

K_L^0 – THIS IS PART 1 OF 4

To reduce the size of this section's PostScript file, we have divided it into four PostScript files. We present the following index:

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$$I(J^P) = \frac{1}{2}(0^-)$$

$$m_{K_L^0} - m_{K_S^0}$$

For earlier measurements, beginning with GOOD 61 and FITCH 61, see our 1986 edition, Physics Letters **170B** 132 (1986).

OUR FIT is described in the note on "Fits for K_L^0 CP-Violation Parameters" in the K_L^0 Particle Listings.

<u>VALUE ($10^{10} \hbar s^{-1}$)</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
0.5301 ± 0.0014	OUR FIT		
0.5311 ± 0.0019	OUR AVERAGE Error includes scale factor of 1.2.		
0.5274 ± 0.0029 ± 0.0005	¹ ADLER	95 CPLR	
0.5297 ± 0.0030 ± 0.0022	² SCHWINGEN...	95 E773	20–160 GeV <i>K</i> beams
0.5257 ± 0.0049 ± 0.0021	² GIBBONS	93C E731	20–160 GeV <i>K</i> beams
0.5340 ± 0.00255 ± 0.0015	³ GEWENIGER	74C SPEC	Gap method
0.5334 ± 0.0040 ± 0.0015	³ GJESDAL	74 SPEC	Charge asymmetry in $K_{\ell 3}^0$
0.542 ± 0.006	CULLEN	70 CNTR	
• • • We do not use the following data for averages, fits, limits, etc. • • •			
0.5307 ± 0.0013	⁴ ADLER	96C RVUE	
0.5286 ± 0.0028	⁵ GIBBONS	93 E731	20–160 GeV <i>K</i> beams
0.482 ± 0.014	⁶ ARONSON	82B SPEC	$E=30-110$ GeV
0.534 ± 0.007	⁷ CARNEGIE	71 ASPK	Gap method
0.542 ± 0.006	⁷ ARONSON	70 ASPK	Gap method

¹ ADLER 95 uses \bar{K}_{e3}^0 and K_{e3}^0 strangeness tagging at production and decay.

² Fits Δm and ϕ_{+-} simultaneously. GIBBONS 93C systematic error is from B. Winstein via private communication.

³ These two experiments have a common systematic error due to the uncertainty in the momentum scale, as pointed out in WAHL 89.

⁴ ADLER 96C is the result of a fit which includes nearly the same data as entered into the "OUR FIT" value above.

⁵ GIBBONS 93 value assume $\phi_{+-} = \phi_{00} = \phi_{SW} = (43.7 \pm 0.2)^\circ$.

⁶ ARONSON 82 find that Δm may depend on the kaon energy.

⁷ ARONSON 70 and CARNEGIE 71 use K_S^0 mean life = $(0.862 \pm 0.006) \times 10^{-10}$ s. We have not attempted to adjust these values for the subsequent change in the K_S^0 mean life or in η_{+-} .

K_L^0 MEAN LIFE

<u>VALUE (10^{-8} s)</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>
5.17 ± 0.04	OUR FIT Error includes scale factor of 1.1.		
5.15 ± 0.04	OUR AVERAGE		
5.154 ± 0.044	0.4M	VOSBURGH	72 CNTR
5.15 ± 0.14		DEVLIN	67 CNTR

••• We do not use the following data for averages, fits, limits, etc. •••

5.0	± 0.5		⁸ LOWYS	67	HLBC
6.1	$+1.5$ -1.2	1700	ASTBURY	65c	CNTR
5.3	± 0.6		FUJII	64	OSPK
5.1	$+2.4$ -1.3	15	DARMON	62	FBC
8.1	$+3.2$ -2.4	34	BARDON	58	CNTR

⁸Sum of partial decay rates.

K_L^0 DECAY MODES

Mode	Fraction (Γ_i/Γ)	Scale factor/ Confidence level
Γ_1 $3\pi^0$	(21.12 \pm 0.27) %	S=1.1
Γ_2 $\pi^+\pi^-\pi^0$	(12.56 \pm 0.20) %	S=1.7
Γ_3 $\pi^\pm\mu^\mp\nu$ Called $K_{\mu 3}^0$.	[a] (27.17 \pm 0.25) %	S=1.1
Γ_4 $\pi^-\mu^+\nu_\mu$		
Γ_5 $\pi^+\mu^-\bar{\nu}_\mu$		
Γ_6 $\pi^\pm e^\mp\nu_e$ Called $K_{e 3}^0$.	[a] (38.78 \pm 0.27) %	S=1.1
Γ_7 $\pi^-e^+\nu_e$		
Γ_8 $\pi^+e^-\bar{\nu}_e$		
Γ_9 2γ	(5.92 \pm 0.15) $\times 10^{-4}$	
Γ_{10} 3γ	< 2.4 $\times 10^{-7}$	CL=90%
Γ_{11} $\pi^0 2\gamma$	[b] (1.70 \pm 0.28) $\times 10^{-6}$	
Γ_{12} $\pi^0\pi^\pm e^\mp\nu$	[a] (5.18 \pm 0.29) $\times 10^{-5}$	
Γ_{13} $(\pi\mu\text{atom})\nu$	(1.06 \pm 0.11) $\times 10^{-7}$	
Γ_{14} $\pi^\pm e^\mp\nu_e\gamma$	[a,b,c] (3.62 $^{+0.26}_{-0.21}$) $\times 10^{-3}$	
Γ_{15} $\pi^+\pi^-\gamma$	[b,c] (4.61 \pm 0.14) $\times 10^{-5}$	
Γ_{16} $\pi^0\pi^0\gamma$	< 5.6 $\times 10^{-6}$	

Charge conjugation \times Parity (CP, CPV) or Lepton Family number (LF) violating modes, or $\Delta S = 1$ weak neutral current ($S1$) modes

Γ_{17} $\pi^+\pi^-$	CPV	(2.067 \pm 0.035) $\times 10^{-3}$	S=1.1
Γ_{18} $\pi^0\pi^0$	CPV	(9.36 \pm 0.20) $\times 10^{-4}$	
Γ_{19} $\mu^+\mu^-$	$S1$	(7.2 \pm 0.5) $\times 10^{-9}$	S=1.4
Γ_{20} $\mu^+\mu^-\gamma$	$S1$	(3.25 \pm 0.28) $\times 10^{-7}$	
Γ_{21} e^+e^-	$S1$	< 4.1 $\times 10^{-11}$	CL=90%
Γ_{22} $e^+e^-\gamma$	$S1$	(9.1 \pm 0.5) $\times 10^{-6}$	
Γ_{23} $e^+e^-\gamma\gamma$	$S1$ [b]	(6.5 \pm 1.2) $\times 10^{-7}$	

Γ_{24}	$\pi^+ \pi^- e^+ e^-$	<i>S1</i>	[b] < 4.6	$\times 10^{-7}$	CL=90%
Γ_{25}	$\mu^+ \mu^- e^+ e^-$	<i>S1</i>	(2.9 $\begin{smallmatrix} +6.7 \\ -2.4 \end{smallmatrix}$)	$\times 10^{-9}$	
Γ_{26}	$e^+ e^- e^+ e^-$	<i>S1</i>	(4.1 ± 0.8)	$\times 10^{-8}$	S=1.2
Γ_{27}	$\pi^0 \mu^+ \mu^-$	<i>CP,S1</i>	[d] < 5.1	$\times 10^{-9}$	CL=90%
Γ_{28}	$\pi^0 e^+ e^-$	<i>CP,S1</i>	[d] < 4.3	$\times 10^{-9}$	CL=90%
Γ_{29}	$\pi^0 \nu \bar{\nu}$	<i>CP,S1</i>	[e] < 5.8	$\times 10^{-5}$	CL=90%
Γ_{30}	$e^\pm \mu^\mp$	<i>LF</i>	[a] < 3.3	$\times 10^{-11}$	CL=90%
Γ_{31}	$e^\pm e^\pm \mu^\mp \mu^\mp$	<i>LF</i>	[a] < 6.1	$\times 10^{-9}$	CL=90%

[a] The value is for the sum of the charge states of particle/antiparticle states indicated.

[b] See the Particle Listings below for the energy limits used in this measurement.

[c] Most of this radiative mode, the low-momentum γ part, is also included in the parent mode listed without γ 's.

[d] Allowed by higher-order electroweak interactions.

[e] Violates *CP* in leading order. Test of direct *CP* violation since the indirect *CP*-violating and *CP*-conserving contributions are expected to be suppressed.

CONSTRAINED FIT INFORMATION

An overall fit to the mean life, 4 decay rate, and 12 branching ratios uses 46 measurements and one constraint to determine 8 parameters. The overall fit has a $\chi^2 = 41.2$ for 39 degrees of freedom.

The following *off-diagonal* array elements are the correlation coefficients $\langle \delta p_i \delta p_j \rangle / (\delta p_i \cdot \delta p_j)$, in percent, from the fit to parameters p_i , including the branching fractions, $x_i \equiv \Gamma_i / \Gamma_{\text{total}}$. The fit constrains the x_i whose labels appear in this array to sum to one.

x_2	-19						
x_3	-37	-28					
x_6	-49	-28	-36				
x_9	-8	22	-6	-5			
x_{17}	-12	35	-8	-8	64		
x_{18}	-10	27	-7	-6	84	77	
Γ	0	0	0	0	0	0	0
	x_1	x_2	x_3	x_6	x_9	x_{17}	x_{18}

	Mode	Rate (10^8 s^{-1})	Scale factor
Γ_1	$3\pi^0$	0.0408 ± 0.0006	
Γ_2	$\pi^+ \pi^- \pi^0$	0.0243 ± 0.0004	1.5
Γ_3	$\pi^\pm \mu^\mp \nu$ Called $K_{\mu 3}^0$.	[a] 0.0525 ± 0.0007	1.1
Γ_6	$\pi^\pm e^\mp \nu_e$ Called $K_{e 3}^0$.	[a] 0.0750 ± 0.0008	1.1
Γ_9	2γ	$(1.144 \pm 0.031) \times 10^{-4}$	
Γ_{17}	$\pi^+ \pi^-$	$(4.00 \pm 0.07) \times 10^{-4}$	1.1
Γ_{18}	$\pi^0 \pi^0$	$(1.81 \pm 0.04) \times 10^{-4}$	

K_L^0 DECAY RATES

$\Gamma(3\pi^0)$					Γ_1
<u>VALUE (10^6 s^{-1})</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>	
4.08 ± 0.06 OUR FIT					
$5.22^{+1.03}_{-0.84}$	54	BEHR	66 HLBC	Assumes CP	

$\Gamma(\pi^+\pi^-\pi^0)$
 Γ_2

<u>VALUE (10^6 s^{-1})</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
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2.43±0.04 OUR FIT Error includes scale factor of 1.5.

2.38±0.09 OUR AVERAGE

2.32 ^{+0.13} _{-0.15}	192	BALDO-...	75	HLBC	Assumes <i>CP</i>
2.35±0.20	180	⁹ JAMES	72	HBC	Assumes <i>CP</i>
2.71±0.28	99	CHO	71	DBC	Assumes <i>CP</i>
2.12±0.33	50	MEISNER	71	HBC	Assumes <i>CP</i>
2.20±0.35	53	WEBBER	70	HBC	Assumes <i>CP</i>
2.62 ^{+0.28} _{-0.27}	136	BEHR	66	HLBC	Assumes <i>CP</i>

• • • We do not use the following data for averages, fits, limits, etc. • • •

2.5 ±0.3	98	⁹ JAMES	71	HBC	Assumes <i>CP</i>
3.26±0.77	18	ANDERSON	65	HBC	
1.4 ±0.4	14	FRANZINI	65	HBC	

In the fit this rate is well determined by the mean life and the branching ratio $\Gamma(\pi^+\pi^-\pi^0)/[\Gamma(\pi^+\pi^-\pi^0) + \Gamma(\pi^\pm\mu^\mp\nu) + \Gamma(\pi^\pm e^\mp\nu_e)]$. For this reason the discrepancy between the $\Gamma(\pi^+\pi^-\pi^0)$ measurements does not affect the scale factor of the overall fit.

⁹JAMES 72 is a final measurement and includes JAMES 71.

 $\Gamma(\pi^\pm\mu^\mp\nu)$
 Γ_3

<u>VALUE (10^6 s^{-1})</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
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5.25±0.07 OUR FIT Error includes scale factor of 1.1.

• • • We do not use the following data for averages, fits, limits, etc. • • •

4.54 ^{+1.24} _{-1.08}	19	LOWYS	67	HLBC	
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 $\Gamma(\pi^\pm e^\mp\nu_e)$
 Γ_6

<u>VALUE (10^6 s^{-1})</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
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7.50±0.08 OUR FIT Error includes scale factor of 1.1.

7.7 ±0.5 OUR AVERAGE

7.81±0.56	620	CHAN	71	HBC	
7.52 ^{+0.85} _{-0.72}		AUBERT	65	HLBC	$\Delta S=\Delta Q, CP$ assumed

 $\Gamma(\pi^+\pi^-\pi^0) + \Gamma(\pi^\pm\mu^\mp\nu) + \Gamma(\pi^\pm e^\mp\nu_e)$
 $(\Gamma_2+\Gamma_3+\Gamma_6)$

$K_L^0 \rightarrow$ charged.

<u>VALUE (10^6 s^{-1})</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
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15.18±0.14 OUR FIT Error includes scale factor of 1.1.

• • • We do not use the following data for averages, fits, limits, etc. • • •

15.1 ±1.9	98	AUERBACH	66B	OSPK	
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$\Gamma(\pi^\pm \mu^\mp \nu) + \Gamma(\pi^\pm e^\mp \nu_e)$ $(\Gamma_3 + \Gamma_6)$

<u>VALUE</u> (10^6 s^{-1})	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
12.75 ± 0.12 OUR FIT	Error includes scale factor of 1.1.			
11.9 ± 0.6 OUR AVERAGE	Error includes scale factor of 1.2.			
12.4 ± 0.7	410	¹⁰ BURGUN	72 HBC	$K^+ p \rightarrow K^0 p \pi^+$
13.1 ± 1.3	252	¹⁰ WEBBER	71 HBC	$K^- p \rightarrow n \bar{K}^0$
11.6 ± 0.9	393	^{10,11} CHO	70 DBC	$K^+ n \rightarrow K^0 p$
9.85 ^{+1.15} _{-1.05}	109	¹⁰ FRANZINI	65 HBC	
• • • We do not use the following data for averages, fits, limits, etc. • • •				
8.47 ± 1.69	126	¹⁰ MANN	72 HBC	$K^- p \rightarrow n \bar{K}^0$
10.3 ± 0.8	335	¹¹ HILL	67 DBC	$K^+ n \rightarrow K^0 p$
¹⁰ Assumes $\Delta S = \Delta Q$ rule.				
¹¹ CHO 70 includes events of HILL 67.				

K_L^0 BRANCHING RATIOS

 $\Gamma(3\pi^0)/\Gamma_{\text{total}}$ Γ_1/Γ

<u>VALUE</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
0.2112 ± 0.0027 OUR FIT	Error includes scale factor of 1.1.			
0.2105 ± 0.0028	38k	¹² KREUTZ	95 NA31	
¹² KREUTZ 95 measure $3\pi^0$, $\pi^+ \pi^- \pi^0$, and $\pi e \nu_e$ modes. They assume PDG 1992 values for $\pi \mu \nu_\mu$, 2π , and 2γ modes.				

 $\Gamma(3\pi^0)/\Gamma(\pi^+ \pi^- \pi^0)$ Γ_1/Γ_2

<u>VALUE</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
1.68 ± 0.04 OUR FIT	Error includes scale factor of 1.3.			
1.63 ± 0.05 OUR AVERAGE	Error includes scale factor of 1.4.			
1.611 ± 0.014 ± 0.034	38k	¹³ KREUTZ	95 NA31	
1.80 ± 0.13	1010	BUDAGOV	68 HLBC	
2.0 ± 0.6	188	ALEKSANYAN	64B FBC	
• • • We do not use the following data for averages, fits, limits, etc. • • •				
1.65 ± 0.07	883	BARMIN	72B HLBC	Error statistical only
¹³ KREUTZ 95 excluded from fit because it is not independent of their $\Gamma(3\pi^0)/\Gamma_{\text{total}}$ measurement, which is in the fit.				

 $\Gamma(3\pi^0)/\Gamma(\pi^\pm e^\mp \nu_e)$ Γ_1/Γ_6

<u>VALUE</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
0.545 ± 0.009 OUR FIT	Error includes scale factor of 1.1.			
0.545 ± 0.004 ± 0.009	38k	¹⁴ KREUTZ	95 NA31	
¹⁴ KREUTZ 95 measurement excluded from fit because it is not independent of their $\Gamma(3\pi^0)/\Gamma_{\text{total}}$ measurement, which is in the fit.				

$$\frac{\Gamma(3\pi^0)}{[\Gamma(\pi^+\pi^-\pi^0) + \Gamma(\pi^\pm\mu^\mp\nu) + \Gamma(\pi^\pm e^\mp\nu_e)]} \quad \Gamma_1/(\Gamma_2+\Gamma_3+\Gamma_6)$$

<u>VALUE</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
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0.269±0.004 OUR FIT Error includes scale factor of 1.1.

0.260±0.011 OUR AVERAGE

0.251±0.014	549	BUDAGOV	68	HLBC	ORSAY measur.
0.277±0.021	444	BUDAGOV	68	HLBC	Ecole polytec.meas
0.31 ^{+0.07} _{-0.06}	29	KULYUKINA	68	CC	
0.24 ±0.08	24	ANIKINA	64	CC	

$$\frac{\Gamma(\pi^+\pi^-\pi^0)}{\Gamma_{\text{total}}} \quad \Gamma_2/\Gamma$$

<u>VALUE</u>	<u>DOCUMENT ID</u>
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0.1256±0.0020 OUR FIT Error includes scale factor of 1.7.

$$\frac{\Gamma(\pi^+\pi^-\pi^0)}{[\Gamma(\pi^+\pi^-\pi^0) + \Gamma(\pi^\pm\mu^\mp\nu) + \Gamma(\pi^\pm e^\mp\nu_e)]} \quad \Gamma_2/(\Gamma_2+\Gamma_3+\Gamma_6)$$

<u>VALUE</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
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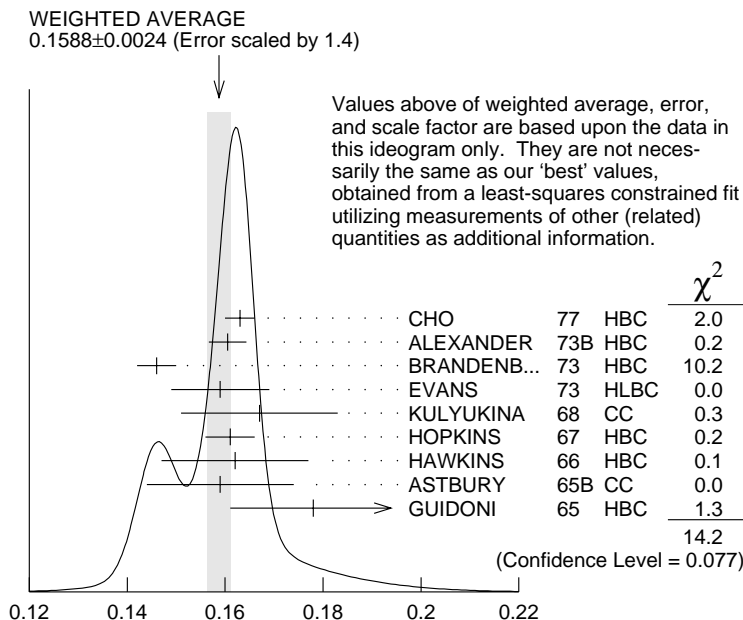
0.1600±0.0025 OUR FIT Error includes scale factor of 1.7.

0.1588±0.0024 OUR AVERAGE Error includes scale factor of 1.4. See the ideogram below.

0.163 ±0.003	6499	CHO	77	HBC	
0.1605±0.0038	1590	ALEXANDER	73B	HBC	
0.146 ±0.004	3200	BRANDENB...	73	HBC	
0.159 ±0.010	558	EVANS	73	HLBC	
0.167 ±0.016	1402	KULYUKINA	68	CC	
0.161 ±0.005		HOPKINS	67	HBC	
0.162 ±0.015	126	HAWKINS	66	HBC	
0.159 ±0.015	326	ASTBURY	65B	CC	
0.178 ±0.017	566	GUIDONI	65	HBC	

• • • We do not use the following data for averages, fits, limits, etc. • • •

0.15 ^{+0.03} _{-0.04}	66	ASTBURY	65	CC	
0.144 ±0.004	1729	HOPKINS	65	HBC	See HOPKINS 67
0.151 ±0.020	79	ADAIR	64	HBC	
0.157 ^{+0.03} _{-0.04}	75	LUERS	64	HBC	
0.185 ±0.038	59	ASTIER	61	CC	



$$\Gamma(\pi^+ \pi^- \pi^0) / [\Gamma(\pi^+ \pi^- \pi^0) + \Gamma(\pi^\pm \mu^\mp \nu) + \Gamma(\pi^\pm e^\mp \nu_e)]$$

$$\Gamma(\pi^+ \pi^- \pi^0) / \Gamma(\pi^\pm e^\mp \nu_e)$$

Γ_2/Γ_6

VALUE	EVTS	DOCUMENT ID	TECN
0.324±0.006 OUR FIT	Error includes scale factor of 1.6.		
0.336±0.003±0.007	28k	KREUTZ	95 NA31

$$\Gamma(\pi^\pm \mu^\mp \nu) / \Gamma(\pi^\pm e^\mp \nu_e)$$

Γ_3/Γ_6

VALUE	EVTS	DOCUMENT ID	TECN	COMMENT
0.701±0.009 OUR FIT				
0.697±0.010 OUR AVERAGE				
0.702±0.011	33k	CHO	80	HBC
0.662±0.037	10k	WILLIAMS	74	ASPK
0.741±0.044	6700	BRANDENB...	73	HBC
0.662±0.030	1309	EVANS	73	HLBC
0.71 ±0.05	770	BUDAGOV	68	HLBC

• • • We do not use the following data for averages, fits, limits, etc. • • •

0.68 ±0.08	3548	BASILE	70	OSPK
0.71 ±0.04	569	¹⁵ BEILLIERE	69	HLBC
0.648±0.030	1309	EVANS	69	HLBC Repl. by EVANS 73
0.67 ±0.13		¹⁶ KULYUKINA	68	CC
0.82 ±0.10		DEBOUARD	67	OSPK
0.7 ±0.2	273	HAWKINS	67	HBC
0.81 ±0.08		HOPKINS	67	HBC
0.81 ±0.19		ADAIR	64	HBC

¹⁵BEILLIERE 69 is a scanning experiment using same exposure as BUDAGOV 68.

¹⁶KULYUKINA 68 $\Gamma(\pi^\pm \mu^\mp \nu)/\Gamma(\pi^\pm e^\mp \nu_e)$ is not measured independently from $\Gamma(\pi^+ \pi^- \pi^0)/[\Gamma(\pi^+ \pi^- \pi^0) + \Gamma(\pi^\pm \mu^\mp \nu) + \Gamma(\pi^\pm e^\mp \nu_e)]$ and $\Gamma(\pi^\pm e^\mp \nu_e)/[\Gamma(\pi^+ \pi^- \pi^0) + \Gamma(\pi^\pm \mu^\mp \nu) + \Gamma(\pi^\pm e^\mp \nu_e)]$.

$$\Gamma(\pi^\pm \mu^\mp \nu)/[\Gamma(\pi^+ \pi^- \pi^0) + \Gamma(\pi^\pm \mu^\mp \nu) + \Gamma(\pi^\pm e^\mp \nu_e)] \quad \Gamma_3/(\Gamma_2+\Gamma_3+\Gamma_6)$$

VALUE EVTS DOCUMENT ID TECN

0.3461±0.0030 OUR FIT Error includes scale factor of 1.1.

• • • We do not use the following data for averages, fits, limits, etc. • • •

0.335 ±0.055	330	¹⁷ KULYUKINA 68	CC
0.39 +0.08 -0.10	172	¹⁷ ASTBURY 65	CC
0.356 ±0.07	251	¹⁷ LUERS 64	HBC

¹⁷This mode not measured independently from $\Gamma(\pi^+ \pi^- \pi^0)/[\Gamma(\pi^+ \pi^- \pi^0) + \Gamma(\pi^\pm \mu^\mp \nu) + \Gamma(\pi^\pm e^\mp \nu_e)]$ and $\Gamma(\pi^\pm e^\mp \nu_e)/[\Gamma(\pi^+ \pi^- \pi^0) + \Gamma(\pi^\pm \mu^\mp \nu) + \Gamma(\pi^\pm e^\mp \nu_e)]$.

$$\Gamma(\pi^\pm e^\mp \nu_e)/[\Gamma(\pi^+ \pi^- \pi^0) + \Gamma(\pi^\pm \mu^\mp \nu) + \Gamma(\pi^\pm e^\mp \nu_e)] \quad \Gamma_6/(\Gamma_2+\Gamma_3+\Gamma_6)$$

VALUE EVTS DOCUMENT ID TECN

0.4939±0.0030 OUR FIT Error includes scale factor of 1.1.

• • • We do not use the following data for averages, fits, limits, etc. • • •

0.498 ±0.052	500	KULYUKINA 68	CC
0.46 +0.08 -0.10	202	ASTBURY 65	CC
0.487 ±0.05	153	LUERS 64	HBC
0.46 ±0.11	24	NYAGU 61	CC

$$\Gamma(\pi^\pm e^\mp \nu_e)/[\Gamma(\pi^\pm \mu^\mp \nu) + \Gamma(\pi^\pm e^\mp \nu_e)] \quad \Gamma_6/(\Gamma_3+\Gamma_6)$$

VALUE EVTS DOCUMENT ID TECN

0.5880±0.0033 OUR FIT

• • • We do not use the following data for averages, fits, limits, etc. • • •

0.415 ±0.120	320	ASTIER 61	CC
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$$[\Gamma(\pi^\pm \mu^\mp \nu) + \Gamma(\pi^\pm e^\mp \nu_e)]/\Gamma_{\text{total}} \quad (\Gamma_3+\Gamma_6)/\Gamma$$

VALUE DOCUMENT ID

0.6596±0.0030 OUR FIT Error includes scale factor of 1.2.

$$\Gamma(2\gamma)/\Gamma_{\text{total}} \quad \Gamma_9/\Gamma$$

VALUE (units 10⁻⁴) EVTS DOCUMENT ID TECN COMMENT

5.92±0.15 OUR FIT

• • • We do not use the following data for averages, fits, limits, etc. • • •

4.54±0.84		¹⁸ BANNER 72B	OSPK
4.5 ±1.0	23	ENSTROM 71	OSPK K_L^0 1.5–9 GeV/c
5.0 ±1.0		¹⁹ REPELLIN 71	OSPK
5.5 ±1.1	90	KUNZ 68	OSPK Norm.to 3 $\pi(C+N)$
7.4 ±1.6	33	²⁰ CRONIN 67	OSPK
6.7 ±2.2	32	TODOROFF 67	OSPK Repl. CRIEGEE 66
1.3 ±0.6		²¹ CRIEGEE 66	OSPK

¹⁸ This value uses $(\eta_{00}/\eta_{+-})^2 = 1.05 \pm 0.14$. In general, $\Gamma(2\gamma)/\Gamma_{\text{total}} = [(4.32 \pm 0.55) \times 10^{-4}] [(\eta_{00}/\eta_{+-})^2]$.

¹⁹ Assumes regeneration amplitude in copper at 2 GeV is 22 mb. To evaluate for a given regeneration amplitude and error, multiply by $(\text{regeneration amplitude}/22\text{mb})^2$.

²⁰ CRONIN 67 replaced by KUNZ 68.

²¹ CRIEGEE 66 replaced by TODOROFF 67.

$\Gamma(2\gamma)/\Gamma(3\pi^0)$

Γ_9/Γ_1

VALUE (units 10^{-3})	EVTS	DOCUMENT ID	TECN	COMMENT
2.80 ± 0.08 OUR FIT				Error includes scale factor of 1.1.

• • • We do not use the following data for averages, fits, limits, etc. • • •

2.13 ± 0.43	28	BARMIN	71	HLBC	
2.24 ± 0.28	115	BANNER	69	OSPK	
2.5 ± 0.7	16	ARNOLD	68B	HLBC	Vacuum decay

$\Gamma(2\gamma)/\Gamma(\pi^0\pi^0)$

Γ_9/Γ_{18}

VALUE	EVTS	DOCUMENT ID	TECN	COMMENT
0.632 ± 0.009 OUR FIT				
0.632 ± 0.004 ± 0.008	110k	BURKHARDT	87	NA31

$\Gamma(3\gamma)/\Gamma_{\text{total}}$

Γ_{10}/Γ

VALUE	CL%	DOCUMENT ID	TECN	COMMENT
< 2.4 × 10⁻⁷	90	²² BARR	95C	NA31

²² Assumes a phase-space decay distribution.

$\Gamma(\pi^0 2\gamma)/\Gamma_{\text{total}}$

Γ_{11}/Γ

VALUE (units 10^{-6})	CL%	EVTS	DOCUMENT ID	TECN	COMMENT
1.7 ± 0.2 ± 0.2		63	²³ BARR	92	SPEC

• • • We do not use the following data for averages, fits, limits, etc. • • •

1.86 ± 0.60 ± 0.60		60	PAPADIMITR...91	E731	$m_{\gamma\gamma} > 280$ MeV
< 5.1	90		PAPADIMITR...91	E731	$m_{\gamma\gamma} < 264$ MeV
2.1 ± 0.6		14	²⁴ BARR	90C	NA31 $m_{\gamma\gamma} > 280$ MeV
< 2.7	90		PAPADIMITR...89	E731	In PAPADI...91
< 230	90	0	BANNER	69	OSPK

²³ BARR 92 find that $\Gamma(\pi^0 2\gamma, m_{\gamma\gamma} < 240 \text{ MeV})/\Gamma(\pi^0 2\gamma) < 0.09$ (90% CL).

²⁴ BARR 90C superseded by BARR 92.

$\Gamma(\pi^0\pi^\pm e^\mp\nu)/\Gamma_{\text{total}}$

Γ_{12}/Γ

VALUE (units 10^{-5})	CL%	EVTS	DOCUMENT ID	TECN	COMMENT
5.18 ± 0.29 OUR AVERAGE					

5.16 ± 0.20 ± 0.22		729	MAKOFF	93	E731
6.2 ± 2.0		16	CARROLL	80C	SPEC

• • • We do not use the following data for averages, fits, limits, etc. • • •

< 220	90		²⁵ DONALDSON	74	SPEC
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²⁵ DONALDSON 74 uses $K_L^0 \rightarrow \pi^+\pi^-\pi^0$ /(all K_L^0) decays = 0.126.

$\Gamma((\pi\mu\text{atom})\nu)/\Gamma(\pi^\pm\mu^\mp\nu)$
 Γ_{13}/Γ_3

VALUE (units 10^{-7})	EVTS	DOCUMENT ID	TECN
3.90 ± 0.39	155	²⁶ ARONSON	86 SPEC

• • • We do not use the following data for averages, fits, limits, etc. • • •

seen 18 COOMBES 76 WIRE

²⁶ ARONSON 86 quote theoretical value of $(4.31 \pm 0.08) \times 10^{-7}$.

 $\Gamma(\pi^\pm e^\mp\nu_e\gamma)/\Gamma(\pi^\pm e^\mp\nu_e)$
 Γ_{14}/Γ_6

VALUE (units 10^{-2})	EVTS	DOCUMENT ID	TECN	COMMENT
0.934 ± 0.036 ^{+0.055} _{-0.039}	1384	LEBER	96 NA31	$E_\gamma^* \geq 30$ MeV, $\theta_{e\gamma}^* \geq 20^\circ$

• • • We do not use the following data for averages, fits, limits, etc. • • •

3.3 ± 2.0 10 PEACH 71 HLBC γ KE >15 MeV

 $\Gamma(\pi^+\pi^-\gamma)/\Gamma_{\text{total}}$
 Γ_{15}/Γ

For earlier limits see our 1992 edition Physical Review **D45**, 1 June, Part II (1992).

VALUE (units 10^{-5})	EVTS	DOCUMENT ID	TECN	COMMENT
4.61 ± 0.14 OUR AVERAGE				
4.66 ± 0.15	3136	²⁷ RAMBERG	93 E731	$E_\gamma > 20$ MeV
4.41 ± 0.32	1062	²⁸ CARROLL	80B SPEC	$E_\gamma > 20$ MeV

• • • We do not use the following data for averages, fits, limits, etc. • • •

1.52 ± 0.16 516 ²⁹ CARROLL 80B SPEC $E_\gamma > 20$ MeV

2.89 ± 0.28 546 ³⁰ CARROLL 80B SPEC

6.2 ± 2.1 24 ³¹ DONALDSON 74C SPEC

²⁷ RAMBERG 93 finds that fraction of Direct Emission (DE) decays with $E_\gamma > 20$ MeV is 0.685 ± 0.041 .

²⁸ Both components. Uses $K_L^0 \rightarrow \pi^+\pi^-\pi^0$ /(all K_L^0) decays = 0.1239.

²⁹ Internal Bremsstrahlung component only.

³⁰ Direct γ emission component only.

³¹ Uses $K_L^0 \rightarrow \pi^+\pi^-\pi^0$ /(all K_L^0) decays = 0.126.

 $\Gamma(\pi^0\pi^0\gamma)/\Gamma_{\text{total}}$
 Γ_{16}/Γ

VALUE (units 10^{-6})	CL%	EVTS	DOCUMENT ID	TECN
< 5.6			BARR	94 NA31

• • • We do not use the following data for averages, fits, limits, etc. • • •

<230 90 0 ROBERTS 94 E799

 $\Gamma(\pi^+\pi^-)/\Gamma_{\text{total}}$
 Γ_{17}/Γ

Violates *CP* conservation.

VALUE (units 10^{-3})	DOCUMENT ID
2.067 ± 0.035 OUR FIT	Error includes scale factor of 1.1.
2.107 ± 0.055	³² ETAFIT 98

³² This ETAFIT value is computed from fitted values of $|\eta_{+-}|$, the K_L^0 and K_S^0 lifetimes, and the $K_S^0 \rightarrow \pi^+\pi^-$ branching fraction. See the discussion in the note "Fits for K_L^0 *CP*-Violation Parameters."

$$\Gamma(\pi^+\pi^-)/\Gamma(\pi^+\pi^-\pi^0) \qquad \Gamma_{17}/\Gamma_2$$

 Violates CP conservation.

<u>VALUE (units 10^{-2})</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
1.645±0.030 OUR FIT		Error includes scale factor of 1.1.		
1.64 ±0.04	4200	MESSNER	73 ASPK	$\eta_{+-} = 2.23$

$$\Gamma(\pi^+\pi^-)/[\Gamma(\pi^\pm\mu^\mp\nu) + \Gamma(\pi^\pm e^\mp\nu_e)] \qquad \Gamma_{17}/(\Gamma_3+\Gamma_6)$$

 Violates CP conservation.

<u>VALUE (units 10^{-3})</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
3.13±0.06 OUR FIT		Error includes scale factor of 1.1.		
3.08±0.10 OUR AVERAGE				
3.13±0.14	1687	COUPAL	85 SPEC	$\eta_{+-}=2.28 \pm 0.06$
3.04±0.14	2703	DEVOE	77 SPEC	$\eta_{+-}=2.25 \pm 0.05$

• • • We do not use the following data for averages, fits, limits, etc. • • •

2.51±0.23	309	³³ DEBOUARD	67 OSPK	$\eta_{+-}=2.00 \pm 0.09$
2.35±0.19	525	³³ FITCH	67 OSPK	$\eta_{+-}=1.94 \pm 0.08$

³³ Old experiments excluded from fit. See subsection on η_{+-} in section on "PARAMETERS FOR $K_L^0 \rightarrow 2\pi$ DECAY" below for average η_{+-} of these experiments and for note on discrepancy.

$$\Gamma(\pi^+\pi^-)/[\Gamma(\pi^+\pi^-\pi^0) + \Gamma(\pi^\pm\mu^\mp\nu) + \Gamma(\pi^\pm e^\mp\nu_e)] \qquad \Gamma_{17}/(\Gamma_2+\Gamma_3+\Gamma_6)$$

 Violates CP conservation.

<u>VALUE (units 10^{-3})</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
2.63 ±0.04 OUR FIT				
• • • We do not use the following data for averages, fits, limits, etc. • • •				
2.60 ±0.07	4200	³⁴ MESSNER	73 ASPK	$\eta_{+-} = 2.23 \pm 0.05$
1.93 ±0.26		³⁵ BASILE	66 OSPK	$\eta_{+-} = 1.92 \pm 0.13$
1.993±0.080		³⁵ BOTT-...	66 OSPK	$\eta_{+-} = 1.95 \pm 0.04$
2.08 ±0.35	54	³⁵ GALBRAITH	65 OSPK	$\eta_{+-} = 1.99 \pm 0.16$
2.0 ±0.4	45	³⁵ CHRISTENS...	64 OSPK	$\eta_{+-} = 1.95 \pm 0.20$

³⁴ From same data as $\Gamma(\pi^+\pi^-)/\Gamma(\pi^+\pi^-\pi^0)$ MESSNER 73, but with different normalization.

³⁵ Old experiments excluded from fit. See subsection on η_{+-} in section on "PARAMETERS FOR $K_L^0 \rightarrow 2\pi$ DECAY" below for average η_{+-} .

$$\Gamma(\pi^0\pi^0)/\Gamma_{\text{total}} \qquad \Gamma_{18}/\Gamma$$

 Violates CP conservation.

<u>VALUE (units 10^{-3})</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
0.936±0.020 OUR FIT				
• • • We do not use the following data for averages, fits, limits, etc. • • •				
2.5 ±0.8	189	³⁶ GAILLARD	69 OSPK	$\eta_{00}=3.6 \pm 0.6$
1.2 $\begin{smallmatrix} +1.5 \\ -1.2 \end{smallmatrix}$	7	³⁷ CRIEGEE	66 OSPK	

³⁶ Latest result of this experiment given by FAISSNER 70 $\Gamma(\pi^0\pi^0)/\Gamma(3\pi^0)$.

³⁷ CRIEGEE 66 experiment not designed to measure $2\pi^0$ decay mode.

$\Gamma(\pi^0\pi^0)/\Gamma(3\pi^0)$
 Γ_{18}/Γ_1

 Violates *CP* conservation.

<u>VALUE (units 10⁻²)</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
0.443±0.012 OUR FIT				Error includes scale factor of 1.1.
0.39 ±0.06 OUR AVERAGE				
0.37 ±0.08	29	BARMIN	70 HLBC	$\eta_{00}=2.02 \pm 0.23$
0.32 ±0.15	30	BUDAGOV	70 HLBC	$\eta_{00}=1.9 \pm 0.5$
0.46 ±0.11	57	BANNER	69 OSPK	$\eta_{00}=2.2 \pm 0.3$
not seen		BARTLETT	68 OSPK	See η_{00} below
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●				
1.21 ±0.30	150	³⁸ REY	76 OSPK	$\eta_{00}=3.8 \pm 0.5$
0.90 ±0.30	172	³⁹ FAISSNER	70 OSPK	$\eta_{00}=3.2 \pm 0.5$
1.31 ±0.31	133	³⁸ CENCE	69 OSPK	$\eta_{00}=3.7 \pm 0.5$
1.89 ±0.31	109	⁴⁰ CRONIN	67 OSPK	$\eta_{00}=4.9 \pm 0.5$
1.36 ±0.18		⁴⁰ CRONIN	67B OSPK	$\eta_{00}=3.92 \pm 0.3$

³⁸ CENCE 69 events are included in REY 76.

³⁹ FAISSNER 70 contains same $2\pi^0$ events as GAILLARD 69 $\Gamma(\pi^0\pi^0)/\Gamma_{\text{total}}$.

⁴⁰ CRONIN 67B is further analysis of CRONIN 67, now both withdrawn.

 $\Gamma(\pi^0\pi^0)/\Gamma(\pi^+\pi^-)$
 Γ_{18}/Γ_{17}

 Violates *CP* conservation.

<u>VALUE</u>	<u>DOCUMENT ID</u>
0.453 ±0.006 OUR FIT	
0.4535±0.0063	⁴¹ ETAFIT 98

⁴¹ This ETAFIT value is computed from fitted values of $|\eta_{00} / \eta_{+-}|$ and the $\Gamma(K_S^0 \rightarrow \pi^+\pi^-) / \Gamma(K_S^0 \rightarrow \pi^0\pi^0)$ branching fraction. See the discussion in the note "Fits for K_L^0 *CP*-Violation Parameters."

 $\Gamma(\mu^+\mu^-)/[\Gamma(\pi^+\pi^-\pi^0) + \Gamma(\pi^\pm\mu^\mp\nu) + \Gamma(\pi^\pm e^\mp\nu_e)]$
 $\Gamma_{19}/(\Gamma_2+\Gamma_3+\Gamma_6)$

 Test for $\Delta S = 1$ weak neutral current. Allowed by higher-order electroweak interaction.

<u>VALUE (units 10⁻⁶)</u>	<u>CL%</u>	<u>DOCUMENT ID</u>	<u>TECN</u>
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●			
< 2.0	90	BOTT-...	67 OSPK
< 35.0	90	FITCH	67 OSPK
<250.0	90	ALFF-...	66B OSPK
<100.0		ANIKINA	65 CC

 $\Gamma(\mu^+\mu^-)/\Gamma(\pi^+\pi^-)$
 Γ_{19}/Γ_{17}

 Test for $\Delta S = 1$ weak neutral current. Allowed by higher-order electroweak interaction.

<u>VALUE (units 10⁻⁶)</u>	<u>CL%</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
3.50±0.21 OUR AVERAGE					Error includes scale factor of 1.4.
3.87±0.30		179	⁴² AKAGI	95 SPEC	
3.38±0.17		707	HEINSON	95 B791	

• • • We do not use the following data for averages, fits, limits, etc. • • •

$3.9 \pm 0.3 \pm 0.1$	178	⁴³ AKAGI	91B SPEC	In AKAGI 95
$3.45 \pm 0.18 \pm 0.13$	368	⁴⁴ HEINSON	91 SPEC	In HEINSON 95
4.1 ± 0.5	54	INAGAKI	89 SPEC	In AKAGI 91B
$2.8 \pm 0.3 \pm 0.2$	87	MATHIAZHA...	89B SPEC	In HEINSON 91
$4.0 \begin{smallmatrix} +1.4 \\ -0.9 \end{smallmatrix}$	15	SHOCHET	79 SPEC	
$4.2 \begin{smallmatrix} +5.1 \\ -2.6 \end{smallmatrix}$	3	⁴⁵ FUKUSHIMA	76 SPEC	
$5.8 \begin{smallmatrix} +2.3 \\ -1.5 \end{smallmatrix}$	9	⁴⁶ CARITHERS	73 SPEC	
< 1.53	90	0	⁴⁷ CLARK	71 SPEC
< 18.	90	0	DARRIULAT	70 SPEC
< 140.	90	0	FOETH	69 SPEC

⁴² AKAGI 95 gives this number multiplied by the PDG 1992 average for $\Gamma(K_L^0 \rightarrow \pi^+ \pi^-) / \Gamma(\text{total})$.

⁴³ AKAGI 91B give this number multiplied by the 1990 PDG average for $\Gamma(K_L^0 \rightarrow \pi^+ \pi^-) / \Gamma(\text{total})$.

⁴⁴ HEINSON 91 give $\Gamma(K_L^0 \rightarrow \mu\mu) / \Gamma_{\text{total}}$. We divide out the $\Gamma(K_L^0 \rightarrow \pi^+ \pi^-) / \Gamma_{\text{total}}$ PDG average which they used.

⁴⁵ FUKUSHIMA 76 errors are at CL = 90%.

⁴⁶ CARITHERS 73 errors are at CL = 68%, W.Carithers, (private communication 79).

⁴⁷ CLARK 71 limit raised from 1.2×10^{-6} by FIELD 74 reanalysis. Not in agreement with subsequent experiments. So not averaged.

$\Gamma(\mu^+ \mu^- \gamma) / \Gamma_{\text{total}}$

Γ_{20} / Γ

Test for $\Delta S = 1$ weak neutral current. Allowed by higher-order electroweak interaction.

VALUE (units 10^{-7})	CL%	EVTS	DOCUMENT ID	TECN
3.25 ± 0.28 OUR AVERAGE				
$3.4 \pm 0.6 \pm 0.4$		45	FANTI	97 NA48
$3.23 \pm 0.23 \pm 0.19$		197	SPENCER	95 E799

• • • We do not use the following data for averages, fits, limits, etc. • • •

2.8 ± 2.8		1	⁴⁸ CARROLL	80D SPEC
< 78.1	90		⁴⁹ DONALDSON	74 SPEC

⁴⁸ Uses $K_L^0 \rightarrow \pi^+ \pi^- \pi^0 / (\text{all } K_L^0)$ decays = 0.1239.

⁴⁹ Uses $K_L^0 \rightarrow \pi^+ \pi^- \pi^0 / (\text{all } K_L^0)$ decays = 0.126.

$\Gamma(e^+ e^-) / \Gamma_{\text{total}}$

Γ_{21} / Γ

Test for $\Delta S = 1$ weak neutral current. Allowed by higher-order electroweak interaction.

VALUE (units 10^{-10})	CL%	EVTS	DOCUMENT ID	TECN	COMMENT
< 0.41	90	0	⁵⁰ ARISAKA	93B B791	

• • • We do not use the following data for averages, fits, limits, etc. • • •

< 1.6	90	1	AKAGI	95 SPEC	
< 1.6	90	1	AKAGI	91 SPEC	Sup. by AKAGI 95
< 5.6	90		INAGAKI	89 SPEC	In AKAGI 91
< 3.2	90		MATHIAZHA...	89 SPEC	In ARISAKA 93B
< 110	90		COUSINS	88 SPEC	
< 45	90		GREENLEE	88 SPEC	Repl. by JASTRZEMB-SKI 88
< 12	90		JASTRZEM...	88 SPEC	
< 15.7	90		⁵¹ CLARK	71 ASPK	
< 1500	90	0	FOETH	69 ASPK	

⁵⁰ ARISAKA 93B includes all events with <6 MeV radiated energy.

⁵¹ Possible (but unknown) systematic errors. See note on CLARK 71 $\Gamma(\mu^+ \mu^-)/\Gamma(\pi^+ \pi^-)$ entry.

$$\Gamma(e^+ e^-)/[\Gamma(\pi^+ \pi^- \pi^0) + \Gamma(\pi^\pm \mu^\mp \nu) + \Gamma(\pi^\pm e^\mp \nu_e)] \quad \Gamma_{21}/(\Gamma_2 + \Gamma_3 + \Gamma_6)$$

Test for $\Delta S = 1$ weak neutral current. Allowed by higher-order electroweak interaction.

<u>VALUE (units 10^{-6})</u>	<u>CL%</u>	<u>DOCUMENT ID</u>	<u>TECN</u>
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• • • We do not use the following data for averages, fits, limits, etc. • • •

< 23.0	90	BOTT-...	67 OSPK
< 200.0	90	ALFF-...	66B OSPK
<1000.0		ANIKINA	65 CC

$$\Gamma(e^+ e^- \gamma)/\Gamma_{\text{total}} \quad \Gamma_{22}/\Gamma$$

Test for $\Delta S = 1$ weak neutral current. Allowed by higher-order electroweak interaction.

<u>VALUE (units 10^{-6})</u>	<u>CL%</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>
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9.1 ± 0.5 OUR AVERAGE

9.2 ± 0.5 ± 0.5	1053	BARR	90B NA31
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9.1 ± 0.4 ^{+0.6} _{-0.5}	919	OHL	90B B845
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• • • We do not use the following data for averages, fits, limits, etc. • • •

17.4 ± 8.7	4	⁵² CARROLL	80D SPEC
<27	90	⁵³ BARMIN	72 HLBC

⁵² Uses $K_L^0 \rightarrow \pi^+ \pi^- \pi^0$ / (all K_L^0) decays = 0.1239.

⁵³ Uses $K_L^0 \rightarrow 3\pi^0$ / total = 0.214.

$$\Gamma(e^+ e^- \gamma \gamma)/\Gamma_{\text{total}} \quad \Gamma_{23}/\Gamma$$

Test for $\Delta S = 1$ weak neutral current. Allowed by higher-order electroweak interaction.

<u>VALUE (units 10^{-7})</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
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6.5 ± 1.2 OUR AVERAGE

6.5 ± 1.2 ± 0.6	58	NAKAYA	94 E799	$E_\gamma > 5$ MeV
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6.6 ± 3.2		MORSE	92 B845	$E_\gamma > 5$ MeV
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$$\Gamma(\pi^+ \pi^- e^+ e^-)/\Gamma_{\text{total}} \quad \Gamma_{24}/\Gamma$$

Test for $\Delta S = 1$ weak neutral current. Allowed by higher-order electroweak interaction.

<u>VALUE (units 10^{-7})</u>	<u>CL%</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
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< 4.6	90		NOMURA	97 SPEC	$m_{ee} > 4$ MeV
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• • • We do not use the following data for averages, fits, limits, etc. • • •

< 25	90	0	BALATS	83 SPEC
< 88.1	90	⁵⁴	DONALDSON	76 SPEC
<300			ANIKINA	73 STRC

⁵⁴ Uses $K_L^0 \rightarrow \pi^+ \pi^- \pi^0$ / (all K_L^0) decays = 0.126.

$$\Gamma(\mu^+ \mu^- e^+ e^-)/\Gamma_{\text{total}} \quad \Gamma_{25}/\Gamma$$

Test for $\Delta S = 1$ weak neutral current. Allowed by higher-order electroweak interaction.

<u>VALUE (units 10^{-9})</u>	<u>CL%</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>
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2.9^{+6.7}_{-2.4}		1	GU	96 E799
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• • • We do not use the following data for averages, fits, limits, etc. • • •

<4900	90		BALATS	83 SPEC
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$\Gamma(e^+e^-e^+e^-)/\Gamma_{\text{total}}$ Γ_{26}/Γ

 Test for $\Delta S = 1$ weak neutral current. Allowed by higher-order electroweak interaction.

VALUE (units 10^{-8})	CL%	EVTS	DOCUMENT ID	TECN	COMMENT
4.1 ± 0.8		OUR AVERAGE	Error includes scale factor of 1.2.		
6 ± 2 ± 1		18	⁵⁵ AKAGI	95 SPEC	$m_{ee} > 470$ MeV
10.4 ± 3.7 ± 1.1		8	⁵⁶ BARR	95 NA31	
3.96 ± 0.78 ± 0.32		27	GU	94 E799	
3.07 ± 1.25 ± 0.26		6	VAGINS	93 B845	
• • • We do not use the following data for averages, fits, limits, etc. • • •					
7 ± 3 ± 2		6	⁵⁵ AKAGI	95 SPEC	$m_{ee} > 470$ MeV
6 ± 2 ± 1		18	AKAGI	93 CNTR	Sup. by AKAGI 95
4 ± 3		2	BARR	91 NA31	Sup. by BARR 95
< 260	90		BALATS	83 SPEC	

⁵⁵ Values are for the total branching fraction, acceptance-corrected for the m_{ee} cuts shown.

⁵⁶ Distribution of angles between two e^+e^- pair planes favors $CP = -1$ for K_L^0 .

 $\Gamma(\pi^0\mu^+\mu^-)/\Gamma_{\text{total}}$ Γ_{27}/Γ

 Violates CP in leading order. Test for $\Delta S = 1$ weak neutral current. Allowed by higher-order electroweak interaction.

VALUE (units 10^{-9})	CL%	EVTS	DOCUMENT ID	TECN
< 5.1	90	0	HARRIS	93 E799
• • • We do not use the following data for averages, fits, limits, etc. • • •				
< 1200	90	0	⁵⁷ CARROLL	80D SPEC
< 56600	90		⁵⁸ DONALDSON	74 SPEC

⁵⁷ Uses $K_L^0 \rightarrow \pi^+\pi^-\pi^0$ / (all K_L^0) decays = 0.1239.

⁵⁸ Uses $K_L^0 \rightarrow \pi^+\pi^-\pi^0$ / (all K_L^0) decays = 0.126.

 $\Gamma(\pi^0e^+e^-)/\Gamma_{\text{total}}$ Γ_{28}/Γ

 Violates CP in leading order. Direct and indirect CP -violating contributions are expected to be comparable and to dominate the CP -conserving part. Test for $\Delta S = 1$ weak neutral current. Allowed by higher-order electroweak interaction.

VALUE (units 10^{-9})	CL%	EVTS	DOCUMENT ID	TECN
< 4.3	90	0	HARRIS	93B E799
< 7.5	90	0	BARKER	90 E731
< 5.5	90	0	OHL	90 B845
• • • We do not use the following data for averages, fits, limits, etc. • • •				
< 40	90		BARR	88 NA31
< 320	90		JASTRZEM...	88 SPEC
< 2300	90	0	⁵⁹ CARROLL	80D SPEC

⁵⁹ Uses $K_L^0 \rightarrow \pi^+\pi^-\pi^0$ / (all K_L^0) decays = 0.1239.

 $\Gamma(\pi^0\nu\bar{\nu})/\Gamma_{\text{total}}$ Γ_{29}/Γ

 Violates CP in leading order. Test of direct CP violation since the indirect CP -violating and CP -conserving contributions are expected to be suppressed. Test of $\Delta S = 1$ weak neutral current.

VALUE (units 10^{-5})	CL%	EVTS	DOCUMENT ID	TECN
< 5.8	90	0	WEAVER	94 E799
• • • We do not use the following data for averages, fits, limits, etc. • • •				
< 22	90	0	GRAHAM	92 CNTR
< 760	90		⁶⁰ LITTENBERG	89 RVUE

⁶⁰ LITTENBERG 89 is from retroactive data analysis of CRONIN 67.

$\Gamma(e^\pm \mu^\mp)/\Gamma_{\text{total}}$ Γ_{30}/Γ

Test of lepton family number conservation.

VALUE (units 10^{-11})	CL%	EVTS	DOCUMENT ID	TECN	COMMENT
< 3.3	90	0	⁶¹ ARISAKA	93 B791	
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●					
< 9.4	90	0	AKAGI	95 SPEC	
< 3.9	90	0	ARISAKA	93 B791	
< 9.4	90	0	AKAGI	91 SPEC	Sup. by AKAGI 95
< 43	90		INAGAKI	89 SPEC	In AKAGI 91
< 22	90		MATHIAZHA...	89 SPEC	
< 190	90		SCHAFFNER	89 SPEC	
< 1100	90		COUSINS	88 SPEC	
< 670	90		GREENLEE	88 SPEC	Repl. by SCHAFFNER 89
< 157	90		⁶² CLARK	71 ASPK	

⁶¹ This is the combined result of ARISAKA 93 and MATHIAZHAGAN 89.

⁶² Possible (but unknown) systematic errors. See note on CLARK 71 $\Gamma(\mu^+ \mu^-)/\Gamma(\pi^+ \pi^-)$ entry.

 $\Gamma(e^\pm e^\pm \mu^\mp \mu^\mp)/\Gamma_{\text{total}}$ Γ_{31}/Γ

Test of lepton family number conservation.

VALUE (units 10^{-9})	CL%	EVTS	DOCUMENT ID	TECN
< 6.1	90	0	⁶³ GU	96 E799

⁶³ Assuming uniform phase space distribution.

 $\Gamma(e^\pm \mu^\mp)/[\Gamma(\pi^+ \pi^- \pi^0) + \Gamma(\pi^\pm \mu^\mp \nu) + \Gamma(\pi^\pm e^\mp \nu_e)]$ $\Gamma_{30}/(\Gamma_2 + \Gamma_3 + \Gamma_6)$

Test of lepton family number conservation.

VALUE (units 10^{-4})	CL%	DOCUMENT ID	TECN
< 0.1	90	BOTT-...	67 OSPK
< 0.08	90	FITCH	67 OSPK
< 1.0	90	CARPENTER	66 OSPK
< 10.0		ANIKINA	65 CC

● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●

< 0.1	90	BOTT-...	67 OSPK
< 0.08	90	FITCH	67 OSPK
< 1.0	90	CARPENTER	66 OSPK
< 10.0		ANIKINA	65 CC