



$$I^G(J^{PC}) = 1^-(0^{-+})$$

We have omitted some results that have been superseded by later experiments. The omitted results may be found in our 1988 edition Physics Letters **B204** (1988).

### $\pi^0$ MASS

The value is calculated from  $m_{\pi^\pm}$  and  $(m_{\pi^\pm} - m_{\pi^0})$ . See notes under the  $\pi^\pm$  Mass Listings concerning recent revision of the charged pion mass.

<u>VALUE (MeV)</u>	<u>DOCUMENT ID</u>
<b>134.9764 ± 0.0006 OUR FIT</b>	

### $m_{\pi^\pm} - m_{\pi^0}$

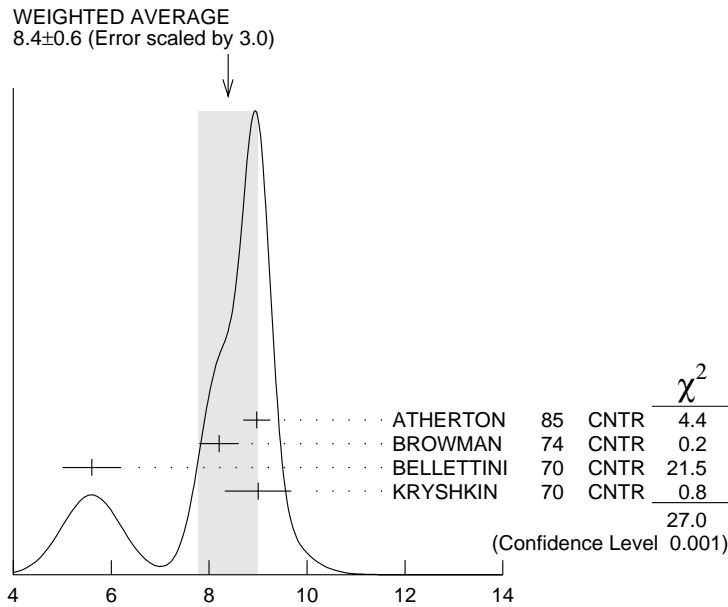
Measurements with an error > 0.01 MeV have been omitted.

<u>VALUE (MeV)</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
<b>4.5936 ± 0.0005 OUR FIT</b>			
<b>4.5936 ± 0.0005 OUR AVERAGE</b>			
4.59364 ± 0.00048	CRAWFORD 91	CNTR	$\pi^- p \rightarrow \pi^0 n, n$ TOF
4.5930 ± 0.0013	CRAWFORD 86	CNTR	$\pi^- p \rightarrow \pi^0 n, n$ TOF
• • • We do not use the following data for averages, fits, limits, etc. • • •			
4.59366 ± 0.00048	CRAWFORD 88B	CNTR	See CRAWFORD 91
4.6034 ± 0.0052	VASILEVSKY 66	CNTR	
4.6056 ± 0.0055	CZIRR 63	CNTR	

### $\pi^0$ MEAN LIFE

Measurements with an error >  $1 \times 10^{-17}$  s have been omitted.

<u>VALUE (<math>10^{-17}</math> s)</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
<b>8.4 ± 0.6 OUR AVERAGE</b>				Error includes scale factor of 3.0. See the ideogram below.
8.97 ± 0.22 ± 0.17		ATHERTON 85	CNTR	
8.2 ± 0.4		<sup>1</sup> BROWMAN 74	CNTR	Primakoff effect
5.6 ± 0.6		BELLETTINI 70	CNTR	Primakoff effect
9 ± 0.68		KRYSHKIN 70	CNTR	Primakoff effect
• • • We do not use the following data for averages, fits, limits, etc. • • •				
8.4 ± 0.5 ± 0.5	1182	<sup>2</sup> WILLIAMS 88	CBAL	$e^+ e^- \rightarrow e^+ e^- \pi^0$
<sup>1</sup> BROWMAN 74 gives a $\pi^0$ width $\Gamma = 8.02 \pm 0.42$ eV. The mean life is $\hbar/\Gamma$ .				
<sup>2</sup> WILLIAMS 88 gives $\Gamma(\gamma\gamma) = 7.7 \pm 0.5 \pm 0.5$ eV. We give here $\tau = \hbar/\Gamma(\text{total})$ .				



$\pi^0$  mean life ( $10^{-17}$  s)

### $\pi^0$ DECAY MODES

Mode	Fraction ( $\Gamma_i/\Gamma$ )	Scale factor/ Confidence level
$\Gamma_1$ $2\gamma$	$(98.798 \pm 0.032) \%$	S=1.1
$\Gamma_2$ $e^+ e^- \gamma$	$(1.198 \pm 0.032) \%$	S=1.1
$\Gamma_3$ $\gamma$ positronium	$(1.82 \pm 0.29) \times 10^{-9}$	
$\Gamma_4$ $e^+ e^+ e^- e^-$	$(3.14 \pm 0.30) \times 10^{-5}$	
$\Gamma_5$ $e^+ e^-$	$(7.5 \pm 2.0) \times 10^{-8}$	
$\Gamma_6$ $4\gamma$	$< 2 \times 10^{-8}$	CL=90%
$\Gamma_7$ $\nu \bar{\nu}$	[a] $< 8.3 \times 10^{-7}$	CL=90%
$\Gamma_8$ $\nu_e \bar{\nu}_e$	$< 1.7 \times 10^{-6}$	CL=90%
$\Gamma_9$ $\nu_\mu \bar{\nu}_\mu$	$< 3.1 \times 10^{-6}$	CL=90%
$\Gamma_{10}$ $\nu_\tau \bar{\nu}_\tau$	$< 2.1 \times 10^{-6}$	CL=90%

#### Charge conjugation (C) or Lepton Family number (LF) violating modes

$\Gamma_{11}$ $3\gamma$	C	$< 3.1 \times 10^{-8}$	CL=90%
$\Gamma_{12}$ $\mu^+ e^-$			
$\Gamma_{13}$ $\mu^+ e^- + e^- \mu^+$	LF	$< 1.72 \times 10^{-8}$	CL=90%

[a] Astrophysical and cosmological arguments give limits of order  $10^{-13}$ ; see the Particle Listings below.

**CONSTRAINED FIT INFORMATION**

An overall fit to 2 branching ratios uses 4 measurements and one constraint to determine 3 parameters. The overall fit has a  $\chi^2 = 1.9$  for 2 degrees of freedom.

The following *off-diagonal* array elements are the correlation coefficients  $\langle \delta x_i \delta x_j \rangle / (\delta x_i \delta x_j)$ , in percent, from the fit to the branching fractions,  $x_i \equiv \Gamma_i / \Gamma_{\text{total}}$ . The fit constrains the  $x_i$  whose labels appear in this array to sum to one.

$x_2$	-100	
$x_4$	-1	0
	$x_1$	$x_2$

 **$\pi^0$  BRANCHING RATIOS** **$\Gamma(e^+ e^- \gamma) / \Gamma(2\gamma)$   $\Gamma_2 / \Gamma_1$** 

<u>VALUE (%)</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
<b>1.213 ± 0.033 OUR FIT</b>				Error includes scale factor of 1.1.
<b>1.213 ± 0.030 OUR AVERAGE</b>				
1.25 ± 0.04		SCHARDT	81 SPEC	$\pi^- p \rightarrow n\pi^0$
1.166 ± 0.047	3071	<sup>3</sup> SAMIOS	61 HBC	$\pi^- p \rightarrow n\pi^0$
1.17 ± 0.15	27	BUDAGOV	60 HBC	
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●				
1.196		JOSEPH	60 THEO	QED calculation
<sup>3</sup> SAMIOS 61 value uses a Panofsky ratio = 1.62.				

 **$\Gamma(\gamma \text{ positronium}) / \Gamma(2\gamma)$   $\Gamma_3 / \Gamma_1$** 

<u>VALUE (units <math>10^{-9}</math>)</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
<b>1.84 ± 0.29</b>	277	AFANASYEV	90 CNTR	$pC$ 70 GeV

 **$\Gamma(e^+ e^+ e^- e^-) / \Gamma(2\gamma)$   $\Gamma_4 / \Gamma_1$** 

<u>VALUE (units <math>10^{-5}</math>)</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
<b>3.18 ± 0.30 OUR FIT</b>				
<b>3.18 ± 0.30</b>	146	<sup>4</sup> SAMIOS	62B HBC	
<sup>4</sup> SAMIOS 62B value uses a Panofsky ratio = 1.62.				

 **$\Gamma(e^+ e^-) / \Gamma_{\text{total}}$   $\Gamma_5 / \Gamma$** 

<u>VALUE (units <math>10^{-8}</math>)</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
<b>7.5 ± 2.0 OUR AVERAGE</b>				
6.9 ± 2.3 ± 0.6	21	<sup>5</sup> DESHPANDE	93 SPEC	$K^+ \rightarrow \pi^+ \pi^0$
8.8 <sup>+4.5</sup> <sub>-3.2</sub> ± 0.6	8	<sup>6</sup> MCFARLAND	93 SPEC	$K_L^0 \rightarrow 3\pi^0$ in flight

<sup>5</sup> The DESHPANDE 93 result with bremsstrahlung radiative corrections is  $(8.0 \pm 2.6 \pm 0.6) \times 10^{-8}$ .

<sup>6</sup> The MCFARLAND 93 result with radiative corrections and excluding  $[m_{e e} / m_{\pi^0}]^2 < 0.95$  is  $(7.6<sup>+3.9</sup><sub>-2.8</sub> ± 0.5) \times 10^{-8}$ .

$\Gamma(e^+e^-)/\Gamma(2\gamma)$ 
 $\Gamma_5/\Gamma_1$ 

<u>VALUE (units <math>10^{-7}</math>)</u>	<u>CL%</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●					
<1.3	90		NIEBUHR	89 SPEC	$\pi^- p \rightarrow \pi^0 n$ at rest
<5.3	90		ZEPHAT	87 SPEC	$\pi^- p \rightarrow \pi^0 n$ 0.3 GeV/c
1.7 $\pm 0.6 \pm 0.3$		59	FRANK	83 SPEC	$\pi^- p \rightarrow n \pi^0$
1.8 $\pm 0.6$		58	MISCHKE	82 SPEC	See FRANK 83
2.23 $^{+2.40}_{-1.10}$	90	8	FISCHER	78B SPRK	$K^+ \rightarrow \pi^+ \pi^0$

 $\Gamma(4\gamma)/\Gamma_{\text{total}}$ 
 $\Gamma_6/\Gamma$ 

<u>VALUE (units <math>10^{-8}</math>)</u>	<u>CL%</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
< 2	90		MCDONOUGH 88	CBOX	$\pi^- p$ at rest
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●					
<160	90		BOLOTOV	86C CALO	
<440	90	0	AUERBACH	80 CNTR	

 $\Gamma(\nu\bar{\nu})/\Gamma_{\text{total}}$ 
 $\Gamma_7/\Gamma$ 

The astrophysical and cosmological limits are many orders of magnitude lower, but we use the best laboratory limit for the Summary Tables.

<u>VALUE (units <math>10^{-6}</math>)</u>	<u>CL%</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
< 0.83	90		<sup>7</sup> ATIYA	91 B787	$K^+ \rightarrow \pi^+ \nu\nu'$
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●					
< 2.9 $\times 10^{-7}$			<sup>8</sup> LAM	91	Cosmological limit
< 3.2 $\times 10^{-7}$			<sup>9</sup> NATALE	91	SN 1987A
< 6.5	90		DORENBOS...	88 CHRM	Beam dump, prompt
<24	90	0	<sup>7</sup> HERCZEG	81 RVUE	$K^+ \rightarrow \pi^+ \nu\nu'$

<sup>7</sup> This limit applies to all possible  $\nu\nu'$  states as well as to other massless, weakly interacting states.

<sup>8</sup> LAM 91 considers the production of right-handed neutrinos produced from the cosmic thermal background at the temperature of about the pion mass through the reaction  $\gamma\gamma \rightarrow \pi^0 \rightarrow \nu\bar{\nu}$ .

<sup>9</sup> NATALE 91 considers the excess energy-loss rate from SN 1987A if the process  $\gamma\gamma \rightarrow \pi^0 \rightarrow \nu\bar{\nu}$  occurs, permitted if the neutrinos have a right-handed component. As pointed out in LAM 91 (and confirmed by Natale), there is a factor 4 error in the NATALE 91 published result ( $0.8 \times 10^{-7}$ ).

 $\Gamma(\nu_e\bar{\nu}_e)/\Gamma_{\text{total}}$ 
 $\Gamma_8/\Gamma$ 

<u>VALUE (units <math>10^{-6}</math>)</u>	<u>CL%</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
<1.7	90	DORENBOS...	88 CHRM	Beam dump, prompt $\nu$
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●				
<3.1	90	<sup>10</sup> HOFFMAN	88 RVUE	Beam dump, prompt $\nu$
<sup>10</sup> HOFFMAN 88 analyzes data from a 400-GeV BEBC beam-dump experiment.				

$\Gamma(\nu_\mu \bar{\nu}_\mu)/\Gamma_{\text{total}}$   $\Gamma_9/\Gamma$ 

VALUE (units $10^{-6}$ )	CL%	DOCUMENT ID	TECN	COMMENT
<3.1	90	<sup>11</sup> HOFFMAN	88	RVUE Beam dump, prompt $\nu$
• • • We do not use the following data for averages, fits, limits, etc. • • •				
<7.8	90	DORENBOS...	88	CHRM Beam dump, prompt $\nu$
<sup>11</sup> HOFFMAN 88 analyzes data from a 400-GeV BEBC beam-dump experiment.				

 $\Gamma(\nu_\tau \bar{\nu}_\tau)/\Gamma_{\text{total}}$   $\Gamma_{10}/\Gamma$ 

VALUE (units $10^{-6}$ )	CL%	DOCUMENT ID	TECN	COMMENT
<2.1	90	<sup>12</sup> HOFFMAN	88	RVUE Beam dump, prompt $\nu$
• • • We do not use the following data for averages, fits, limits, etc. • • •				
<4.1	90	DORENBOS...	88	CHRM Beam dump, prompt $\nu$
<sup>12</sup> HOFFMAN 88 analyzes data from a 400-GeV BEBC beam-dump experiment.				

 $\Gamma(3\gamma)/\Gamma_{\text{total}}$   $\Gamma_{11}/\Gamma$ 

Forbidden by  $C$  invariance.

VALUE (units $10^{-8}$ )	CL%	EVTS	DOCUMENT ID	TECN	COMMENT
< 3.1	90		MCDONOUGH	88	CBOX $\pi^- p$ at rest
• • • We do not use the following data for averages, fits, limits, etc. • • •					
< 38	90	0	HIGHLAND	80	CNTR
<150	90	0	AUERBACH	78	CNTR
<490	90	0	<sup>13</sup> DUCLOS	65	CNTR
<490	90		<sup>13</sup> KUTIN	65	CNTR
<sup>13</sup> These experiments give $B(3\gamma/2\gamma) < 5.0 \times 10^{-6}$ .					

 $\Gamma(\mu^+ e^-)/\Gamma_{\text{total}}$   $\Gamma_{12}/\Gamma$ 

Forbidden by lepton family number conservation.

VALUE (units $10^{-9}$ )	CL%	DOCUMENT ID	TECN	COMMENT
• • • We do not use the following data for averages, fits, limits, etc. • • •				
<16	90	LEE	90	SPEC $K^+ \rightarrow \pi^+ \mu^+ e^-$
<78	90	CAMPAGNARI	88	SPEC See LEE 90

 $[\Gamma(\mu^+ e^-) + \Gamma(e^- \mu^+)]/\Gamma_{\text{total}}$   $\Gamma_{13}/\Gamma$ 

Forbidden by lepton family number conservation.

VALUE (units $10^{-9}$ )	CL%	DOCUMENT ID	TECN	COMMENT
< 17.2	90	KROLAK	94	E799 In $K_L^0 \rightarrow 3\pi^0$
• • • We do not use the following data for averages, fits, limits, etc. • • •				
<140		HERCZEG	84	RVUE $K^+ \rightarrow \pi^+ \mu e$
< 2 $\times 10^{-6}$		HERCZEG	84	THEO $\mu^- \rightarrow e^-$ conversion
< 70	90	BRYMAN	82	RVUE $K^+ \rightarrow \pi^+ \mu e$

**$\pi^0$  ELECTROMAGNETIC FORM FACTOR**

The amplitude for the process  $\pi^0 \rightarrow e^+ e^- \gamma$  contains a form factor  $F(x)$  at the  $\pi^0 \gamma \gamma$  vertex, where  $x = [m_{e^+ e^-} / m_{\pi^0}]^2$ . The parameter  $a$  in the linear expansion  $F(x) = 1 + ax$  is listed below.

All the measurements except that of BEHREND 91 are in the time-like region of momentum transfer.

**LINEAR COEFFICIENT OF  $\pi^0$  ELECTROMAGNETIC FORM FACTOR**

<u>VALUE</u>	<u>EVTs</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
<b>0.032 ±0.004 OUR AVERAGE</b>				
+0.026 ±0.024 ±0.048	7548	FARZANPAY	92 SPEC	$\pi^- p \rightarrow \pi^0 n$ at rest
+0.025 ±0.014 ±0.026	54k	MEIJERDREES	92B SPEC	$\pi^- p \rightarrow \pi^0 n$ at rest
+0.0326 ±0.0026 ±0.0026	127	<sup>14</sup> BEHREND	91 CELL	$e^+ e^- \rightarrow e^+ e^- \pi^0$
-0.11 ±0.03 ±0.08	32k	FONVIEILLE	89 SPEC	Radiation corr.
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●				
0.12 +0.05 -0.04		<sup>15</sup> TUPPER	83 THEO	FISCHER 78 data
+0.10 ±0.03	31k	<sup>16</sup> FISCHER	78 SPEC	Radiation corr.
+0.01 ±0.11	2200	DEVONS	69 OSPK	No radiation corr.
-0.15 ±0.10	7676	KOBRAK	61 HBC	No radiation corr.
-0.24 ±0.16	3071	SAMIOS	61 HBC	No radiation corr.

<sup>14</sup> BEHREND 91 estimates that their systematic error is of the same order of magnitude as their statistical error, and so we have included a systematic error of this magnitude. The value of  $a$  is obtained by extrapolation from the region of large space-like momentum transfer assuming vector dominance.

<sup>15</sup> TUPPER 83 is a theoretical analysis of FISCHER 78 including 2-photon exchange in the corrections.

<sup>16</sup> The FISCHER 78 error is statistical only. The result without radiation corrections is  $+0.05 \pm 0.03$ .

 **$\pi^0$  REFERENCES**

We have omitted some papers that have been superseded by later experiments. The omitted papers may be found in our 1988 edition Physics Letters **B204** (1988).

KROLAK	94	PL B320 407	+	(EFI, UCLA, COLO, ELMT, FNAL, ILL, OSAK, RUTG)
DESHPANDE	93	PRL 71 27	+Alliegro, Chaloupka+	(BNL E851 Collab.)
MCFARLAND	93	PRL 71 31	+	(EFI, UCLA, COLO, ELMT, FNAL, ILL, OSAK, RUTG)
FARZANPAY	92	PL B278 413	+	(ORST, TRIU, BRCO, QUKI, LBL, BIRM, OXF)
MEIJERDREES	92B	PR D45 1439	Meijer Drees, Waltham+	(PSI SINDRUM-I Collab.)
ATIYA	91	PRL 66 2189	+Chiang, Frank, Haggerty+	(BNL, LANL, PRIN, TRIU)
BEHREND	91	ZPHY C49 401	+Criegee, Field, Franke+	(CELLO Collab.)
CRAWFORD	91	PR D43 46	+Daum, Frosch, Jost, Kettle+	(VILL, VIRG)
LAM	91	PR D44 3345	+Ng	(AST)
NATALE	91	PL B258 227		(SPIFT)
AFANASYEV	90	PL B236 116	+Chvyrov, Karpukhin+	(JINR, MOSU, SERP)
Also	90B	SJNP 51 664	Afanasyev, Gorchakov, Karpukhin, Komarov+	(JINR)
			Translated from YAF 51 1040.	

LEE	90	PRL 64 165	+Alliegro, Campagnari+	(BNL, FNAL, VILL, WASH, YALE)
FONVIEILLE	89	PL B233 65	+Bensayah, Berthot, Bertin+	(CLER, LYON, SACL)
NIEBUHR	89	PR D40 2796	+Eichler, Felawka, Kozlowski+	(SINDRUM Collab.)
CAMPAGNARI	88	PRL 61 2062	+Alliegro, Chaloupka+	(BNL, FNAL, PSI, WASH, YALE)
CRAWFORD	88B	PL B213 391	+Daum, Frosch, Jost, Kettle, Marshall+	(PSI, VIRG)
DORENBOS...	88	ZPHY C40 497	+Dorenbosch, Allaby, Amaldi, Barbiellini+	(CHARM Collab.)
HOFFMAN	88	PL B208 149		(LANL)
MCDONOUGH	88	PR D38 2121	+Highland, McFarlane, Bolton+	(TEMP, LANL, CHIC)
PDG	88	PL B204	Yost, Barnett+	(LBL+)
WILLIAMS	88	PR D38 1365	+Antreasyan, Bartels, Besset+	(Crystal Ball Collab.)
ZEPHAT	87	JPG 13 1375	+Playfer, van Doesburg, Bressani+	(OMICRON Collab.)
BOLOTOV	86C	JETPL 43 520	+Gninenko, Dzhilkibaev, Isakov	(INRM)
		Translated from ZETFP 43 405.		
CRAWFORD	86	PRL 56 1043	+Daum, Frosch, Jost, Kettle+	(SIN, VIRG)
ATHERTON	85	PL 158B 81	+Bovet, Coet+	(CERN, ISU, LUND, CURIN, EFI)
HERCZEG	84	PR D29 1954	+Hoffman	(LANL)
FRANK	83	PR D28 423	+Hoffman, Mischke, Moir+	(LANL, ARZS)
TUPPER	83	PR D28 2905	+Grose, Samuel	(OKSU)
BRYMAN	82	PR D26 2538		(TRIU)
MISCHKE	82	PRL 48 1153	+Frank, Hoffman, Moir, Sarracino+	(LANL, ARZS)
HERCZEG	81	PL 100B 347	+Hoffman	(LANL)
SCHARDT	81	PR D23 639	+Frank, Hoffmann, Mischke, Moir+	(ARZS, LANL)
AUERBACH	80	PL 90B 317	+Haik, Highland, McFarlane, Macek+	(TEMP, LASL)
HIGHLAND	80	PRL 44 628	+Auerbach, Haik, McFarlane, Macek+	(TEMP, LASL)
AUERBACH	78	PRL 41 275	+Highland, Johnson+	(TEMP, LASL)
FISCHER	78	PL 73B 359	+Extermann, Guisan, Mermod+	(GEVA, SACL)
FISCHER	78B	PL 73B 364	+Extermann, Guisan, Mermod+	(GEVA, SACL)
BROWMAN	74	PRL 33 1400	+Dewire, Gittelman, Hanson+	(CORN, BING)
BELLETTINI	70	NC 66A 243	+Bemporad, Lubelsmey+	(PISA, BONN)
KRYSHKIN	70	JETP 30 1037	+Sterligov, Usov	(TMSK)
		Translated from ZETF 57 1917.		
DEVONS	69	PR 184 1356	+Nemethy, Nissim-Sabat, Capua+	(COLU, ROMA)
VASILEVSKY	66	PL 23 281	+Vishnyakov, Dunaitsev+	(JINR)
DUCLOS	65	PL 19 253	+Freytag, Heintze+	(CERN, HEID)
KUTIN	65	JETPL 2 243	+Petrukhin, Prokoshkin	(JINR)
		Translated from unknown journal.		
CZIRR	63	PR 130 341		(LRL)
SAMIOS	62B	PR 126 1844	+Plano, Prodell+	(COLU, BNL)
KOBRAK	61	NC 20 1115		(EFI)
SAMIOS	61	PR 121 275		(COLU, BNL)
BUDAGOV	60	JETP 11 755	+Viktor, Dzhelepov, Ermolov+	(JINR)
		Translated from ZETF 38 1047.		
JOSEPH	60	NC 16 997		(EFI)