0.14	2703	DEVOE	77 SPEC	$\eta_{+-} = 2.25 \pm 0.05$	

• • • We do not use the following data for averages, fits, limits, etc. • • •

2.51 ± 0.23	309	³⁸ DEBOUARD	67 OSPK	$\eta_{+-} = 2.00 \pm 0.09$
2.35 ± 0.19	525	³⁸ FITCH	67 OSPK	$\eta_{+-} = 1.94 \pm 0.08$

³⁸ Old experiments excluded from fit. See subsection on η_{+-} in section on "PARAMETERS FOR $K_L^0 \rightarrow 2\pi$ DECAY" below for average η_{+-} of these experiments and for note on discrepancy.

$\Gamma(\pi^+\pi^-)/[\Gamma(\pi^+\pi^-\pi^0) + \Gamma(\pi^\pm\mu^\mp\nu_\mu) + \Gamma(\pi^\pm e^\mp\nu_e)]$ $\Gamma_{22}/(\Gamma_2+\Gamma_3+\Gamma_6)$

Violates CP conservation.

VALUE (units 10^{-3})	EVTS	DOCUMENT ID	TECN	COMMENT
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2.62 ± 0.04 OUR FIT

• • • We do not use the following data for averages, fits, limits, etc. • • •

2.60 ± 0.07	4200	³⁹ MESSNER	73 ASPK	$\eta_{+-} = 2.23 \pm 0.05$
1.93 ± 0.26		⁴⁰ BASILE	66 OSPK	$\eta_{+-} = 1.92 \pm 0.13$
1.993 ± 0.080		⁴⁰ BOTT-...	66 OSPK	$\eta_{+-} = 1.95 \pm 0.04$
2.08 ± 0.35	54	⁴⁰ GALBRAITH	65 OSPK	$\eta_{+-} = 1.99 \pm 0.16$
2.0 ± 0.4	45	⁴⁰ CHRISTENS...	64 OSPK	$\eta_{+-} = 1.95 \pm 0.20$

³⁹ From same data as $\Gamma(\pi^+\pi^-)/\Gamma(\pi^+\pi^-\pi^0)$ MESSNER 73, but with different normalization.

⁴⁰ Old experiments excluded from fit. See subsection on η_{+-} in section on "PARAMETERS FOR $K_L^0 \rightarrow 2\pi$ DECAY" below for average η_{+-} .

$\Gamma(\pi^0\pi^0)/\Gamma_{total}$ Γ_{23}/Γ

Violates CP conservation.

VALUE (units 10^{-3})	EVTS	DOCUMENT ID	TECN	COMMENT
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0.927 ± 0.019 OUR FIT

• • • We do not use the following data for averages, fits, limits, etc. • • •

2.5 ± 0.8	189	⁴¹ GAILLARD	69 OSPK	$\eta_{00} = 3.6 \pm 0.6$
1.2 ^{+1.5} _{-1.2}	7	⁴² CRIEGEE	66 OSPK	

⁴¹ Latest result of this experiment given by FAISSNER 70 $\Gamma(\pi^0\pi^0)/\Gamma(3\pi^0)$.

⁴² CRIEGEE 66 experiment not designed to measure $2\pi^0$ decay mode.

$\Gamma(\pi^0\pi^0)/\Gamma(3\pi^0)$ Γ_{23}/Γ_1

Violates CP conservation.

VALUE (units 10^{-2})	EVTS	DOCUMENT ID	TECN	COMMENT
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0.439 ± 0.011 OUR FIT Error includes scale factor of 1.1.

0.39 ± 0.06 OUR AVERAGE

0.37 ± 0.08	29	BARMIN	70 HLBC	$\eta_{00} = 2.02 \pm 0.23$
0.32 ± 0.15	30	BUDAGOV	70 HLBC	$\eta_{00} = 1.9 \pm 0.5$
0.46 ± 0.11	57	BANNER	69 OSPK	$\eta_{00} = 2.2 \pm 0.3$
not seen		BARTLETT	68 OSPK	See η_{00} below

• • • We do not use the following data for averages, fits, limits, etc. • • •

1.21 ± 0.30	150	⁴³ REY	76 OSPK	$\eta_{00} = 3.8 \pm 0.5$
0.90 ± 0.30	172	⁴⁴ FAISSNER	70 OSPK	$\eta_{00} = 3.2 \pm 0.5$
1.31 ± 0.31	133	⁴³ CENCE	69 OSPK	$\eta_{00} = 3.7 \pm 0.5$
1.89 ± 0.31	109	⁴⁵ CRONIN	67 OSPK	$\eta_{00} = 4.9 \pm 0.5$
1.36 ± 0.18		⁴⁵ CRONIN	67B OSPK	$\eta_{00} = 3.92 \pm 0.3$

⁴³ CENCE 69 events are included in REY 76.

⁴⁴ FAISSNER 70 contains same $2\pi^0$ events as GAILLARD 69 $\Gamma(\pi^0\pi^0)/\Gamma_{total}$.

⁴⁵ CRONIN 67B is further analysis of CRONIN 67, now both withdrawn.

$$\Gamma(\pi^0 \pi^0) / \Gamma(\pi^+ \pi^-)$$

$\Gamma_{23} / \Gamma_{22}$

Violates CP conservation.

VALUE	DOCUMENT ID
0.451 ± 0.006 OUR FIT	
0.452 ± 0.006 OUR AVERAGE	
0.4517 ± 0.0060	⁴⁶ ETAFIT 00

⁴⁶ This ETAFIT value is computed from fitted values of $|\eta_{00} / \eta_{+-}|$ and the $\Gamma(K_S^0 \rightarrow \pi^+ \pi^-) / \Gamma(K_S^0 \rightarrow \pi^0 \pi^0)$ branching fraction. See the discussion in the note "Fits for K_L^0 CP-Violation Parameters."

$$\Gamma(\mu^+ \mu^-) / [\Gamma(\pi^+ \pi^- \pi^0) + \Gamma(\pi^\pm \mu^\mp \nu_\mu) + \Gamma(\pi^\pm e^\mp \nu_e)] \quad \Gamma_{24} / (\Gamma_2 + \Gamma_3 + \Gamma_6)$$

Test for $\Delta S = 1$ weak neutral current. Allowed by higher-order electroweak interaction.

VALUE (units 10^{-6})	CL%	DOCUMENT ID	TECN
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• • • We do not use the following data for averages, fits, limits, etc. • • •

< 2.0	90	BOTT-...	67 OSPK
< 35.0	90	FITCH	67 OSPK
< 250.0	90	ALFF-...	66B OSPK
< 100.0		ANIKINA	65 CC

$$\Gamma(\mu^+ \mu^-) / \Gamma(\pi^+ \pi^-)$$

$\Gamma_{24} / \Gamma_{22}$

Test for $\Delta S = 1$ weak neutral current. Allowed by higher-order electroweak interaction.

VALUE (units 10^{-6})	CL%	EVTS	DOCUMENT ID	TECN	COMMENT
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3.48 ± 0.05 OUR AVERAGE

3.474 ± 0.057	6210		AMBROSE	00 B871	
3.87 ± 0.30	179	⁴⁷	AKAGI	95 SPEC	
3.38 ± 0.17	707		HEINSON	95 B791	

• • • We do not use the following data for averages, fits, limits, etc. • • •

3.9 ± 0.3 ± 0.1	178	⁴⁸	AKAGI	91B SPEC	In AKAGI 95
3.45 ± 0.18 ± 0.13	368	⁴⁹	HEINSON	91 SPEC	In HEINSON 95
4.1 ± 0.5	54		INAGAKI	89 SPEC	In AKAGI 91B
2.8 ± 0.3 ± 0.2	87		MATHIAZHA...	89B SPEC	In HEINSON 91
4.0 ^{+1.4} _{-0.9}	15		SHOCHET	79 SPEC	
4.2 ^{+5.1} _{-2.6}	3	⁵⁰	FUKUSHIMA	76 SPEC	
5.8 ^{+2.3} _{-1.5}	9	⁵¹	CARITHERS	73 SPEC	
< 1.53	90	0	⁵² CLARK	71 SPEC	
< 18.	90	0	DARRIULAT	70 SPEC	
< 140.	90	0	FOETH	69 SPEC	

⁴⁷ AKAGI 95 gives this number multiplied by the PDG 1992 average for $\Gamma(K_L^0 \rightarrow \pi^+ \pi^-) / \Gamma(\text{total})$.

⁴⁸ AKAGI 91B give this number multiplied by the 1990 PDG average for $\Gamma(K_L^0 \rightarrow \pi^+ \pi^-) / \Gamma(\text{total})$.

⁴⁹ HEINSON 91 give $\Gamma(K_L^0 \rightarrow \mu\mu) / \Gamma_{\text{total}}$. We divide out the $\Gamma(K_L^0 \rightarrow \pi^+ \pi^-) / \Gamma_{\text{total}}$ PDG average which they used.

⁵⁰ FUKUSHIMA 76 errors are at CL = 90%.

⁵¹ CARITHERS 73 errors are at CL = 68%, W.Carithers, (private communication 79).

⁵² CLARK 71 limit raised from 1.2×10^{-6} by FIELD 74 reanalysis. Not in agreement with subsequent experiments. So not averaged.

$\Gamma(e^+ e^-)/\Gamma_{\text{total}}$ Γ_{25}/Γ

Test for $\Delta S = 1$ weak neutral current. Allowed by higher-order electroweak interaction.

VALUE (units 10^{-10})	CL%	EVTS	DOCUMENT ID	TECN	COMMENT
$0.087^{+0.057}_{-0.041}$		4	AMBROSE	98 B871	

• • • We do not use the following data for averages, fits, limits, etc. • • •

< 1.6	90	1	AKAGI	95 SPEC	
< 0.41	90	0	⁵³ ARISAKA	93B B791	
< 1.6	90	1	AKAGI	91 SPEC	Sup. by AKAGI 95
< 5.6	90		INAGAKI	89 SPEC	In AKAGI 91
< 3.2	90		MATHIAZHA...	89 SPEC	In ARISAKA 93B
< 110	90		COUSINS	88 SPEC	
< 45	90		GREENLEE	88 SPEC	Repl. by JAS-TRZEMBSKI 88
< 12	90		JASTRZEM...	88 SPEC	
< 15.7	90		⁵⁴ CLARK	71 ASPK	
< 1500	90	0	FOETH	69 ASPK	

⁵³ ARISAKA 93B includes all events with <6 MeV radiated energy.

⁵⁴ Possible (but unknown) systematic errors. See note on CLARK 71 $\Gamma(\mu^+ \mu^-)/\Gamma(\pi^+ \pi^-)$ entry.

$\Gamma(e^+ e^-)/[\Gamma(\pi^+ \pi^- \pi^0) + \Gamma(\pi^\pm \mu^\mp \nu_\mu) + \Gamma(\pi^\pm e^\mp \nu_e)]$ $\Gamma_{25}/(\Gamma_2 + \Gamma_3 + \Gamma_6)$

Test for $\Delta S = 1$ weak neutral current. Allowed by higher-order electroweak interaction.

VALUE (units 10^{-6})	CL%	DOCUMENT ID	TECN
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• • • We do not use the following data for averages, fits, limits, etc. • • •

< 23.0	90	BOTT-...	67 OSPK
< 200.0	90	ALFF-...	66B OSPK
< 1000.0		ANIKINA	65 CC

$\Gamma(\pi^+ \pi^- e^+ e^-)/\Gamma_{\text{total}}$ Γ_{26}/Γ

Test for $\Delta S = 1$ weak neutral current. Allowed by higher-order electroweak interaction.

VALUE (units 10^{-7})	CL%	EVTS	DOCUMENT ID	TECN	COMMENT
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3.5 ± 0.6 OUR AVERAGE

$3.2 \pm 0.6 \pm 0.4$		37	ADAMS	98 KTEV
$4.4 \pm 1.3 \pm 0.5$		13	TAKEUCHI	98 SPEC

• • • We do not use the following data for averages, fits, limits, etc. • • •

< 4.6	90		NOMURA	97 SPEC	$m_{ee} > 4$ MeV
< 25	90	0	BALATS	83 SPEC	
< 88.1	90		⁵⁵ DONALDSON	76 SPEC	
< 300			ANIKINA	73 STRC	

⁵⁵ Uses $K_L^0 \rightarrow \pi^+ \pi^- \pi^0$ / (all K_L^0) decays = 0.126.

$\Gamma(\mu^+ \mu^- e^+ e^-)/\Gamma_{\text{total}}$ Γ_{27}/Γ

Test for $\Delta S = 1$ weak neutral current. Allowed by higher-order electroweak interaction.

VALUE (units 10^{-9})	CL%	EVTS	DOCUMENT ID	TECN
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$2.9^{+6.7}_{-2.4}$ 1 GU 96 E799

• • • We do not use the following data for averages, fits, limits, etc. • • •

< 4900	90		BALATS	83 SPEC
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$\Gamma(e^+ e^- e^+ e^-)/\Gamma_{\text{total}}$ Γ_{28}/Γ

Test for $\Delta S = 1$ weak neutral current. Allowed by higher-order electroweak interaction.

VALUE (units 10^{-8})	CL%	EVTS	DOCUMENT ID	TECN	COMMENT
4.1 ± 0.8 OUR AVERAGE			Error includes scale factor of 1.2.		
6 ± 2 ± 1		18	⁵⁶ AKAGI	95 SPEC	$m_{ee} > 470$ MeV
10.4 ± 3.7 ± 1.1		8	⁵⁷ BARR	95 NA31	
3.96 ± 0.78 ± 0.32		27	GU	94 E799	
3.07 ± 1.25 ± 0.26		6	VAGINS	93 B845	

• • • We do not use the following data for averages, fits, limits, etc. • • •

7 ± 3 ± 2		6	⁵⁶ AKAGI	95 SPEC	$m_{ee} > 470$ MeV
6 ± 2 ± 1		18	AKAGI	93 CNTR	Sup. by AKAGI 95
4 ± 3		2	BARR	91 NA31	Sup. by BARR 95
< 260	90		BALATS	83 SPEC	

⁵⁶ Values are for the total branching fraction, acceptance-corrected for the m_{ee} cuts shown.

⁵⁷ Distribution of angles between two $e^+ e^-$ pair planes favors $CP = -1$ for K_L^0 .

$\Gamma(\pi^0 \mu^+ \mu^-)/\Gamma_{\text{total}}$ Γ_{29}/Γ

Violates CP in leading order. Test for $\Delta S = 1$ weak neutral current. Allowed by higher-order electroweak interaction.

VALUE (units 10^{-9})	CL%	EVTS	DOCUMENT ID	TECN
< 5.1	90	0	HARRIS	93 E799

• • • We do not use the following data for averages, fits, limits, etc. • • •

< 1200	90	0	⁵⁸ CARROLL	80D SPEC
< 56600	90		⁵⁹ DONALDSON	74 SPEC

⁵⁸ Uses $K_L^0 \rightarrow \pi^+ \pi^- \pi^0 / (\text{all } K_L^0)$ decays = 0.1239.

⁵⁹ Uses $K_L^0 \rightarrow \pi^+ \pi^- \pi^0 / (\text{all } K_L^0)$ decays = 0.126.

$\Gamma(\pi^0 e^+ e^-)/\Gamma_{\text{total}}$ Γ_{30}/Γ

Violates CP in leading order. Direct and indirect CP -violating contributions are expected to be comparable and to dominate the CP -conserving part. Test for $\Delta S = 1$ weak neutral current. Allowed by higher-order electroweak interaction.

VALUE (units 10^{-9})	CL%	EVTS	DOCUMENT ID	TECN
< 4.3	90	0	HARRIS	93B E799
< 7.5	90	0	BARKER	90 E731
< 5.5	90	0	OHL	90 B845

• • • We do not use the following data for averages, fits, limits, etc. • • •

< 40	90		BARR	88 NA31
< 320	90		JASTRZEM...	88 SPEC
< 2300	90	0	⁶⁰ CARROLL	80D SPEC

⁶⁰ Uses $K_L^0 \rightarrow \pi^+ \pi^- \pi^0 / (\text{all } K_L^0)$ decays = 0.1239.

$\Gamma(\pi^0 \nu \bar{\nu})/\Gamma_{\text{total}}$ Γ_{31}/Γ

Violates CP in leading order. Test of direct CP violation since the indirect CP -violating and CP -conserving contributions are expected to be suppressed. Test of $\Delta S = 1$ weak neutral current.

VALUE (units 10^{-5})	CL%	EVTS	DOCUMENT ID	TECN
< 0.059 (CL = 90%)				
< 0.059	90	0	ALAVI-HARATI00	KTEV

• • • We do not use the following data for averages, fits, limits, etc. • • •

< 0.16	90	0	ADAMS	99	KTEV
< 5.8	90	0	WEAVER	94	E799
< 22	90	0	GRAHAM	92	CNTR
<760	90		⁶¹ LITTENBERG	89	RVUE

⁶¹LITTENBERG 89 is from retroactive data analysis of CRONIN 67.

$\Gamma(e^\pm \mu^\mp)/\Gamma_{\text{total}}$

Γ_{32}/Γ

Test of lepton family number conservation.

VALUE (units 10^{-11})	CL%	EVTS	DOCUMENT ID	TECN	COMMENT
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< **0.47 (CL = 90%)**

< 0.47	90		AMBROSE	98B	B871
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• • • We do not use the following data for averages, fits, limits, etc. • • •

< 9.4	90	0	AKAGI	95	SPEC
< 3.9	90	0	ARISAKA	93	B791
< 3.3	90	0	⁶² ARISAKA	93	B791
< 9.4	90	0	AKAGI	91	SPEC Sup. by AKAGI 95
< 43	90		INAGAKI	89	SPEC In AKAGI 91
< 22	90		MATHIAZHA...	89	SPEC
< 190	90		SCHAFFNER	89	SPEC
<1100	90		COUSINS	88	SPEC
< 670	90		GREENLEE	88	SPEC Repl. by SCHAFFNER 89
< 157	90		⁶³ CLARK	71	ASPK

⁶²This is the combined result of ARISAKA 93 and MATHIAZHAGAN 89.

⁶³Possible (but unknown) systematic errors. See note on CLARK 71 $\Gamma(\mu^+ \mu^-)/\Gamma(\pi^+ \pi^-)$ entry.

$\Gamma(e^\pm e^\pm \mu^\mp \mu^\mp)/\Gamma_{\text{total}}$

Γ_{33}/Γ

Test of lepton family number conservation.

VALUE (units 10^{-9})	CL%	EVTS	DOCUMENT ID	TECN
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< 6.1	90	0	⁶⁴ GU	96	E799
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⁶⁴Assuming uniform phase space distribution.

$\Gamma(e^\pm \mu^\mp)/[\Gamma(\pi^+ \pi^- \pi^0) + \Gamma(\pi^\pm \mu^\mp \nu_\mu) + \Gamma(\pi^\pm e^\mp \nu_e)]$

$\Gamma_{32}/(\Gamma_2 + \Gamma_3 + \Gamma_6)$

Test of lepton family number conservation.

VALUE (units 10^{-4})	CL%	DOCUMENT ID	TECN
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• • • We do not use the following data for averages, fits, limits, etc. • • •

< 0.1	90	BOTT-...	67	OSPK
< 0.08	90	FITCH	67	OSPK
< 1.0	90	CARPENTER	66	OSPK
<10.0		ANIKINA	65	CC

$\Gamma(\pi^0 \mu^\pm e^\mp)/\Gamma_{\text{total}}$

Γ_{34}/Γ

Test of lepton family number conservation.

VALUE	CL%	DOCUMENT ID	TECN
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< 6.2×10^{-9}	90	ARISAKA	98	E799
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ENERGY DEPENDENCE OF K_L^0 DALITZ PLOT

For discussion, see note on Dalitz plot parameters in the K^\pm section of the Particle Listings above. For definitions of a_v , a_t , a_u , and a_y , see the earlier version of the same note in the 1982 edition of this *Review* published in Physics Letters **111B** 70 (1982).

$$|\text{matrix element}|^2 = 1 + gu + hu^2 + jv + kv^2 + fuv$$

where $u = (s_3 - s_0) / m_\pi^2$ and $v = (s_1 - s_2) / m_\pi^2$

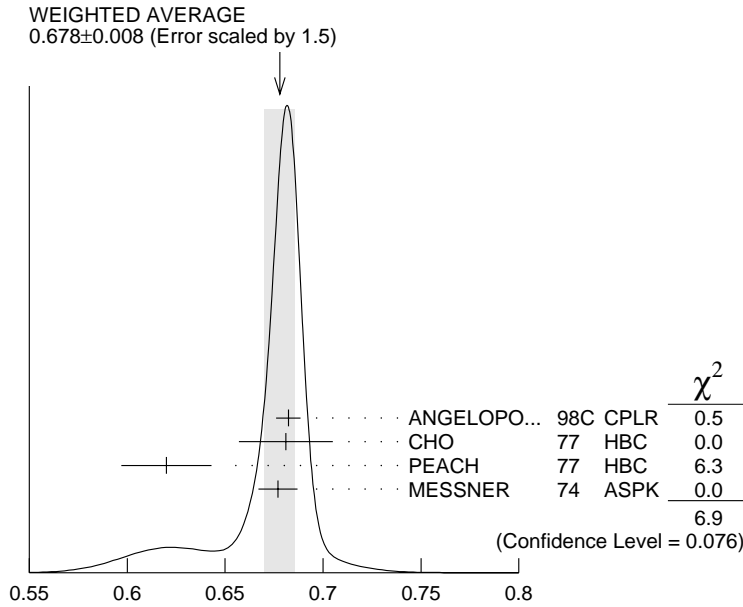
LINEAR COEFFICIENT g FOR $K_L^0 \rightarrow \pi^+ \pi^- \pi^0$

VALUE	EVTs	DOCUMENT ID	TECN	COMMENT
0.678 ± 0.008	OUR AVERAGE	Error includes scale factor of 1.5. See the ideogram below.		
0.6823 ± 0.0044 ± 0.0044	500k	ANGELOPO...	98C	CPLR
0.681 ± 0.024	6499	CHO	77	HBC
0.620 ± 0.023	4709	PEACH	77	HBC
0.677 ± 0.010	509k	MESSNER	74	ASPK $a_y = -0.917 \pm 0.013$
• • • We do not use the following data for averages, fits, limits, etc. • • •				
0.69 ± 0.07	192	⁶⁵ BALDO-...	75	HLBC
0.590 ± 0.022	56k	⁶⁵ BUCHANAN	75	SPEC $a_u = -0.277 \pm 0.010$
0.619 ± 0.027	20k	^{65,66} BISI	74	ASPK $a_t = -0.282 \pm 0.011$
0.612 ± 0.032		⁶⁵ ALEXANDER	73B	HBC
0.73 ± 0.04	3200	⁶⁵ BRANDENB...	73	HBC
0.50 ± 0.11	180	⁶⁵ JAMES	72	HBC
0.608 ± 0.043	1486	⁶⁵ KRENZ	72	HLBC $a_t = -0.277 \pm 0.018$
0.688 ± 0.074	384	⁶⁵ METCALF	72	ASPK $a_t = -0.31 \pm 0.03$
0.650 ± 0.012	29k	⁶⁵ ALBROW	70	ASPK $a_y = -0.858 \pm 0.015$
0.593 ± 0.022	36k	^{65,67} BUCHANAN	70	SPEC $a_u = -0.278 \pm 0.010$
0.664 ± 0.056	4400	⁶⁵ SMITH	70	OSPK $a_t = -0.306 \pm 0.024$
0.400 ± 0.045	2446	⁶⁵ BASILE	68B	OSPK $a_t = -0.188 \pm 0.020$
0.649 ± 0.044	1350	⁶⁵ HOPKINS	67	HBC $a_t = -0.294 \pm 0.018$
0.428 ± 0.055	1198	⁶⁵ NEFKENS	67	OSPK $a_u = -0.204 \pm 0.025$
0.64 ± 0.17	280	⁶⁵ ANIKINA	66	CC $a_v = -8.2^{+0.9}_{-1.3}$
0.70 ± 0.12	126	⁶⁵ HAWKINS	66	HBC $a_v = -8.6 \pm 0.7$
0.32 ± 0.13	66	⁶⁵ ASTBURY	65	CC $a_v = -5.5 \pm 1.5$
0.51 ± 0.09	310	⁶⁵ ASTBURY	65B	CC $a_v = -7.3^{+0.6}_{-0.8}$
0.55 ± 0.23	79	⁶⁵ ADAIR	64	HBC $a_v = -7.6 \pm 1.7$
0.51 ± 0.20	77	⁶⁵ LUERS	64	HBC $a_v = -7.3 \pm 1.6$

⁶⁵ Quadratic dependence required by some experiments. (See sections on "QUADRATIC COEFFICIENT h " and "QUADRATIC COEFFICIENT k " below.) Correlations prevent us from averaging results of fits not including g , h , and k terms.

⁶⁶ BISI 74 value comes from quadratic fit with quad. term consistent with zero. g error is thus larger than if linear fit were used.

⁶⁷ BUCHANAN 70 result revised by BUCHANAN 75 to include radiative correlations and to use more reliable K_L^0 momentum spectrum of second experiment (had same beam).



Linear coeff. g for $K_L^0 \rightarrow \pi^+ \pi^- \pi^0$ matrix element squared

QUADRATIC COEFFICIENT h FOR $K_L^0 \rightarrow \pi^+ \pi^- \pi^0$

VALUE	EVTS	DOCUMENT ID	TECN
0.076 ± 0.006 OUR AVERAGE			
$0.061 \pm 0.004 \pm 0.015$	500k	ANGELOPO... 98C CPLR	
0.095 ± 0.032	6499	CHO 77 HBC	
0.048 ± 0.036	4709	PEACH 77 HBC	
0.079 ± 0.007	509k	MESSNER 74 ASPK	

• • • We do not use the following data for averages, fits, limits, etc. • • •

-0.011 ± 0.018	29k	⁶⁸ ALBROW 70 ASPK	
0.043 ± 0.052	4400	⁶⁸ SMITH 70 OSPK	

See notes in section "LINEAR COEFFICIENT g FOR $K_L^0 \rightarrow \pi^+ \pi^- \pi^0$ | MATRIX ELEMENT|²" above.

⁶⁸Quadratic coefficients h and k required by some experiments. (See section on "QUADRATIC COEFFICIENT k " below.) Correlations prevent us from averaging results of fits not including g , h , and k terms.

QUADRATIC COEFFICIENT k FOR $K_L^0 \rightarrow \pi^+ \pi^- \pi^0$

VALUE	EVTS	DOCUMENT ID	TECN
0.0099 ± 0.0015 OUR AVERAGE			
$0.0104 \pm 0.0017 \pm 0.0024$	500k	ANGELOPO... 98C CPLR	
0.024 ± 0.010	6499	CHO 77 HBC	
-0.008 ± 0.012	4709	PEACH 77 HBC	
0.0097 ± 0.0018	509k	MESSNER 74 ASPK	

LINEAR COEFFICIENT j FOR $K_L^0 \rightarrow \pi^+ \pi^- \pi^0$ (CP-VIOLATING TERM)

Listed in CP-violation section below.

QUADRATIC COEFFICIENT f FOR $K_L^0 \rightarrow \pi^+ \pi^- \pi^0$ (CP-VIOLATING TERM)

Listed in CP-violation section below.

QUADRATIC COEFFICIENT h FOR $K_L^0 \rightarrow \pi^0 \pi^0 \pi^0$

<u>VALUE (units 10^{-3})</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>
$-3.3 \pm 1.1 \pm 0.7$	5M	⁶⁹ SOMALWAR	92 E731

⁶⁹SOMALWAR 92 chose m_{π^+} as normalization to make it compatible with the Particle Data Group $K_L^0 \rightarrow \pi^+ \pi^- \pi^0$ definitions.

K_L^0 FORM FACTORS

For discussion, see note on form factors in the K^\pm section of the Particle Listings above.

In the form factor comments, the following symbols are used.

f_+ and f_- are form factors for the vector matrix element.

f_S and f_T refer to the scalar and tensor term.

$f_0 = f_+ + f_- t / (m_K^2 - m_\pi^2)$.

λ_+ , λ_- , and λ_0 are the linear expansion coefficients of f_+ , f_- , and f_0 .

λ_+ refers to the $K_{\mu 3}^0$ value except in the $K_{e 3}^0$ sections.

$d\xi(0)/d\lambda_+$ is the correlation between $\xi(0)$ and λ_+ in $K_{\mu 3}^0$.

$d\lambda_0/d\lambda_+$ is the correlation between λ_0 and λ_+ in $K_{\mu 3}^0$.

t = momentum transfer to the π in units of m_π^2 .

DP = Dalitz plot analysis.

PI = π spectrum analysis.

MU = μ spectrum analysis.

POL = μ polarization analysis.

BR = $K_{\mu 3}^0 / K_{e 3}^0$ branching ratio analysis.

E = positron or electron spectrum analysis.

RC = radiative corrections.

λ_+ (LINEAR ENERGY DEPENDENCE OF f_+ IN $K_{e 3}^0$ DECAY)

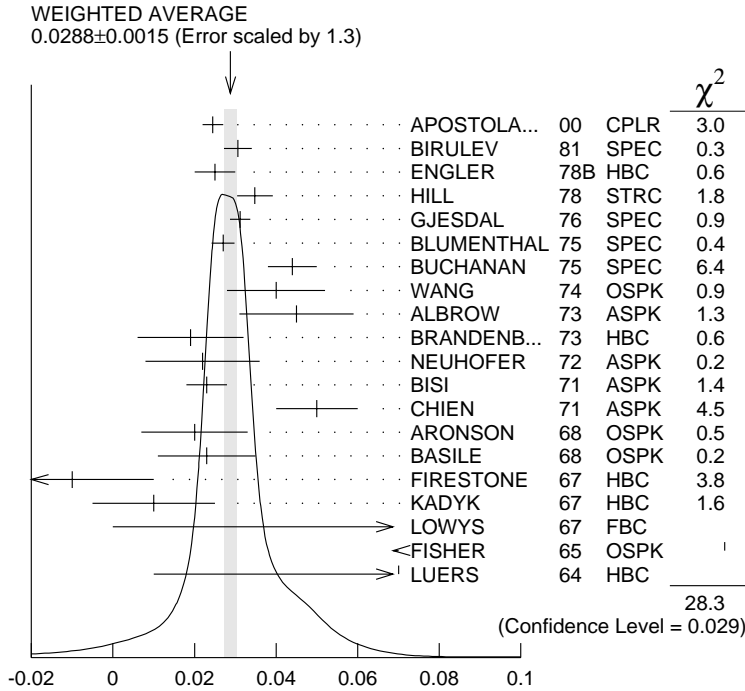
For radiative correction of $K_{e 3}^0$ DP, see GINSBERG 67 and BECHERRAWY 70.

<u>VALUE</u>	<u>EVTs</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
0.0288 ± 0.0015 OUR AVERAGE		Error includes scale factor of 1.3. See the ideogram below.		
0.0245 ± 0.0012 ± 0.0022	366k	APOSTOLA...	00 CPLR	DP
0.0306 ± 0.0034	74k	BIRULEV	81 SPEC	DP
0.025 ± 0.005	12k	⁷⁰ ENGLER	78B HBC	DP
0.0348 ± 0.0044	18k	HILL	78 STRC	DP
0.0312 ± 0.0025	500k	GJESDAL	76 SPEC	DP
0.0270 ± 0.0028	25k	BLUMENTHAL	75 SPEC	DP
0.044 ± 0.006	24k	BUCHANAN	75 SPEC	DP
0.040 ± 0.012	2171	WANG	74 OSPK	DP
0.045 ± 0.014	5600	ALBROW	73 ASPK	DP
0.019 ± 0.013	1871	BRANDENB...	73 HBC	PI transv.
0.022 ± 0.014	1910	NEUHOFER	72 ASPK	PI
0.023 ± 0.005	42k	BISI	71 ASPK	DP
0.05 ± 0.01	16k	CHIEN	71 ASPK	DP, no RC
0.02 ± 0.013	1000	ARONSON	68 OSPK	PI
+0.023 ± 0.012	4800	BASILE	68 OSPK	DP, no RC
-0.01 ± 0.02	762	FIRESTONE	67 HBC	DP, no RC
+0.01 ± 0.015	531	KADYK	67 HBC	e,PI, no RC
+0.08 ^{+0.10} _{-0.08}	240	LOWYS	67 FBC	PI
+0.15 ± 0.08	577	FISHER	65 OSPK	DP, no RC
+0.07 ± 0.06	153	LUERS	64 HBC	DP, no RC

• • • We do not use the following data for averages, fits, limits, etc. • • •

0.029 ± 0.005 19k ⁷⁰CHO 80 HBC DP
 0.0286 ± 0.0049 26k BIRULEV 79 SPEC Repl. by BIRULEV 81
 0.032 ± 0.0042 48k BIRULEV 76 SPEC Repl. by BIRULEV 81

⁷⁰ENGLER 78B uses an unique K_{e3} subset of CHO 80 events and is less subject to systematic effects.



λ_+ (Linear energy dependence of f_+ , K_{e3} decay)

$\xi_a = f_-/f_+$ (determined from $K_{\mu 3}^0$ spectra)

The parameter ξ is redundant with λ_0 below and is not put into the Meson Summary Table.

VALUE	$d\xi(0)/d\lambda_+$	EVTs	DOCUMENT ID	TECN	COMMENT
-0.11±0.09 OUR EVALUATION			Error includes scale factor of 2.3. Correlation is $d\xi(0)/d\lambda_+ = -14$. From a fit discussed in note on $K_{\ell 3}$ form factors in 1982 edition, PL 111B (April 1982).		
-0.10±0.09	-12	150k	⁷¹ BIRULEV	81 SPEC	DP
+0.26±0.16	-13	14k	⁷² CHO	80 HBC	DP
+0.13±0.23	-20	16k	⁷² HILL	79 STRC	DP
-0.25±0.22	-5.9	32k	⁷³ BUCHANAN	75 SPEC	DP
-0.11±0.07	-17	1.6M	⁷⁴ DONALDSON	74B SPEC	DP
-1.00±0.45	-20	1385	⁷⁵ PEACH	73 HLBC	DP
-1.5 ±0.7	-28	9086	⁷⁶ ALBROW	72 ASPK	DP
+1.2 ±0.8	-18	1341	⁷⁷ CARPENTER	66 OSPK	DP
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●					
+0.50±0.61	unknown	16k	⁷⁸ DALLY	72 ASPK	DP
-3.9 ±0.4		3140	⁷⁹ BASILE	70 OSPK	DP, indep of λ_+
-0.68 ^{+0.12} _{-0.20}	-26	16k	⁷⁸ CHIEN	70 ASPK	DP

⁷¹ BIRULEV 81 error, $d\xi(0)/d\lambda_+$ calculated by us from λ_0, λ_+ . $d\lambda_0/d\lambda_+ = 0$ used.

⁷² HILL 79 and CHO 80 calculated by us from λ_0, λ_+ , and $d\lambda_0/d\lambda_+$.

⁷³ BUCHANAN 75 is calculated by us from λ_0, λ_+ and $d\lambda_0/d\lambda_+$ because their appendix A value -0.20 ± 22 assumes $\xi(t)$ constant, i.e. $\lambda_- = \lambda_+$.

⁷⁴ DONALDSON 74B gives $\xi = -0.11 \pm 0.02$ not including systematics. Above error and $d\xi(0)/d\lambda_+$ were calculated by us from λ_0 and λ_+ errors (which include systematics) and $d\lambda_0/d\lambda_+$.

⁷⁵ PEACH 73 gives $\xi(0) = -0.95 \pm 0.45$ for $\lambda_+ = \lambda_- = 0.025$. The above value is for $\lambda_- = 0$. K.Peach, private communication (1974).

⁷⁶ ALBROW 72 fit has λ_- free, gets $\lambda_- = -0.030 \pm 0.060$ or $\Lambda = +0.15^{+0.17}_{-0.11}$.

⁷⁷ CARPENTER 66 $\xi(0)$ is for $\lambda_+ = 0$. $d\xi(0)/d\lambda_+$ is from figure 9.

⁷⁸ CHIEN 70 errors are statistical only. $d\xi(0)/d\lambda_+$ from figure 4. DALLY 72 is a reanalysis of CHIEN 70. The DALLY 72 result is not compatible with assumption $\lambda_- = 0$ so not included in our fit. The nonzero λ_- value and the relatively large λ_+ value found by DALLY 72 come mainly from a single low t bin (figures 1,2). The (f_+, ξ) correlation was ignored. We estimate from figure 2 that fixing $\lambda_- = 0$ would give $\xi(0) = -1.4 \pm 0.3$ and would add 10 to χ^2 . $d\xi(0)/d\lambda_+$ is not given.

⁷⁹ BASILE 70 is incompatible with all other results. Authors suggest that efficiency estimates might be responsible.

$\xi_b = f_-/f_+$ (determined from $K_{\mu 3}^0/K_{e 3}^0$)

The $K_{\mu 3}^0/K_{e 3}^0$ branching ratio fixes a relationship between $\xi(0)$ and λ_+ . We quote the author's $\xi(0)$ and associated λ_+ but do not average because the λ_+ values differ. The fit result and scale factor given below are not obtained from these ξ_b values. Instead they are obtained directly from the authors $K_{\mu 3}^0/K_{e 3}^0$ branching ratio via the fitted $K_{\mu 3}^0/K_{e 3}^0$ ratio ($\Gamma(\pi^\pm \mu^\mp \nu_\mu)/\Gamma(\pi^\pm e^\mp \nu_e)$). The parameter ξ is redundant with λ_0 below and is not put into the Meson Summary Table.

VALUE	EVTS	DOCUMENT ID	TECN	COMMENT
-0.11 ± 0.09 OUR EVALUATION				Error includes scale factor of 2.3. Correlation is $d\xi(0)/d\lambda_+ = -14$. From a fit discussed in note on $K_{\ell 3}$ form factors in 1982 edition, PL 111B (April 1982).

• • • We do not use the following data for averages, fits, limits, etc. • • •

0.5 ± 0.4	6700	BRANDENB...	73	HBC	BR, $\lambda_+ = 0.019 \pm 0.013$
-0.08 ± 0.25	1309	⁸⁰ EVANS	73	HLBC	BR, $\lambda_+ = 0.02$
-0.5 ± 0.5	3548	BASILE	70	OSPK	BR, $\lambda_+ = 0.02$
+0.45 ± 0.28	569	BEILLIERE	69	HLBC	BR, $\lambda_+ = 0$
-0.22 ± 0.30	1309	⁸⁰ EVANS	69	HLBC	
+0.2 ^{+0.8} -1.2		KULYUKINA	68	CC	BR, $\lambda_+ = 0$
+1.1 ± 1.1	389	ADAIR	64	HBC	BR, $\lambda_+ = 0$
+0.66 ^{+0.9} -1.3		LUERS	64	HBC	BR, $\lambda_+ = 0$

⁸⁰EVANS 73 replaces EVANS 69.

$\xi_c = f_-/f_+$ (determined from μ polarization in $K_{\mu 3}^0$)

The μ polarization is a measure of $\xi(t)$. No assumptions on λ_{+-} necessary, t (weighted by sensitivity to $\xi(t)$) should be specified. In λ_+ , $\xi(0)$ parametrization this is $\xi(0)$ for $\lambda_+ = 0$. $d\xi/d\lambda = \xi t$. For radiative correction to μ polarization in $K_{\mu 3}^0$, see GINSBERG 73. The parameter ξ is redundant with λ_0 below and is not put into the Meson Summary Table.

VALUE	EVTS	DOCUMENT ID	TECN	COMMENT	
-0.11 ± 0.09 OUR EVALUATION				Error includes scale factor of 2.3. Correlation is $d\xi(0)/d\lambda_+ = -14$. From a fit discussed in note on $K_{\ell 3}$ form factors in 1982 edition, PL 111B (April 1982).	
+0.178 ± 0.105	207k	⁸¹ CLARK	77	SPEC	POL, $d\xi(0)/d\lambda_+ = +0.68$
-0.385 ± 0.105	2.2M	⁸² SANDWEISS	73	CNTR	POL, $d\xi(0)/d\lambda_+ = -6$
-1.81 ^{+0.50} -0.26		⁸³ LONGO	69	CNTR	POL, $t=3.3$

• • • We do not use the following data for averages, fits, limits, etc. • • •

-1.6 ± 0.5	638	⁸⁴ ABRAMS	68B	OSPK	Polarization
-1.2 ± 0.5	2608	⁸⁴ AUERBACH	66B	OSPK	Polarization

⁸¹CLARK 77 $t = +3.80$, $d\xi(0)/d\lambda_+ = \xi(t)t = 0.178 \times 3.80 = +0.68$.

⁸²SANDWEISS 73 is for $\lambda_+ = 0$ and $t = 0$.

⁸³LONGO 69 $t = 3.3$ calculated from $d\xi(0)/d\lambda_+ = -6.0$ (table 1) divided by $\xi = -1.81$.

⁸⁴ t value not given.

$\text{Im}(\xi)$ in $K_{\mu 3}^0$ DECAY (from transverse μ pol.)

Test of T reversal invariance.

<u>VALUE</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
-0.007 ± 0.026 OUR AVERAGE				
0.009 ± 0.030	12M	MORSE	80	CNTR Polarization
0.35 ± 0.30	207k	⁸⁵ CLARK	77	SPEC POL, $t=0$
-0.085 ± 0.064	2.2M	⁸⁶ SANDWEISS	73	CNTR POL, $t=0$
-0.02 ± 0.08		LONGO	69	CNTR POL, $t=3.3$
-0.2 ± 0.6		ABRAMS	68B	OSPK Polarization

• • • We do not use the following data for averages, fits, limits, etc. • • •

0.012 ± 0.026 SCHMIDT 79 CNTR Repl. by MORSE 80

⁸⁵ CLARK 77 value has additional $\xi(0)$ dependence $+0.21\text{Re}[\xi(0)]$.

⁸⁶ SANDWEISS 73 value corrected from value quoted in their paper due to new value of $\text{Re}(\xi)$. See footnote 4 of SCHMIDT 79.

λ_+ (LINEAR ENERGY DEPENDENCE OF f_+ IN $K_{\mu 3}^0$ DECAY)

See also the corresponding entries and notes in section " $\xi_A = f_-/f_+$ " above and section " λ_0 (LINEAR ENERGY DEPENDENCE OF f_0 IN $K_{\mu 3}^0$ DECAY)" below. For radiative correction of $K_{\mu 3}^0$ Dalitz plot see GINSBERG 70 and BECHERRAWY 70.

<u>VALUE</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
0.034 ± 0.005 OUR EVALUATION From a fit discussed in note on $K_{\ell 3}$ form factors in 1982 edition, PL 111B (April 1982).				
0.0427 ± 0.0044	150k	BIRULEV	81	SPEC DP
0.028 ± 0.010	14k	CHO	80	HBC DP
0.028 ± 0.011	16k	HILL	79	STRC DP
0.046 ± 0.030	32k	BUCHANAN	75	SPEC DP
0.030 ± 0.003	1.6M	DONALDSON	74B	SPEC DP
0.085 ± 0.015	9086	ALBROW	72	ASPK DP

• • • We do not use the following data for averages, fits, limits, etc. • • •

0.0337 ± 0.0033 129k DZHORD... 77 SPEC Repl. by BIRULEV 81

0.046 ± 0.008 82k ALBRECHT 74 WIRE Repl. by BIRULEV 81

0.11 ± 0.04 16k DALLY 72 ASPK DP

0.07 ± 0.02 16k CHIEN 70 ASPK Repl. by DALLY 72

λ_0 (LINEAR ENERGY DEPENDENCE OF f_0 IN $K_{\mu 3}^0$ DECAY)

Wherever possible, we have converted the above values of $\xi(0)$ into values of λ_0 using the associated λ_+^μ and $d\xi(0)/d\lambda_+$.

VALUE	$d\lambda_0/d\lambda_+$	EVTS	DOCUMENT ID	TECN	COMMENT
0.025 ± 0.006					OUR EVALUATION Error includes scale factor of 2.3. Correlation is $d\lambda_0/d\lambda_+ = -0.16$. From a fit discussed in note on $K_{\ell 3}$ form factors in 1982 edition, PL 111B (April 1982).
0.0341 ± 0.0067	unknown	150k	87 BIRULEV	81 SPEC	DP
+0.050 ± 0.008	-0.11	14k	CHO	80 HBC	DP
+0.039 ± 0.010	-0.67	16k	HILL	79 STRC	DP
+0.047 ± 0.009	1.06	207k	88 CLARK	77 SPEC	POL
+0.025 ± 0.019	+0.5	32k	89 BUCHANAN	75 SPEC	DP
+0.019 ± 0.004	-0.47	1.6M	90 DONALDSON	74B SPEC	DP
-0.060 ± 0.038	-0.71	1385	91 PEACH	73 HLBC	DP
-0.018 ± 0.009	+0.49	2.2M	88 SANDWEISS	73 CNTR	POL
-0.043 ± 0.052	-1.39	9086	92 ALBROW	72 ASPK	DP
-0.140 ^{+0.043} _{-0.022}	+0.49		88 LONGO	69 CNTR	POL
+0.08 ± 0.07	-0.54	1371	88 CARPENTER	66 OSPK	DP
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●					
0.041 ± 0.008		14k	93 CHO	80 HBC	BR, $\lambda_+ = 0.028$
+0.0485 ± 0.0076		47k	DZHORD...	77 SPEC	In BIRULEV 81
+0.024 ± 0.011		82k	ALBRECHT	74 WIRE	In BIRULEV 81
+0.06 ± 0.03		6700	94 BRANDENB...	73 HBC	BR, $\lambda_+ = 0.019 \pm 0.013$
-0.067 ± 0.227	unknown	16k	95 DALLY	72 ASPK	DP
-0.333 ± 0.034	+1.	3140	96 BASILE	70 OSPK	DP

⁸⁷ BIRULEV 81 gives $d\lambda_0/d\lambda_+ = -1.5$, giving an unreasonably narrow error ellipse which dominates all other results. We use $d\lambda_0/d\lambda_+ = 0$.

⁸⁸ λ_0 value is for $\lambda_+ = 0.03$ calculated by us from $\xi(0)$ and $d\xi(0)/d\lambda_+$.

⁸⁹ BUCHANAN 75 value is from their appendix A and uses only $K_{\mu 3}$ data. $d\lambda_0/d\lambda_+$ was obtained by private communication, C.Buchanan, 1976.

⁹⁰ DONALDSON 74B $d\lambda_0/d\lambda_+$ obtained from figure 18.

⁹¹ PEACH 73 assumes $\lambda_+ = 0.025$. Calculated by us from $\xi(0)$ and $d\xi(0)/d\lambda_+$.

⁹² ALBROW 72 λ_0 is calculated by us from ξ_A , λ_+ and $d\xi(0)/d\lambda_+$. They give $\lambda_0 = -0.043 \pm 0.039$ for $\lambda_- = 0$. We use our larger calculated error.

⁹³ CHO 80 BR result not independent of their Dalitz plot result.

⁹⁴ Fit for λ_0 does not include this value but instead includes the $K_{\mu 3}/K_{e 3}$ result from this experiment.

⁹⁵ DALLY 72 gives $f_0 = 1.20 \pm 0.35$, $\lambda_0 = -0.080 \pm 0.272$, $\lambda_0' = -0.006 \pm 0.045$, but with a different definition of λ_0 . Our quoted λ_0 is his λ_0/f_0 . We cannot calculate true λ_0 error without his (λ_0, f_0) correlations. See also note on DALLY 72 in section ξ_A .

⁹⁶ BASILE 70 λ_0 is for $\lambda_+ = 0$. Calculated by us from ξ_A with $d\xi(0)/d\lambda_+ = 0$. BASILE 70 is incompatible with all other results. Authors suggest that efficiency estimates might be responsible.

$|f_S/f_+|$ FOR K_{e3}^0 DECAY

Ratio of scalar to f_+ couplings.

<u>VALUE</u>	<u>CL%</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
<0.04	68	25k	BLUMENTHAL75	SPEC	
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●					
<0.095	95	18k	HILL	78	STRC
<0.07	68	48k	BIRULEV	76	SPEC See also BIRULEV 81
<0.19	95	5600	ALBROW	73	ASPK
<0.15	68		KULYUKINA	67	CC

$|f_T/f_+|$ FOR K_{e3}^0 DECAY

Ratio of tensor to f_+ couplings.

<u>VALUE</u>	<u>CL%</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
<0.23	68	25k	BLUMENTHAL75	SPEC	
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●					
<0.40	95	18k	HILL	78	STRC
<0.34	68	48k	BIRULEV	76	SPEC See also BIRULEV 81
<1.0	95	5600	ALBROW	73	ASPK
<1.0	68		KULYUKINA	67	CC

$|f_T/f_+|$ FOR $K_{\mu 3}^0$ DECAY

Ratio of tensor to f_+ couplings.

<u>VALUE</u>	<u>DOCUMENT ID</u>	<u>TECN</u>
0.12 ± 0.12	BIRULEV	81 SPEC

α_{K^*} DECAY FORM FACTOR FOR $K_L \rightarrow e^+ e^- \gamma$

α_{K^*} is the constant in the model of BERGSTROM 83 which measures the relative strength of the vector-vector transition $K_L \rightarrow K^* \gamma$ with $K^* \rightarrow \rho, \omega, \phi \rightarrow \gamma^*$ and the pseudoscalar-pseudoscalar transition $K_L \rightarrow \pi, \eta, \eta' \rightarrow \gamma \gamma^*$.

<u>VALUE</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>
-0.33 ± 0.05 OUR AVERAGE			
-0.36 ± 0.06 ± 0.02	6864	FANTI	99B NA48
-0.28 ± 0.13		BARR	90B NA31
-0.280 ^{+0.099} _{-0.090}		OHL	90B B845

DECAY FORM FACTORS FOR $K_L^0 \rightarrow \pi^\pm \pi^0 e^\mp \nu_e$

Given in MAKOFF 93.

FITS FOR K_L^0 CP-VIOLATION PARAMETERS

Revised April 2000 by T.G. Trippe (LBNL).

In recent years, K_L^0 CP-violation experiments have improved our knowledge of CP-violation parameters and their consistency with the

expectations of CPT invariance and unitarity. For definitions of K_L^0 CP -violation parameters and a brief discussion of the theory, see the article “ CP Violation” by L. Wolfenstein in Section 12 of this *Review*.

This note describes our two fits for the CP -violation parameters in $K_L^0 \rightarrow \pi^+\pi^-$ and $\pi^0\pi^0$ decay, one for the phases ϕ_{+-} and ϕ_{00} , and another for the amplitudes $|\eta_{+-}|$ and $|\eta_{00}|$.

Fit to ϕ_{+-} , ϕ_{00} , $\Delta\phi$, Δm , and τ_S data: We perform a joint fit to the data on ϕ_{+-} , ϕ_{00} , the phase difference $\Delta\phi = \phi_{00} - \phi_{+-}$, the $K_L^0 - K_S^0$ mass difference Δm , and the K_S^0 mean life τ_S , including the effects of correlations. Measurements of ϕ_{+-} and ϕ_{00} are highly correlated with Δm and τ_S . Some measurements of τ_S are correlated with Δm . The correlations are given in the footnotes of the ϕ_{+-} and ϕ_{00} sections of the K_L^0 Particle Listings and the τ_S section of the K_S^0 Particle listings. In editions of the Review prior to 1996, we adjusted the experimental values of ϕ_{+-} and ϕ_{00} to account for correlations with Δm and τ_S but did not include the effects of these correlations when evaluating Δm and τ_S . In 1996, we introduced a joint fit including these correlations. In this fit, the ϕ_{+-} measurements have a strong influence on the fitted value of Δm . This is because the CERN NA31 vacuum regeneration experiments (CAROSI 90 [1] and GEWENIGER 74B [2]), the Fermilab E773/E731 regenerator experiments (SCHWINGENHEUER 95 [3] and GIBBONS 93 [4]), and the CPLEAR $K^0 - \bar{K}^0$ asymmetry experiment (APOSTOLAKIS 99C [5]) have very different dependences of ϕ_{+-} on Δm , as can be seen from their diagonal bands in Fig. 1.

The region where the ϕ_{+-} bands from these experiments cross gives a powerful measurement of Δm which decreases the fitted Δm value relative to our pre-1996 average Δm and earlier measurements such as CULLEN 70 [6], GEWENIGER 74C [7], and GJESDAL 74 [8].

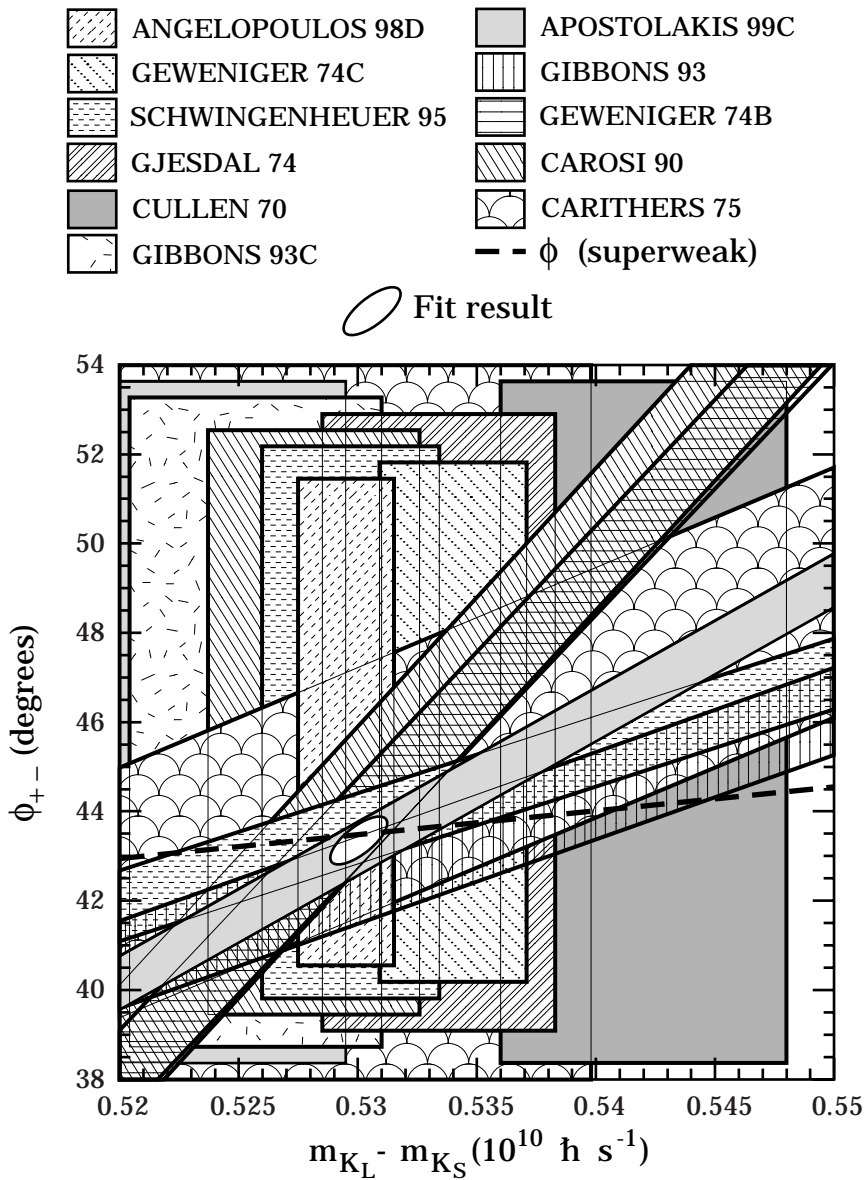


Figure 1: ϕ_{+-} vs Δm . Δm measurements appear as vertical bands spanning $\Delta m \pm 1\sigma$, some of which are cut near the top to aid the eye. The ϕ_{+-} measurements appear as diagonal bands spanning $\phi_{+-} \pm \sigma_\phi$. The dashed line shows $\phi(\text{superweak})$. The ellipse shows the 1σ contour of the fit result. See Table 1 for data references.

Table 1: References and location of input data for Fig. 1 and Fig. 2. Unless otherwise indicated by a footnote, a check (\checkmark) indicates that the data can be found in the ϕ_{+-} or Δm sections of the K_L Particle Listings, or the τ_S section of the K_S Particle Listings, according to the column headers.

Location of input data				PDG Document ID	Ref.
Fig. 1		Fig. 2			
ϕ_{+-}	Δm	ϕ_{+-}	τ_S		
\checkmark	\checkmark	\checkmark		APOSTOLAKIS 99C	[5]
\checkmark		\checkmark	\checkmark	GIBBONS 93	[4]
\checkmark	\checkmark	\checkmark	\checkmark	SCHWINGENHEUER 95	[3]
\checkmark		\checkmark	\checkmark	GEWENIGER 74B	[2]
\checkmark	\checkmark^*	\checkmark	\checkmark^*	CAROSI 90	[1]
\checkmark	\checkmark^\dagger	\checkmark	\checkmark	CARITHERS 75	[10]
	\checkmark			ANGELOPOULOS 98D	[11]
	\checkmark			GEWENIGER 74C	[7]
	\checkmark			GJESDAL 74	[8]
	\checkmark			CULLEN 70	[6]
	\checkmark			GIBBONS 93C	[12]
			\checkmark	BERTANZA 97	[9]
			\checkmark	GROSSMAN 87	[13]
			\checkmark	SKJEGGESTAD 72	[14]
			\checkmark	ARONSON 76	[15]

* from $\phi_{00}(\Delta m, \tau_S)$ in ϕ_{00} Particle Listings.

† from $\tau_S(\Delta m)$ in τ_S Particle Listings.

This decrease brings the Δm -dependent ϕ_{+-} measurements into good agreement with each other and with $\phi(\text{superweak})$, where

$$\phi(\text{superweak}) = \tan^{-1} \left(\frac{2\Delta m}{\Delta\Gamma} \right) = \tan^{-1} \left(\frac{2\Delta m \tau_S \tau_L}{\hbar(\tau_L - \tau_S)} \right). \quad (1)$$

The (ϕ_{+-}, τ_S) correlations influence the τ_S fit result in a similar manner, as can be seen in Fig. 2. The influence of the ϕ_{+-} experiments is not as great on τ_S as it is on Δm because the indirect measurements of τ_S derived from the diagonal crossing bands in Fig. 2 are not as precise as the direct measurements of τ_S from E773 (SCHWINGENHEUER 95 [3]), E731 (GIBBONS 93 [4]), and NA31 (BERTANZA 97 [9]).

In Fig. 1 [Fig. 2] the slope of the diagonal ϕ_{+-} bands shows the Δm [τ_S] dependence; the unseen τ_S [Δm] dependent term is evaluated using the fitted τ_S [Δm]. The vertical half-width σ_ϕ of each band is the ϕ_{+-} error for fixed Δm [τ_S] and includes the systematic error due to the error in the fitted τ_S [Δm].

Table 2 gives the resulting fit values for the parameters and Table 3 gives the correlation matrix. The resulting ϕ_{+-} is in good agreement with $\phi(\text{superweak}) = 43.49 \pm 0.07^\circ$ obtained from Eq. (1) using Δm and τ_S from Table 2.

Table 2: Results of the fit for ϕ_{+-} , ϕ_{00} , $\phi_{00} - \phi_{+-}$, Δm , and τ_S . The fit has $\chi^2 = 16.0$ for 20 degrees of freedom (24 measurements -5 parameters $+1$ constraint).

Quantity	Fit Result
ϕ_{+-}	$43.3 \pm 0.5^\circ$
Δm	$(0.5300 \pm 0.0012) \times 10^{10} \hbar \text{ s}^{-1}$
τ_S	$(0.8935 \pm 0.0008) \times 10^{-10} \text{ s}$
ϕ_{00}	$43.2 \pm 1.0^\circ$
$\Delta\phi$	$-0.1 \pm 0.8^\circ$

The χ^2 is 16.0 for 20 degrees of freedom, indicating good agreement of the input data. Nevertheless, there has been criticism that Fermilab E773 (SCHWINGENHEUER 95 [3]) and E731 (GIBBONS 93 [4]) measure $\phi_{+-} - \phi_f$ and calculate the regeneration phase ϕ_f from the power law momentum dependence of the regeneration amplitude using analyticity

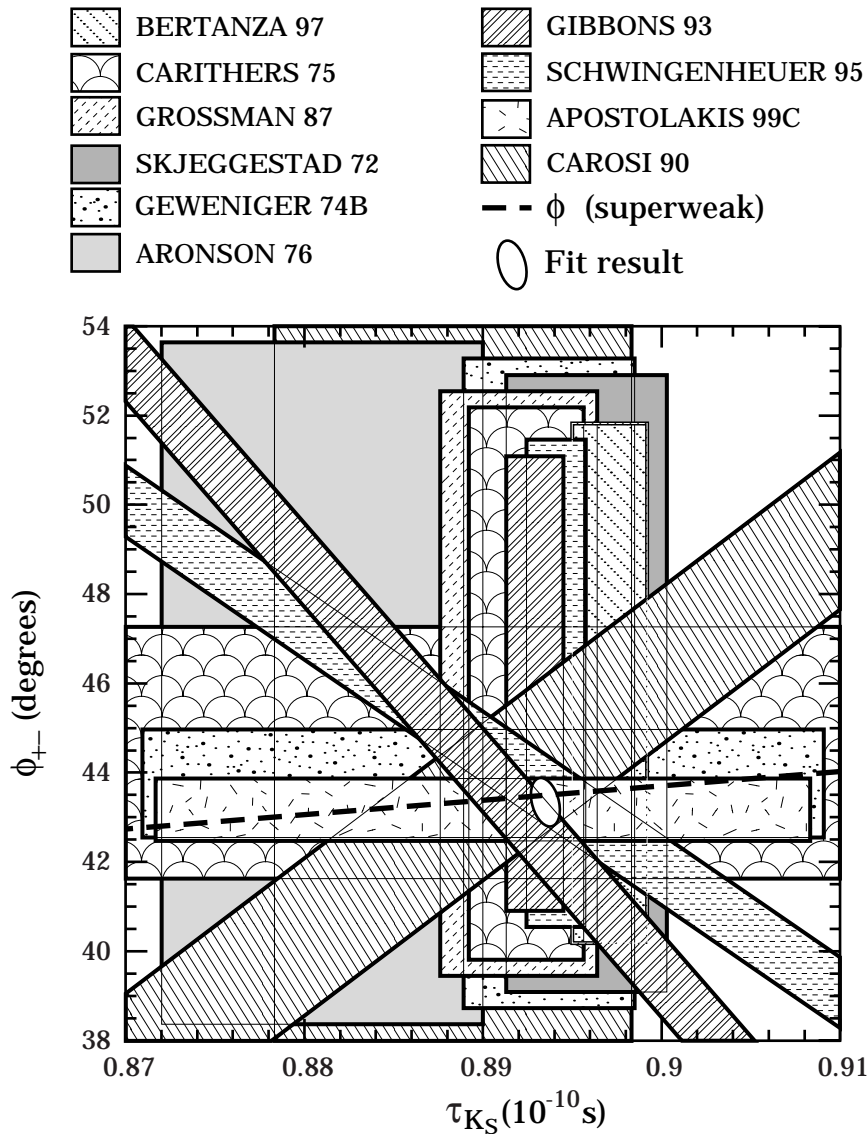


Figure 2: ϕ_{+-} vs τ_{K_S} . τ_{K_S} measurements appear as vertical bands spanning $\tau_{K_S} \pm 1\sigma$, some of which are cut near the top to aid the eye. The ϕ_{+-} measurements appear as diagonal bands spanning $\phi_{+-} \pm \sigma_{\phi}$. The dashed line shows $\phi(\text{superweak})$. The ellipse shows the fit result's 1σ contour. See Table 1 for data references.

Table 3: Correlation matrix for the fitted parameters.

	ϕ_{+-}	Δm	τ_S	ϕ_{00}	$\Delta\phi$
ϕ_{+-}	1.00	0.71	-0.30	0.54	-0.02
Δm	0.71	1.00	-0.19	0.43	0.04
τ_S	-0.30	-0.19	1.00	-0.14	0.04
ϕ_{00}	0.54	0.43	-0.14	1.00	0.83
$\Delta\phi$	-0.02	0.04	0.04	0.83	1.00

and dispersion relations. In the E731 result, a systematic error of ± 0.5 degrees for departures from a pure power-law is included. For the E773 result, they modeled a variety of effects that do distort the amplitude from a pure power law and ascribed a $\pm 0.35^\circ$ systematic error from uncertainties in these effects. Even so, the E731 result remains valid within its quoted errors. KLEINKNECHT 94 [16] and KLEINKNECHT 95 [17] argue that these systematic errors should be around 3° , primarily because of the absence of data on the momentum dependence of the regeneration amplitude above 160 GeV/ c . BRIERE 95 [18] and BRIERE 95C [19] reply that the current understanding of regeneration is sufficient to allow a precise and reliable correction for the region above 160 GeV/ c . The question is one of judgement about the reliability of the assumptions used. In the absence of any contradictory evidence, we choose to accept the judgement of the E731/E773 experimenters in setting their systematic errors.

Fit for ϵ'/ϵ , $|\eta_{+-}|$, $|\eta_{00}|$, and $\mathbf{B}(K_L \rightarrow \pi\pi)$

We list measurements of $|\eta_{+-}|$, $|\eta_{00}|$, $|\eta_{00}/\eta_{+-}|$ and ϵ'/ϵ . Independent information on $|\eta_{+-}|$ and $|\eta_{00}|$ can be obtained from measurements of the

K_L^0 and K_S^0 lifetimes (τ_L , τ_S) and branching ratios (B) to $\pi\pi$, using the relations

$$|\eta_{+-}| = \left[\frac{\text{B}(K_L^0 \rightarrow \pi^+\pi^-)}{\tau_L} \frac{\tau_S}{\text{B}(K_S^0 \rightarrow \pi^+\pi^-)} \right]^{1/2}, \quad (2a)$$

$$|\eta_{00}| = \left[\frac{\text{B}(K_L^0 \rightarrow \pi^0\pi^0)}{\tau_L} \frac{\tau_S}{\text{B}(K_S^0 \rightarrow \pi^0\pi^0)} \right]^{1/2}. \quad (2b)$$

For historical reasons the branching ratio fits and the CP -violation fits are done separately, but we want to include the influence of $|\eta_{+-}|$, $|\eta_{00}|$, $|\eta_{00}/\eta_{+-}|$, and ϵ'/ϵ measurements on $\text{B}(K_L^0 \rightarrow \pi^+\pi^-)$ and $\text{B}(K_L^0 \rightarrow \pi^0\pi^0)$ and vice versa. We approximate a global fit to all of these measurements by first performing two independent fits: 1) BRFIT, a fit to the K_L^0 branching ratios, rates, and mean life, and 2) ETAFIT, a fit to the $|\eta_{+-}|$, $|\eta_{00}|$, $|\eta_{+-}/\eta_{00}|$, and ϵ'/ϵ measurements. The results from fit 1, along with the K_S^0 values from this edition are used to compute values of $|\eta_{+-}|$ and $|\eta_{00}|$ which are included as measurements in the $|\eta_{00}|$ and $|\eta_{+-}|$ sections with a document ID of BRFIT 00. Thus the fit values of $|\eta_{+-}|$ and $|\eta_{00}|$ given in this edition include both the direct measurements and the results from the branching ratio fit.

The process is reversed in order to include the direct $|\eta|$ measurements in the branching ratio fit. The results from fit 2 above (before including BRFIT 00 values) are used along with the K_L^0 and K_S^0 mean lives and the $K_S^0 \rightarrow \pi\pi$ branching fractions to compute the K_L^0 branching ratios $\Gamma(K_L^0 \rightarrow \pi^+\pi^-)/\Gamma(\text{total})$ and $\Gamma(K_L^0 \rightarrow \pi^0\pi^0)/\Gamma(K_L^0 \rightarrow \pi^+\pi^-)$. These branching ratio values are included as measurements in the branching ratio section with a document ID of ETAFIT 00. Thus the K_L^0 branching ratio fit values in this edition include the results of direct measurements of $|\eta_{+-}|$, $|\eta_{00}|$, $|\eta_{00}/\eta_{+-}|$, and ϵ'/ϵ . A more detailed discussion of these fits is given in the 1990 edition of this *Review* [20].

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CP-VIOLATION PARAMETERS IN K_L^0 DECAYS

———— CHARGE ASYMMETRY IN K_{e3}^0 DECAYS ————

Such asymmetry violates *CP*. It is related to $\text{Re}(\epsilon)$.

δ = weighted average of $\delta(\mu)$ and $\delta(e)$

VALUE (%)	EVTS	DOCUMENT ID	TECN	COMMENT
0.327 ± 0.012 OUR AVERAGE		Includes data from the 2 datablocks that follow this one.		
0.333 ± 0.050	33M	WILLIAMS	73 ASPK	$K_{\mu 3} + K_{e 3}$

$$\delta(\mu) = [\Gamma(\pi^- \mu^+ \nu_\mu) - \Gamma(\pi^+ \mu^- \bar{\nu}_\mu)]/\text{SUM}$$

Only the combined value below is put into the Meson Summary Table.

<u>VALUE (%)</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>
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The data in this block is included in the average printed for a previous datablock.

0.304±0.025 OUR AVERAGE

0.313±0.029	15M	GEWENIGER	74	ASPK
0.278±0.051	7.7M	PICCIONI	72	ASPK

• • • We do not use the following data for averages, fits, limits, etc. • • •

0.60 ±0.14	4.1M	MCCARTHY	73	CNTR
0.57 ±0.17	1M	⁹⁷ PACIOTTI	69	OSPK
0.403±0.134	1M	⁹⁷ DORFAN	67	OSPK

⁹⁷PACIOTTI 69 is a reanalysis of DORFAN 67 and is corrected for $\mu^+ \mu^-$ range difference in MCCARTHY 72.

$$\delta(e) = [\Gamma(\pi^- e^+ \nu_e) - \Gamma(\pi^+ e^- \bar{\nu}_e)]/\text{SUM}$$

Only the combined value below is put into the Meson Summary Table.

<u>VALUE (%)</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>
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The data in this block is included in the average printed for a previous datablock.

0.333±0.014 OUR AVERAGE

0.341±0.018	34M	GEWENIGER	74	ASPK
0.318±0.038	40M	FITCH	73	ASPK
0.346±0.033	10M	MARX	70	CNTR
0.246±0.059	10M	⁹⁸ SAAL	69	CNTR

• • • We do not use the following data for averages, fits, limits, etc. • • •

0.36 ±0.18	600k	ASHFORD	72	ASPK
0.224±0.036	10M	⁹⁸ BENNETT	67	CNTR

⁹⁸SAAL 69 is a reanalysis of BENNETT 67.

———— **PARAMETERS FOR $K_L^0 \rightarrow 2\pi$ DECAY** ————

$$\eta_{+-} = A(K_L^0 \rightarrow \pi^+ \pi^-) / A(K_S^0 \rightarrow \pi^+ \pi^-)$$

$$\eta_{00} = A(K_L^0 \rightarrow \pi^0 \pi^0) / A(K_S^0 \rightarrow \pi^0 \pi^0)$$

The fitted values of $|\eta_{+-}|$ and $|\eta_{00}|$ given below are the results of a fit to $|\eta_{+-}|$, $|\eta_{00}|$, $|\eta_{00}/\eta_{+-}|$, and $\text{Re}(\epsilon'/\epsilon)$. Independent information on $|\eta_{+-}|$ and $|\eta_{00}|$ can be obtained from the fitted values of the $K_L^0 \rightarrow \pi\pi$ and $K_S^0 \rightarrow \pi\pi$ branching ratios and the K_L^0 and K_S^0 lifetimes. This information is included as data in the $|\eta_{+-}|$ and $|\eta_{00}|$ sections with a Document ID "BRFIT." See the note "Fits for K_L^0 CP-Violation Parameters" above for details.

$$|\eta_{00}| = |A(K_L^0 \rightarrow 2\pi^0) / A(K_S^0 \rightarrow 2\pi^0)|$$

<u>VALUE (units 10^{-3})</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
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2.262±0.017 OUR FIT

2.23 ±0.11 OUR AVERAGE

2.12 ±0.16	⁹⁹ BRFIT	00	
2.47 ±0.31 ±0.24	ANGELOPO...	98	CPLR
2.33 ±0.18	CHRISTENS...	79	ASPK

• • • We do not use the following data for averages, fits, limits, etc. • • •

2.49 ± 0.40	100	ADLER	96B	CPLR	Sup. by ANGELOPOU- LOS 98
2.71 ± 0.37	101	WOLFF	71	OSPK	Cu reg., 4γ's
2.95 ± 0.63	101	CHOLLET	70	OSPK	Cu reg., 4γ's

⁹⁹This BRFIT value is computed from fitted values of the K_L^0 and K_S^0 lifetimes and branching fractions to $\pi\pi$. See the discussion in the note "Fits for K_L^0 CP-Violation Parameters."

¹⁰⁰Error is statistical only.

¹⁰¹CHOLLET 70 gives $|\eta_{00}| = (1.23 \pm 0.24) \times (\text{regeneration amplitude, 2 GeV/c Cu})/10000\text{mb}$. WOLFF 71 gives $|\eta_{00}| = (1.13 \pm 0.12) \times (\text{regeneration amplitude, 2 GeV/c Cu})/10000\text{mb}$. We compute both $|\eta_{00}|$ values for (regeneration amplitude, 2 GeV/c Cu) = $24 \pm 2\text{mb}$. This regeneration amplitude results from averaging over FAISSNER 69, extrapolated using optical-model calculations of Bohm *et al.*, Physics Letters **27B** 594 (1968) and the data of BALATS 71. (From H. Faissner, private communication).

$$|\eta_{+-}| = |A(K_L^0 \rightarrow \pi^+\pi^-) / A(K_S^0 \rightarrow \pi^+\pi^-)|$$

<u>VALUE (units 10^{-3})</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
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2.276 ± 0.017 OUR FIT

2.277 ± 0.017 OUR AVERAGE

2.272 ± 0.024		102	BRFIT	00	
2.264 ± 0.023 ± 0.027	70M	103	APOSTOLA...	99C	CPLR $K^0\bar{K}^0$ asymmetry
2.30 ± 0.035			GEWENIGER	74B	ASPK

• • • We do not use the following data for averages, fits, limits, etc. • • •

2.310 ± 0.043 ± 0.031		104	ADLER	95B	CPLR $K^0\bar{K}^0$ asymmetry
2.32 ± 0.14 ± 0.03	10 ⁵		ADLER	92B	CPLR $K^0\bar{K}^0$ asymmetry

¹⁰²This BRFIT value is computed from fitted values of the K_L^0 and K_S^0 lifetimes and branching fractions to $\pi\pi$. See the discussion in the note "Fits for K_L^0 CP-Violation Parameters."

¹⁰³APOSTOLAKIS 99C report $(2.264 \pm 0.023 \pm 0.026 + 9.1[\tau_S - 0.8934]) \times 10^{-3}$. We evaluate for our 1998 best value $\tau_S = (0.8934 \pm 0.0008) \times 10^{-10}$ s.

¹⁰⁴ADLER 95B report $(2.312 \pm 0.043 \pm 0.030 - 1[\Delta m - 0.5274] + 9.1[\tau_S - 0.8926]) \times 10^{-3}$. We evaluate for our 1996 best values $\Delta m = (0.5304 \pm 0.0014) \times 10^{-10} \text{h}_s^{-1}$ and $\tau_S = (0.8927 \pm 0.0009) \times 10^{-10}$ s. Superseded by APOSTOLAKIS 99C.

$$|\eta_{00}/\eta_{+-}|$$

<u>VALUE</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>
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0.9936 ± 0.0014 OUR FIT Error includes scale factor of 1.6.

0.9930 ± 0.0020 OUR AVERAGE

0.9931 ± 0.0020		105,106	BARR	93D	NA31
0.9904 ± 0.0084 ± 0.0036		107	WOODS	88	E731

• • • We do not use the following data for averages, fits, limits, etc. • • •

0.9939 ± 0.0013 ± 0.0015	1M	105	BARR	93D	NA31
0.9899 ± 0.0020 ± 0.0025		105	BURKHARDT	88	NA31

¹⁰⁵This is the square root of the ratio R given by BURKHARDT 88 and BARR 93D.

¹⁰⁶This is the combined results from BARR 93D and BURKHARDT 88, taking into account a common systematic uncertainty of 0.0014.

¹⁰⁷We calculate $|\eta_{00}/\eta_{+-}| = 1 - 3(\epsilon'/\epsilon)$ from WOODS 88 (ϵ'/ϵ) value.

$$\epsilon'/\epsilon \approx \text{Re}(\epsilon'/\epsilon) = (1 - |\eta_{00}/\eta_{+-}|)/3$$

VALUE (units 10^{-3})	DOCUMENT ID	TECN	COMMENT
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2.1 ± 0.5 OUR FIT Error includes scale factor of 1.6.
2.1 ± 0.5 OUR AVERAGE Error includes scale factor of 1.7. See the ideogram below.

2.80 ± 0.30 ± 0.28	ALAVI-HARATI 99D	KTEV	
1.85 ± 0.45 ± 0.58	FANTI	99C NA48	
2.3 ± 0.65	108,109 BARR	93D NA31	
0.74 ± 0.52 ± 0.29	GIBBONS	93B E731	

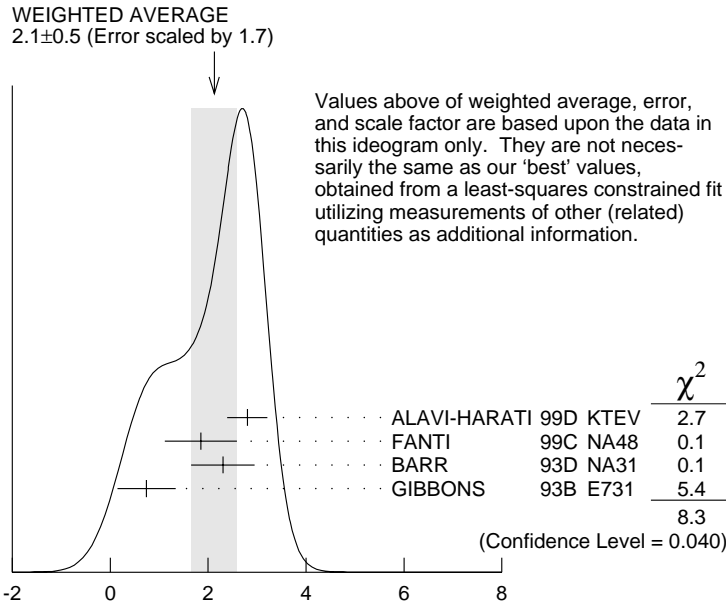
• • • We do not use the following data for averages, fits, limits, etc. • • •

2.0 ± 0.7	110 BARR	93D NA31	
-0.4 ± 1.4 ± 0.6	PATTERSON	90 E731	in GIBBONS 93B
3.3 ± 1.1	110 BURKHARDT	88 NA31	
3.2 ± 2.8 ± 1.2	108 WOODS	88 E731	

¹⁰⁸ These values are derived from $|\eta_{00}/\eta_{+-}|$ measurements. They enter the average in this section but enter the fit via the $|\eta_{00}/\eta_{+-}|$ section only.

¹⁰⁹ This is the combined results from BARR 93D and BURKHARDT 88, taking into account their common systematic uncertainty.

¹¹⁰ These values are derived from $|\eta_{00}/\eta_{+-}|$ measurements.



$$\epsilon'/\epsilon \approx \text{Re}(\epsilon'/\epsilon) = (1 - |\eta_{00}/\eta_{+-}|)/3$$

ϕ_{+-} , PHASE of η_{+-}

The dependence of the phase on Δm and τ_S is given for each experiment in the comments below, where Δm is the $K_L^0 - K_S^0$ mass difference in units $10^{10} \hbar s^{-1}$ and τ_S is the K_S mean life in units 10^{-10} s. For the "used" data, we have evaluated these mass dependences using our 2000 values, $\Delta m = 0.5300 \pm 0.0012$, $\tau_S = 0.8935 \pm 0.0008$

to obtain the values quoted below. We also give the regeneration phase ϕ_f in the comments below.

OUR FIT is described in the note on "Fits for K_L^0 CP-Violation Parameters" in the K_L^0 Particle Listings.

VALUE (°)	EVTS	DOCUMENT ID	TECN	COMMENT
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43.3 ± 0.5 OUR FIT

Average is meaningless.

43.2 ± 0.7	70M	111 APOSTOLA...	99C CPLR	$K^0-\bar{K}^0$ asymmetry
43.6 ± 0.8		112,113 SCHWINGEN...	95 E773	CH _{1,1} regenerator
42.4 ± 1.0		113,114 GIBBONS	93 E731	B ₄ C regenerator
44.4 ± 1.7		115 CAROSI	90 NA31	Vacuum regen.
44.4 ± 2.8		116 CARITHERS	75 SPEC	C regenerator
43.8 ± 1.2		117 GEWENIGER	74B ASPK	Vacuum regen.

• • • We do not use the following data for averages, fits, limits, etc. • • •

43.82 ± 0.63		118,119 ADLER	96C RVUE	
43.6 ± 1.2		120 ADLER	95B CPLR	$K^0-\bar{K}^0$ asymmetry
42.3 ± 4.4 ± 1.4	10 ⁵	121 ADLER	92B CPLR	$K^0-\bar{K}^0$ asymmetry
47.7 ± 2.0 ± 0.9		113,122 KARLSSON	90 E731	

111 APOSTOLAKIS 99C report $(43.19 \pm 0.53 \pm 0.28)^\circ + 300 [\Delta m - 0.5301]^\circ$.

112 SCHWINGENHEUER 95 reports $\phi_{+-} = 43.53 \pm 0.76 + 173[\Delta m - 0.5282] - 275[\tau_S - 0.8926]$.

113 These experiments measure $\phi_{+-} - \phi_f$ and calculate the regeneration phase from the power law momentum dependence of the regeneration amplitude using analyticity and dispersion relations. SCHWINGENHEUER 95 [GIBBONS 93] includes a systematic error of 0.35° [0.5°] for uncertainties in their modeling of the regeneration amplitude. See the discussion of these systematic errors, including criticism that they could be underestimated, in the note on "C violation in K_L^0 decay."

114 GIBBONS 93 measures $\phi_+ - \phi_f$ and calculates the regeneration phase ϕ_f from the power law momentum dependence of the regeneration amplitude using analyticity. An error of 0.6° is included for possible uncertainties in the regeneration phase. They find $\phi_{+-} = 42.21 \pm 0.9 + 189 [\Delta m - 0.5257] - 460 [\tau_S - 0.8922]^\circ$, as given in SCHWINGENHEUER 95, footnote 8. GIBBONS 93 reports $\phi_{+-} (42.2 \pm 1.4)^\circ$

115 CAROSI 90 $\phi_{+-} = 46.9 \pm 1.4 \pm 0.7 + 579 [\Delta m - 0.5351] + 303 [\tau_S - 0.8922]^\circ$.

116 CARITHERS 75 $\phi_{+-} = (45.5 \pm 2.8) + 224 [\Delta m - 0.5348]^\circ$. $\phi_f = -40.9 \pm 2.6^\circ$.

117 GEWENIGER 74B $\phi_{+-} = (49.4 \pm 1.0) + 565 [\Delta m - 0.540]^\circ$.

118 ADLER 96C fit gives $(43.82 \pm 0.41)^\circ + 339(\Delta m - 0.5307)^\circ - 252(\tau_S - 0.8922)^\circ$.

119 ADLER 96C is the result of a fit which includes nearly the same data as entered into the "OUR FIT" value in the 1996 edition of this Review (Physical Review **D54** 1 (1996)).

120 ADLER 95B report $42.7^\circ \pm 0.9^\circ \pm 0.6^\circ + 316[\Delta m - 0.5274]^\circ + 30[\tau_S - 0.8926]^\circ$.

121 ADLER 92B quote separately two systematic errors: ± 0.4 from their experiment and ± 1.0 degrees due to the uncertainty in the value of Δm .

122 KARLSSON 90 systematic error does not include regeneration phase uncertainty.

ϕ_{00} , PHASE OF η_{00}

See comment in ϕ_{+-} header above for treatment of Δm and τ_S dependence.

OUR FIT is described in the note on "Fits for K_L^0 CP-Violation Parameters" in the K_L^0 Particle Listings.

VALUE (°)	DOCUMENT ID	TECN	COMMENT
43.2 ± 1.0 OUR FIT			
Average is meaningless.			
41.9 ± 5.6 ± 1.9	123 ANGELOPO...	98 CPLR	
44.5 ± 2.5	124 CAROSI	90 NA31	
• • • We do not use the following data for averages, fits, limits, etc. • • •			
50.8 ± 7.1 ± 1.7	125 ADLER	96B CPLR	Sup. by ANGELOPOU-LOS 98
47.4 ± 1.4 ± 0.9	126 KARLSSON	90 E731	
123 ANGELOPOULOS 98 $\phi_{00} = 42.0 \pm 5.6 \pm 1.9 + 240[\Delta m - 0.5307]$ with negligible τ_S dependence.			
124 CAROSI 90 $\phi_{00} = 47.1 \pm 2.1 \pm 1.0 + 579 [\Delta m - 0.5351] + 252 [\tau_S - 0.8922]^\circ$.			
125 ADLER 96B identified initial neutral kaon individually as being a K^0 or a \bar{K}^0 . The systematic uncertainty is $\pm 1.5^\circ$ combined in quadrature with $\pm 0.8^\circ$ due to Δm .			
126 KARLSSON 90 systematic error does not include regeneration phase uncertainty.			

PHASE DIFFERENCE $\phi_{00} - \phi_{+-}$

Test of CPT.

OUR FIT is described in the note on "Fits for K_L^0 CP-Violation Parameters" in the K_L^0 Particle Listings.

VALUE (°)	DOCUMENT ID	TECN	COMMENT
-0.1 ± 0.8 OUR FIT			
-0.3 ± 0.8 OUR AVERAGE			
-0.30 ± 0.88	127 SCHWINGEN...95		Combined E731, E773
0.2 ± 2.6 ± 1.2	128 CAROSI	90 NA31	
• • • We do not use the following data for averages, fits, limits, etc. • • •			
0.62 ± 0.71 ± 0.75	SCHWINGEN...95	E773	
-1.6 ± 1.2	129 GIBBONS	93 E731	
-0.3 ± 2.4 ± 1.2	KARLSSON	90 E731	
127 This SCHWINGENHEUER 95 values is the combined result of SCHWINGENHEUER 95 and GIBBONS 93, accounting for correlated systematic errors.			
128 CAROSI 90 is excluded from the fit because it is not independent of ϕ_{+-} and ϕ_{00} values.			
129 GIBBONS 93 give detailed dependence of systematic error on lifetime (see the section on the K_S^0 mean life) and mass difference (see the section on $m_{K_L^0} - m_{K_S^0}$).			

DECAY-PLANE ASYMMETRY IN $\pi^+ \pi^- e^+ e^-$ DECAYS

This is the CP-violating asymmetry

$$A = \frac{N_{\sin\phi\cos\phi > 0.0} - N_{\sin\phi\cos\phi < 0.0}}{N_{\sin\phi\cos\phi > 0.0} + N_{\sin\phi\cos\phi < 0.0}}$$

where ϕ is the angle between the $e^+ e^-$ and $\pi^+ \pi^-$ planes in the K_L^0 rest frame.

CP ASYMMETRY A in $K_L^0 \rightarrow \pi^+ \pi^- e^+ e^-$

VALUE (%)	DOCUMENT ID	TECN
13.6 ± 2.5 ± 1.2	ALAVI-HARATI00B	KTEV

———— CHARGE ASYMMETRY IN $\pi^+\pi^-\pi^0$ DECAYS ————

These are *CP*-violating charge-asymmetry parameters, defined at beginning of section "LINEAR COEFFICIENT *g* FOR $K_L^0 \rightarrow \pi^+\pi^-\pi^0$ above.

See also note on Dalitz plot parameters in K^\pm section and note on *CP* violation in K_L^0 decay above.

LINEAR COEFFICIENT *j* FOR $K_L^0 \rightarrow \pi^+\pi^-\pi^0$

<u>VALUE</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>
0.0011 ± 0.0008 OUR AVERAGE			
0.0010 ± 0.0024 ± 0.0030	500k	ANGELOPO...	98C CPLR
0.001 ± 0.011	6499	CHO	77
−0.001 ± 0.003	4709	PEACH	77
0.0013 ± 0.0009	3M	SCRIBANO	70
0.0 ± 0.017	4400	SMITH	70 OSPK
0.001 ± 0.004	238k	BLANPIED	68

QUADRATIC COEFFICIENT *f* FOR $K_L^0 \rightarrow \pi^+\pi^-\pi^0$

<u>VALUE</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>
0.0045 ± 0.0024 ± 0.0059	500k	ANGELOPO...	98C CPLR

———— PARAMETERS for $K_L^0 \rightarrow \pi^+\pi^-\gamma$ DECAY ————

$$|\eta_{+-\gamma}| = |A(K_L^0 \rightarrow \pi^+\pi^-\gamma, \text{CP violating})/A(K_S^0 \rightarrow \pi^+\pi^-\gamma)|$$

<u>VALUE (units 10^{-3})</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>
2.35 ± 0.07 OUR AVERAGE			
2.359 ± 0.062 ± 0.040	9045	MATTHEWS	95 E773
2.15 ± 0.26 ± 0.20	3671	RAMBERG	93B E731

$$\phi_{+-\gamma} = \text{phase of } \eta_{+-\gamma}$$

<u>VALUE (°)</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>
44 ± 4 OUR AVERAGE			
43.8 ± 3.5 ± 1.9	9045	MATTHEWS	95 E773
72 ± 23 ± 17	3671	RAMBERG	93B E731

$$|\epsilon'_{+-\gamma}|/\epsilon \text{ for } K_L^0 \rightarrow \pi^+\pi^-\gamma$$

<u>VALUE</u>	<u>CL%</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>
<0.3	90	3671	130 RAMBERG	93B E731

130 RAMBERG 93B limit on $|\epsilon'_{+-\gamma}|/\epsilon$ assumes that any difference between η_{+-} and $\eta_{+-\gamma}$ is due to direct *CP* violation.

Δ*S* = Δ*Q* IN K^0 DECAYS

The relative amount of $\Delta S \neq \Delta Q$ component present is measured by the parameter *x*, defined as

$$x = A(\bar{K}^0 \rightarrow \pi^-\ell^+\nu)/A(K^0 \rightarrow \pi^-\ell^+\nu).$$

We list $\text{Re}\{x\}$ and $\text{Im}\{x\}$ for K_{e3} and $K_{\mu3}$ combined.

$$x = A(\bar{K}^0 \rightarrow \pi^- \ell^+ \nu) / A(K^0 \rightarrow \pi^- \ell^+ \nu) = A(\Delta S = -\Delta Q) / A(\Delta S = \Delta Q)$$

REAL PART OF x

VALUE	EVTs	DOCUMENT ID	TECN	COMMENT
-0.002 ± 0.006 OUR AVERAGE				
-0.0018 ± 0.0041 ± 0.0045				
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●				
0.10 ^{+0.18} _{-0.19}	79	SMITH	75B WIRE	$\pi^- p \rightarrow K^0 \Lambda$
0.04 ± 0.03	4724	NIEBERGALL	74 ASPK	$K^+ p \rightarrow K^0 p \pi^+$
-0.008 ± 0.044	1757	FACKLER	73 OSPK	K_{e3} from K^0
-0.03 ± 0.07	1367	HART	73 OSPK	K_{e3} from $K^0 \Lambda$
-0.070 ± 0.036	1079	MALLARY	73 OSPK	K_{e3} from $K^0 \Lambda X$
0.03 ± 0.06	410	131 BURGUN	72 HBC	$K^+ p \rightarrow K^0 p \pi^+$
0.04 ^{+0.10} _{-0.13}	100	132 GRAHAM	72 OSPK	$K_{\mu 3}$ from $K^0 \Lambda$
-0.05 ± 0.09	442	132 GRAHAM	72 OSPK	$\pi^- p \rightarrow K^0 \Lambda$
0.26 ^{+0.10} _{-0.14}	126	MANN	72 HBC	$K^- p \rightarrow n \bar{K}^0$
-0.13 ± 0.11	342	132 MANTSCH	72 OSPK	K_{e3} from $K^0 \Lambda$
0.04 ^{+0.07} _{-0.08}	222	131 BURGUN	71 HBC	$K^+ p \rightarrow K^0 p \pi^+$
0.25 ^{+0.07} _{-0.09}	252	WEBBER	71 HBC	$K^- p \rightarrow n \bar{K}^0$
0.12 ± 0.09	215	133 CHO	70 DBC	$K^+ d \rightarrow K^0 p p$
-0.020 ± 0.025		134 BENNETT	69 CNTR	Charge asym+ Cu regen.
0.09 ^{+0.14} _{-0.16}	686	LITTENBERG	69 OSPK	$K^+ n \rightarrow K^0 p$
0.03 ± 0.03		134 BENNETT	68 CNTR	
0.09 ^{+0.07} _{-0.09}	121	JAMES	68 HBC	$\bar{p} p$
0.17 ^{+0.16} _{-0.35}	116	FELDMAN	67B OSPK	$\pi^- p \rightarrow K^0 \Lambda$
0.17 ± 0.10	335	133 HILL	67 DBC	$K^+ d \rightarrow K^0 p p$
0.035 ^{+0.11} _{-0.13}	196	AUBERT	65 HLBC	K^+ charge exchange
0.06 ^{+0.18} _{-0.44}	152	135 BALDO-...	65 HLBC	K^+ charge exchange
-0.08 ^{+0.16} _{-0.28}	109	136 FRANZINI	65 HBC	$\bar{p} p$

¹³¹ BURGUN 72 is a final result which includes BURGUN 71.

¹³² First GRAHAM 72 value is second GRAHAM 72 value combined with MANTSCH 72.

¹³³ CHO 70 is analysis of unambiguous events in new data and HILL 67.

¹³⁴ BENNETT 69 is a reanalysis of BENNETT 68.

¹³⁵ BALDO-CEOLIN 65 gives x and θ converted by us to $\text{Re}(x)$ and $\text{Im}(x)$.

¹³⁶ FRANZINI 65 gives x and θ for $\text{Re}(x)$ and $\text{Im}(x)$. See SCHMIDT 67.

IMAGINARY PART OF x

Assumes $m_{K_L^0} - m_{K_S^0}$ positive. See Listings above.

VALUE	EVTs	DOCUMENT ID	TECN	COMMENT
0.0012 ± 0.0019 OUR AVERAGE				
0.0012 ± 0.0019	640k	ANGELOPO...	98E CPLR	K_{e3} from K^0
• • • We do not use the following data for averages, fits, limits, etc. • • •				
-0.10 $\begin{smallmatrix} +0.16 \\ -0.19 \end{smallmatrix}$	79	SMITH	75B WIRE	$\pi^- p \rightarrow K^0 \Lambda$
-0.06 ± 0.05	4724	NIEBERGALL	74 ASPK	$K^+ p \rightarrow K^0 p \pi^+$
-0.017 ± 0.060	1757	FAKLER	73 OSPK	K_{e3} from K^0
0.09 ± 0.07	1367	HART	73 OSPK	K_{e3} from $K^0 \Lambda$
0.107 $\begin{smallmatrix} +0.092 \\ -0.074 \end{smallmatrix}$	1079	MALLARY	73 OSPK	K_{e3} from $K^0 \Lambda X$
0.07 $\begin{smallmatrix} +0.06 \\ -0.07 \end{smallmatrix}$	410	¹³⁷ BURGUN	72 HBC	$K^+ p \rightarrow K^0 p \pi^+$
0.12 $\begin{smallmatrix} +0.17 \\ -0.16 \end{smallmatrix}$	100	¹³⁸ GRAHAM	72 OSPK	$K_{\mu 3}$ from $K^0 \Lambda$
0.05 ± 0.13	442	¹³⁸ GRAHAM	72 OSPK	$\pi^- p \rightarrow K^0 \Lambda$
0.21 $\begin{smallmatrix} +0.15 \\ -0.12 \end{smallmatrix}$	126	MANN	72 HBC	$K^- p \rightarrow n \bar{K}^0$
-0.04 ± 0.16	342	¹³⁸ MANTSCH	72 OSPK	K_{e3} from $K^0 \Lambda$
0.12 $\begin{smallmatrix} +0.08 \\ -0.09 \end{smallmatrix}$	222	¹³⁷ BURGUN	71 HBC	$K^+ p \rightarrow K^0 p \pi^+$
0.0 ± 0.08	252	WEBBER	71 HBC	$K^- p \rightarrow n \bar{K}^0$
-0.08 ± 0.07	215	¹³⁹ CHO	70 DBC	$K^+ d \rightarrow K^0 p p$
-0.11 $\begin{smallmatrix} +0.10 \\ -0.11 \end{smallmatrix}$	686	LITTENBERG	69 OSPK	$K^+ n \rightarrow K^0 p$
+0.22 $\begin{smallmatrix} +0.37 \\ -0.29 \end{smallmatrix}$	121	JAMES	68 HBC	$\bar{p} p$
0.0 ± 0.25	116	FELDMAN	67B OSPK	$\pi^- p \rightarrow K^0 \Lambda$
-0.20 ± 0.10	335	¹³⁹ HILL	67 DBC	$K^+ d \rightarrow K^0 p p$
-0.21 $\begin{smallmatrix} +0.11 \\ -0.15 \end{smallmatrix}$	196	AUBERT	65 HLBC	K^+ charge exchange
-0.44 $\begin{smallmatrix} +0.32 \\ -0.19 \end{smallmatrix}$	152	¹⁴⁰ BALDO-...	65 HLBC	K^+ charge exchange
+0.24 $\begin{smallmatrix} +0.40 \\ -0.30 \end{smallmatrix}$	109	¹⁴¹ FRANZINI	65 HBC	$\bar{p} p$

¹³⁷BURGUN 72 is a final result which includes BURGUN 71.

¹³⁸First GRAHAM 72 value is second GRAHAM 72 value combined with MANTSCH 72.

¹³⁹Footnote 10 of HILL 67 should read +0.58, not -0.58 (private communication) CHO 70 is analysis of unambiguous events in new data and HILL 67.

¹⁴⁰BALDO-CEOLIN 65 gives x and θ converted by us to $\text{Re}(x)$ and $\text{Im}(x)$.

¹⁴¹FRANZINI 65 gives x and θ for $\text{Re}(x)$ and $\text{Im}(x)$. See SCHMIDT 67.

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HEINSON	91	PR D44 R1	A.P. Heinson <i>et al.</i>	(UCI, UCLA, LANL+)
PAPADIMITR...	91	PR D44 R573	V. Papadimitriou <i>et al.</i>	(FNAL E731 Collab.)
BARKER	90	PR D41 3546	A.R. Barker <i>et al.</i>	(FNAL E731 Collab.)
Also	88	PRL 61 2661	L.K. Gibbons <i>et al.</i>	(FNAL E731 Collab.)
BARR	90B	PL B240 283	G.D. Barr <i>et al.</i>	(CERN, EDIN, MANZ, LALO+)
BARR	90C	PL B242 523	G.D. Barr <i>et al.</i>	(CERN, EDIN, MANZ, LALO+)
CAROSI	90	PL B237 303	R. Carosi <i>et al.</i>	(CERN, EDIN, MANZ, LALO+)
KARLSSON	90	PRL 64 2976	M. Karlsson <i>et al.</i>	(FNAL E731 Collab.)
OHL	90	PRL 64 2755	K.E. Ohl <i>et al.</i>	(BNL E845 Collab.)
OHL	90B	PRL 65 1407	K.E. Ohl <i>et al.</i>	(BNL E845 Collab.)
PATTERSON	90	PRL 64 1491	J.R. Patterson <i>et al.</i>	(FNAL E731 Collab.)
INAGAKI	89	PR D40 1712	T. Inagaki <i>et al.</i>	(KEK, TOKY, KYOT)
LITTENBERG	89	PR D39 3322	L.S. Littenberg	(BNL)
MATHIAZHA...	89	PRL 63 2181	C. Mathiazhagan <i>et al.</i>	(UCI, UCLA, LANL+)
MATHIAZHA...	89B	PRL 63 2185	C. Mathiazhagan <i>et al.</i>	(UCI, UCLA, LANL+)
PAPADIMITR...	89	PRL 63 28	V. Papadimitriou <i>et al.</i>	(FNAL E731 Collab.)
SCHAFFNER	89	PR D39 990	S.F. Schaffner <i>et al.</i>	(YALE, BNL)
WAHL	89	CERN-EP/89-86, H. Wahl	H. Wahl - <i>Particle Decay Symposium, Vancouver</i>	(CERN)
BARR	88	PL B214 303	G.D. Barr <i>et al.</i>	(CERN, EDIN, MANZ, LALO+)
BURKHARDT	88	PL B206 169	H. Burkhardt <i>et al.</i>	(CERN, EDIN, MANZ+)
COUSINS	88	PR D38 2914	R.D. Cousins <i>et al.</i>	(UCLA, LASL, PENN+)
GREENLEE	88	PRL 60 893	H.B. Greenlee <i>et al.</i>	(YALE, BNL)
JASTRZEM...	88	PRL 61 2300	E. Jastrzemski <i>et al.</i>	(BNL, YALE)
WOODS	88	PRL 60 1695	M. Woods <i>et al.</i>	(FNAL E731 Collab.)
BURKHARDT	87	PL B199 139	H. Burkhardt <i>et al.</i>	(CERN, EDIN, MANZ+)
ARONSON	86	PR D33 3180	S.H. Aronson <i>et al.</i>	(BNL, CHIC, STAN+)
Also	82	PRL 48 1078	S.H. Aronson <i>et al.</i>	(BNL, CHIC, STAN+)
PDG	86C	PL 170B 132	M. Aguilar-Benitez <i>et al.</i>	(CERN, CIT+)
COUPAL	85	PRL 55 566	D.P. Coupal <i>et al.</i>	(CHIC, SACL)
BALATS	83	SJNP 38 556	M.Y. Balats <i>et al.</i>	(ITEP)
BERGSTROM	83	Translated from YAF 38 927. PL 131B 229	L. Bergstrom, E. Masso, P. Singer	(CERN)
ARONSON	82	PRL 48 1078	S.H. Aronson <i>et al.</i>	(BNL, CHIC, STAN+)
ARONSON	82B	PRL 48 1306	S.H. Aronson <i>et al.</i>	(BNL, CHIC, PURD)
Also	82B	PL 116B 73	E. Fischbach <i>et al.</i>	(PURD, BNL, CHIC)
Also	83	PR D28 476	S.H. Aronson <i>et al.</i>	(BNL, CHIC, PURD)
Also	83B	PR D28 495	S.H. Aronson <i>et al.</i>	(BNL, CHIC, PURD)
PDG	82B	PL 111B 70	M. Roos <i>et al.</i>	(HELSE, CIT, CERN)
BIRULEV	81	NP B182 1	V.K. Birulev <i>et al.</i>	(JINR)
Also	80	SJNP 31 622	V.K. Birulev <i>et al.</i>	(JINR)
CARROLL	80B	PRL 44 529	A.S. Carroll <i>et al.</i>	(BNL, ROCH)
CARROLL	80C	PL 96B 407	A.S. Carroll <i>et al.</i>	(BNL, ROCH)
CARROLL	80D	PRL 44 525	A.S. Carroll <i>et al.</i>	(BNL, ROCH)
CHO	80	PR D22 2688	Y. Cho <i>et al.</i>	(ANL, CMU)
MORSE	80	PR D21 1750	W.M. Morse <i>et al.</i>	(BNL, YALE)
BIRULEV	79	SJNP 29 778	V.K. Birulev <i>et al.</i>	(JINR)
CHRISTENS...	79	Translated from YAF 29 1516. PRL 43 1209	J.H. Christenson <i>et al.</i>	(NYU)
HILL	79	NP B153 39	D.G. Hill <i>et al.</i>	(BNL, SLAC, SBER)
SCHMIDT	79	PRL 43 556	M.P. Schmidt <i>et al.</i>	(YALE, BNL)
SHOCHET	79	PR D19 1965	M.J. Shochet <i>et al.</i>	(EFI, ANL)
Also	77	PRL 39 59	M.J. Shochet <i>et al.</i>	(EFI, ANL)
ENGLER	78B	PR D18 623	A. Engler <i>et al.</i>	(CMU, ANL)
HILL	78	PL 73B 483	D.G. Hill <i>et al.</i>	(BNL, SLAC, SBER)
CHO	77	PR D15 587	Y. Cho <i>et al.</i>	(ANL, CMU)
CLARK	77	PR D15 553	A.R. Clark <i>et al.</i>	(LBL)
Also	75	Thesis LBL-4275	G. Shen	(LBL)
DEVOE	77	PR D16 565	R. Devoe <i>et al.</i>	(EFI, ANL)
DZHORD...	77	SJNP 26 478	V.P. Dzhordzhadze <i>et al.</i>	(JINR)
PEACH	77	Translated from YAF 26 910. NP B127 399	K.J. Peach <i>et al.</i>	(BGNA, EDIN, GLAS+)
BIRULEV	76	SJNP 24 178	V.K. Birulev <i>et al.</i>	(JINR)
		Translated from YAF 24 340.		

COOMBES	76	PRL 37 249	R.W. Coombes <i>et al.</i>	(STAN, NYU)
DONALDSON	76	PR D14 2839	G. Donaldson <i>et al.</i>	(SLAC)
Also	74	Thesis SLAC-0184	G. Donaldson	(SLAC)
FUKUSHIMA	76	PRL 36 348	Y. Fukushima <i>et al.</i>	(PRIN, MASA)
GJESDAL	76	NP B109 118	G. Gjesdal <i>et al.</i>	(CERN, HEIDH)
REY	76	PR D13 1161	C.A. Rey <i>et al.</i>	(NDAM, HAWA, LBL)
Also	69	PRL 22 1210	R.J. Cence <i>et al.</i>	(HAWA, LRL)
BALDO-...	75	NC 25A 688	M. Baldo-Ceolin <i>et al.</i>	(PADO, WISC)
BLUMENTHAL	75	PRL 34 164	R.B. Blumenthal <i>et al.</i>	(PENN, CHIC, TEMP)
BUCHANAN	75	PR D11 457	C.D. Buchanan <i>et al.</i>	(UCLA, SLAC, JHU)
CARITHERS	75	PRL 34 1244	W.C.J. Carithers <i>et al.</i>	(COLU, NYU)
SMITH	75B	Thesis UCSD unpub.	J.G. Smith	(UCSD)
ALBRECHT	74	PL 48B 393	K.F. Albrecht	(JINR, BERL, BUDA, PRAG, SERP+)
BISI	74	PL 50B 504	V. Bisi, M.I. Ferrero	(TORI)
DONALDSON	74	Thesis SLAC-0184	G. Donaldson	(SLAC)
Also	76	PR D14 2839	G. Donaldson <i>et al.</i>	(SLAC)
DONALDSON	74B	PR D9 2960	G. Donaldson <i>et al.</i>	(SLAC, UCSC)
Also	73B	PRL 31 337	G. Donaldson <i>et al.</i>	(SLAC, UCSC)
DONALDSON	74C	PRL 33 554	G. Donaldson <i>et al.</i>	(SLAC)
Also	74	Thesis SLAC-0184	G. Donaldson	(SLAC)
Also	76	PR D14 2839	G. Donaldson <i>et al.</i>	(SLAC)
FIELD	74	SLAC-PUB-1498 unpub.	R.C. Field	(SLAC)
GEWENIGER	74	PL 48B 483	C. Geweniger <i>et al.</i>	(CERN, HEIDH)
Also	74	Thesis CERN Int. 74-4	V. Luth	(CERN)
GEWENIGER	74B	PL 48B 487	C. Geweniger <i>et al.</i>	(CERN, HEIDH)
Also	74B	PL 52B 119	S. Gjesdal <i>et al.</i>	(CERN, HEIDH)
GEWENIGER	74C	PL 52B 108	C. Geweniger <i>et al.</i>	(CERN, HEIDH)
GJESDAL	74	PL 52B 113	S. Gjesdal <i>et al.</i>	(CERN, HEIDH)
MESSNER	74	PRL 33 1458	R. Messner <i>et al.</i>	(COLO, SLAC, UCSC)
NIEBERGALL	74	PL 49B 103	F. Niebergall <i>et al.</i>	(CERN, ORSAY, VIEN)
WANG	74	PR D9 540	L. Wang <i>et al.</i>	(UMD, BNL)
WILLIAMS	74	PRL 33 240	H.H. Williams <i>et al.</i>	(BNL, YALE)
ALBROW	73	NP B58 22	M.G. Albrow <i>et al.</i>	(MCHS, DARE)
ALEXANDER	73B	NP B65 301	G. Alexander <i>et al.</i>	(TELA, HEID)
ANIKINA	73	JINR P1 7539	M.K. Anikina <i>et al.</i>	(JINR)
BRANDENB...	73	PR D8 1978	G.W. Brandenburg <i>et al.</i>	(SLAC)
CARITHERS	73	PRL 31 1025	W.C.J. Carithers <i>et al.</i>	(COLU, BNL, CERN)
Also	73B	PRL 30 1336	W.C.J. Carithers <i>et al.</i>	(COLU, CERN, NYU)
EVANS	73	PR D7 36	G.R. Evans <i>et al.</i>	(EDIN, CERN)
Also	69	PRL 23 427	G.R. Evans <i>et al.</i>	(EDIN, CERN)
FACKLER	73	PRL 31 847	O. Fackler <i>et al.</i>	(MIT)
FITCH	73	PRL 31 1524	V.L. Fitch <i>et al.</i>	(PRIN)
Also	72	Thesis COO-3072-13	R.C. Webb	(PRIN)
GINSBERG	73	PR D8 3887	E.S. Ginsberg, J. Smith	(MIT, STON)
HART	73	NP B66 317	J.C. Hart <i>et al.</i>	(CAVE, RHEL)
MALLARY	73	PR D7 1953	M.L. Mallery <i>et al.</i>	(CIT)
Also	70	PRL 25 1214	F.J. Sciulli <i>et al.</i>	(CIT)
MCCARTHY	73	PR D7 687	R.L. McCarthy <i>et al.</i>	(LBL)
Also	72	PL 42B 291	R.L. McCarthy <i>et al.</i>	(LBL)
Also	71	Thesis LBL-550	R.L. McCarthy	(LBL)
MESSNER	73	PRL 30 876	R. Messner <i>et al.</i>	(COLO, SLAC, UCSC)
PEACH	73	PL 43B 441	K.J. Peach <i>et al.</i>	(EDIN, CERN, AACH)
SANDWEISS	73	PRL 30 1002	J. Sandweiss <i>et al.</i>	(YALE, ANL)
WILLIAMS	73	PRL 31 1521	H.H. Williams <i>et al.</i>	(BNL, YALE)
ALBROW	72	NP B44 1	M.G. Albrow <i>et al.</i>	(MCHS, DARE)
ASHFORD	72	PL 38B 47	V.A. Ashford <i>et al.</i>	(UCSD)
BANNER	72B	PRL 29 237	M. Banner <i>et al.</i>	(PRIN)
BARMIN	72	SJNP 15 636	V.V. Barmin <i>et al.</i>	(ITEP)
Also	72B	Translated from YAF 15 1149.	V.V. Barmin <i>et al.</i>	(ITEP)
Also	72B	SJNP 15 638	V.V. Barmin <i>et al.</i>	(ITEP)
Also	72B	Translated from YAF 15 1152.	V.V. Barmin <i>et al.</i>	(ITEP)
BURGUN	72	NP B50 194	G. Burgun <i>et al.</i>	(SACL, CERN, OSLO)
DALLY	72	PL 41B 647	E.B. Dally <i>et al.</i>	(SLAC, JHU, UCLA)
Also	70	PL 33B 627	C.Y. Chien <i>et al.</i>	(JHU, SLAC, UCLA)
Also	71	PL 35B 261	C.Y. Chien <i>et al.</i>	(JHU, SLAC, UCLA)
GRAHAM	72	NC 9A 166	M.F. Graham <i>et al.</i>	(ILL, NEAS)
JAMES	72	NP B49 1	F. James <i>et al.</i>	(CERN, SACL, OSLO)
KRENZ	72	LNC 4 213	W. Krenz <i>et al.</i>	(AACH, CERN, EDIN)
MANN	72	PR D6 137	W.A. Mann <i>et al.</i>	(MASA, BNL, YALE)
MANTSCH	72	NC 9A 160	P.M. Mantsch <i>et al.</i>	(ILL, NEAS)

MCCARTHY	72	PL 42B 291	R.L. McCarthy <i>et al.</i>	(LBL)
METCALF	72	PL 40B 703	M. Metcalf <i>et al.</i>	(CERN, IPN, WIEN)
NEUHOFER	72	PL 41B 642	G. Neuhofer <i>et al.</i>	(CERN, ORSAY, VIEN)
PICCIONI	72	PRL 29 1412	R. Piccioni <i>et al.</i>	(SLAC)
Also	74	PR D9 2939	R. Piccioni <i>et al.</i>	(SLAC, UCSC, COLO)
VOSBURGH	72	PR D6 1834	K.G. Vosburgh <i>et al.</i>	(RUTG, MASA)
Also	71	PRL 26 866	K.G. Vosburgh <i>et al.</i>	(RUTG, MASA)
BALATS	71	SJNP 13 53	M.Y. Balats <i>et al.</i>	(ITEP)
		Translated from YAF 13 93.		
BARMIN	71	PL 35B 604	V.V. Barmin <i>et al.</i>	(ITEP)
BISI	71	PL 36B 533	V. Bisi <i>et al.</i>	(AACH, CERN, TORI)
BURGUN	71	LNC 2 1169	G. Burgun <i>et al.</i>	(SACL, CERN, OSLO)
CARNEGIE	71	PR D4 1	R.K. Carnegie <i>et al.</i>	(PRIN)
CHAN	71	Thesis LBL-350	J.H.S. Chan	(LBL)
CHIEN	71	PL 35B 261	C.Y. Chien <i>et al.</i>	(JHU, SLAC, UCLA)
Also	72	PL 41B 647	E.B. Dally <i>et al.</i>	(SLAC, JHU, UCLA)
CHO	71	PR D3 1557	Y. Cho <i>et al.</i>	(CMU, BNL, CASE)
CLARK	71	PRL 26 1667	A.R. Clark <i>et al.</i>	(LRL)
Also	70	Thesis UCRL 19709	R.P. Johnson	(LRL)
Also	71	Thesis UCRL 20264	H.J. Frisch	(LRL)
Also	74	SLAC-PUB-1498 unpub.	R.C. Field	(SLAC)
ENSTROM	71	PR D4 2629	J. Enstrom <i>et al.</i>	(SLAC, STAN)
Also	70	Thesis SLAC-0125	J.E. Enstrom	(STAN)
JAMES	71	PL 35B 265	F. James <i>et al.</i>	(CERN, SACL, OSLO)
MEISNER	71	PR D3 59	G.W. Meisner <i>et al.</i>	(MASA, BNL, YALE)
PEACH	71	PL 35B 351	K.J. Peach <i>et al.</i>	(EDIN, CERN)
REPELLIN	71	PL 36B 603	J.P. Repellin <i>et al.</i>	(ORSAY, CERN)
WEBBER	71	PR D3 64	B.R. Webber <i>et al.</i>	(LRL)
Also	68	PRL 21 498	B.R. Webber <i>et al.</i>	(LRL)
Also	69	Thesis UCRL 19226	B.R. Webber	(LRL)
WOLFF	71	PL 36B 517	B. Wolff <i>et al.</i>	(ORSAY, CERN)
ALBROW	70	PL 33B 516	M.G. Albrow <i>et al.</i>	(MCHS, DARE)
ARONSON	70	PRL 25 1057	S.H. Aronson <i>et al.</i>	(EFI, ILLC, SLAC)
BARMIN	70	PL 33B 377	V.V. Barmin <i>et al.</i>	(ITEP, JINR)
BASILE	70	PR D2 78	P. Basile <i>et al.</i>	(SACL)
BECHERRAWY	70	PR D1 1452	T. Becherrawy	(ROCH)
BUCHANAN	70	PL 33B 623	C.D. Buchanan <i>et al.</i>	(SLAC, JHU, UCLA)
Also	71	Private Comm.	Cox	
BUDAGOV	70	PR D2 815	I.A. Budagov <i>et al.</i>	(CERN, ORSAY, EPOL)
Also	68B	PL 28B 215	I.A. Budagov <i>et al.</i>	(CERN, ORSAY, EPOL)
CHIEN	70	PL 33B 627	C.Y. Chien <i>et al.</i>	(JHU, SLAC, UCLA)
Also	71	Private Comm.	Cox	
CHO	70	PR D1 3031	Y. Cho <i>et al.</i>	(CMU, BNL, CASE)
Also	67	PRL 19 668	D.G. Hill <i>et al.</i>	(BNL, CMU)
CHOLLET	70	PL 31B 658	J.C. Chollet <i>et al.</i>	(CERN)
CULLEN	70	PL 32B 523	M. Cullen <i>et al.</i>	(AACH, CERN, TORI)
DARRIULAT	70	PL 33B 249	P. Darriulat <i>et al.</i>	(AACH, CERN, TORI)
FAISSNER	70	NC 70A 57	H. Faissner <i>et al.</i>	(AACH3, CERN, RHEL)
GINSBERG	70	PR D1 229	E.S. Ginsberg	(HAIF)
MARX	70	PL 32B 219	J. Marx <i>et al.</i>	(COLU, HARV, CERN)
Also	70B	Thesis Nevis 179	J. Marx	(COLU)
SCRIBANO	70	PL 32B 224	A. Scribano <i>et al.</i>	(PISA, COLU, HARV)
SMITH	70	PL 32B 133	R.C. Smith <i>et al.</i>	(UMD, BNL)
WEBBER	70	PR D1 1967	B.R. Webber <i>et al.</i>	(LRL)
Also	69	Thesis UCRL 19226	B.R. Webber	(LRL)
BANNER	69	PR 188 2033	M. Banner <i>et al.</i>	(PRIN)
Also	68	PRL 21 1103	M. Banner <i>et al.</i>	(PRIN)
Also	68	PRL 21 1107	J.W. Cronin, J.K. Liu, J.E. Pilcher	(PRIN)
BEILLIERE	69	PL 30B 202	P. Beilliere, G. Boutang, J. Limon	(EPOL)
BENNETT	69	PL 29B 317	S. Bennett <i>et al.</i>	(COLU, BNL)
CENCE	69	PRL 22 1210	R.J. Cence <i>et al.</i>	(HAWA, LRL)
EVANS	69	PRL 23 427	G.R. Evans <i>et al.</i>	(EDIN, CERN)
FAISSNER	69	PL 30B 204	H. Faissner <i>et al.</i>	(AACH3, CERN, TORI)
FOETH	69	PL 30B 282	H. Foeth <i>et al.</i>	(AACH, CERN, TORI)
GAILLARD	69	NC 59A 453	J.M. Gaillard <i>et al.</i>	(CERN, RHEL, AACH)
Also	67	PRL 18 20	J.M. Gaillard <i>et al.</i>	(CERN, RHEL, AACH)
LITTENBERG	69	PRL 22 654	L.S. Littenberg <i>et al.</i>	(UCSD)
LONGO	69	PR 181 1808	M.J. Longo, K.K. Young, J.A. Helland	(MICH, UCLA)
PACIOTTI	69	Thesis UCRL 19446	M.A. Paciotti	(LRL)

SAAL	69	Thesis	H.J. Saal	(COLU)
ABRAMS	68B	PR 176 1603	R.J. Abrams <i>et al.</i>	(ILL)
ARNOLD	68B	PL 28B 56	R.G. Arnold <i>et al.</i>	(CERN, ORSAY)
ARONSON	68	PRL 20 287	S.H. Aronson, K.W. Chen	(PRIN)
Also	69	PR 175 1708	S.H. Aronson, K.W. Chen	(PRIN)
BARTLETT	68	PRL 21 558	D.F. Bartlett <i>et al.</i>	(PRIN)
BASILE	68	PL 26B 542	P. Basile <i>et al.</i>	(SACL)
BASILE	68B	PL 28B 58	P. Basile <i>et al.</i>	(SACL)
BENNETT	68	PL 27B 244	S. Bennett <i>et al.</i>	(COLU, CERN)
BLANPIED	68	PRL 21 1650	W.A. Blanpied <i>et al.</i>	(CASE, HARV, MCGI)
BOHM	68B	PL 27B 594	A. Bohm <i>et al.</i>	
BUDAGOV	68	NC 57A 182	I.A. Budagov <i>et al.</i>	(CERN, ORSAY, IPNP)
Also	68B	PL 28B 215	I.A. Budagov <i>et al.</i>	(CERN, ORSAY, EPOL)
JAMES	68	NP B8 365	F. James, H. Briand	(IPNP, CERN)
Also	68	PRL 21 257	J.A. Helland, M.J. Longo, K.K. Young	(UCLA, MICH)
KULYUKINA	68	JETP 26 20	L.A. Kulyukina <i>et al.</i>	(JINR)
		Translated from ZETF 53 29.		
KUNZ	68	Thesis PU-68-46	P.F. Kunz	(PRIN)
BENNETT	67	PRL 19 993	S. Bennett <i>et al.</i>	(COLU)
BOTT-...	67	PL 24B 194	M. Bott-Bodenhausen <i>et al.</i>	(CERN)
CRONIN	67	PRL 18 25	J.W. Cronin <i>et al.</i>	(PRIN)
Also	68	Thesis unpub.	Wheeler	(PRIN)
CRONIN	67B	Princeton 11/67	J.W. Cronin <i>et al.</i>	(PRIN)
DEBOUARD	67	NC 52A 662	X. de Bouard <i>et al.</i>	(CERN)
Also	65	PL 15 58	X. de Bouard <i>et al.</i>	(CERN, ORSAY, MPIM)
DEVLIN	67	PRL 18 54	T.J. Devlin <i>et al.</i>	(PRIN, UMD)
Also	68	PR 169 1045	G.A. Sayer <i>et al.</i>	(UMD, PPA, PRIN)
DORFAN	67	PRL 19 987	D.E. Dorfman <i>et al.</i>	(SLAC, LRL)
FELDMAN	67B	PR 155 1611	L. Feldman <i>et al.</i>	(PENN)
FIRESTONE	67	PRL 18 176	A. Firestone <i>et al.</i>	(YALE, BNL)
FITCH	67	PR 164 1711	V.L. Fitch <i>et al.</i>	(PRIN)
GINSBERG	67	PR 162 1570	E.S. Ginsberg	(MASB)
HAWKINS	67	PR 156 1444	C.J.B. Hawkins	(YALE)
HILL	67	PRL 19 668	D.G. Hill <i>et al.</i>	(BNL, CMU)
HOPKINS	67	PRL 19 185	H.W.K. Hopkins, T.C. Bacon, F.R. Eisler	(BNL)
KADYK	67	PRL 19 597	J.A. Kadyk <i>et al.</i>	(LRL)
KULYUKINA	67	Preprint	L.A. Kulyukina <i>et al.</i>	(JINR)
LOWYS	67	PL 24B 75	J.P. Lowys <i>et al.</i>	(EPOL, ORSAY)
NEFKENS	67	PR 157 1233	B.M.K. Nefkens <i>et al.</i>	(ILL)
SCHMIDT	67	Thesis Nevis 160	Schmidt	(COLU)
TODOROFF	67	Thesis	Todoroff	(ILL)
ALFF-...	66B	PL 21 595	C. Alff-Steinberger <i>et al.</i>	(CERN)
ANIKINA	66	SJNP 2 339	M.K. Anikina <i>et al.</i>	(JINR)
		Translated from YAF 2 471.		
AUERBACH	66B	PRL 17 980	L.B. Auerbach <i>et al.</i>	(PENN)
BASILE	66	Balaton Conf.	P. Basile <i>et al.</i>	(SACL)
BEHR	66	PL 22 540	L. Behr <i>et al.</i>	(EPOL, MILA, PADO, ORSAY)
BOTT-...	66	PL 23 277	M. Bott-Bodenhausen <i>et al.</i>	(CERN)
CARPENTER	66	PR 142 871	D.W. Carpenter <i>et al.</i>	(ILL)
CRIEGEE	66	PRL 17 150	L. Criegee <i>et al.</i>	(ILL)
HAWKINS	66	PL 21 238	C.J.B. Hawkins	(YALE)
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ANDERSON	65	PRL 14 475	J.A. Anderson <i>et al.</i>	(LRL, WISC)
ANIKINA	65	JINR P 2488	M.K. Anikina <i>et al.</i>	(JINR)
ASTBURY	65	PL 16 80	P. Astbury <i>et al.</i>	(CERN, ZURI)
Also	65	HPA 39 523	M. Pepin	
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Also	67	PL 24B 75	J.P. Lowys <i>et al.</i>	(EPOL, ORSAY)
BALDO-...	65	NC 38 684	M. Baldo-Ceolin <i>et al.</i>	(PADO)
FISHER	65	ANL 7130 83	G.P. Fisher <i>et al.</i>	(ILL)
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GUIDONI	65	Argonne Conf. 49	P. Guidoni <i>et al.</i>	(BNL, YALE)
HOPKINS	65	Argonne Conf. 67	H.W.K. Hopkins, T.C. Bacon, F. Eisler	(VAND+)
ADAIR	64	PL 12 67	R.K. Adair, L.B. Leipuner	(YALE, BNL)
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Also	64	JETP 19 1019	A.S. Aleksanyan <i>et al.</i>	(LEBD, MPEI, YERE)
		Translated from ZETF 46 1504.		
ANIKINA	64	JETP 19 42	M.K. Anikina <i>et al.</i>	(GEOR, JINR)
		Translated from ZETF 46 59.		

CHRISTENS...	64	PRL 13 138	J.H. Christenson <i>et al.</i>	(PRIN)
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