

**$f_J(1710)$** 

$$I^G(J^{PC}) = 0^{+(\text{even}++)}$$

**THE  $f_J(1710)$** 

Written March 1998 by M. Doser (CERN).

The  $f_J(1710)$  is seen in the radiative decay  $J/\psi(1S) \rightarrow \gamma f_J(1710)$ ; therefore  $C = +1$ . It decays into  $2\eta$  and  $K_S^0 K_S^0$ , which implies  $I^G J^{PC} = 0^{+(\text{even})^{++}}$ . The spin of the  $f_J(1710)$  is controversial. Combined amplitude analyses of the  $K^+ K^-$ ,  $K_S K_S$  and  $\pi^+ \pi^-$  systems produced in  $J/\psi(1S)$  radiative decay (in recent and some earlier unpublished analyses by the Mark III Collaboration) find a large spin-0 component, as well as reproducing known parameters of the  $f_2(1270)$  and  $f_2'(1525)$ . A recent reanalysis (BUGG 95) of the  $4\pi$  channel from MARK III, allowing both  $\rho\rho$  and two  $\pi\pi$   $S$  waves, finds two states, a  $0^{++}$  at  $\sim 1750$  MeV and a  $2^{++}$  at  $\sim 1620$  MeV. Earlier analyses of the  $\rho\rho$  final state (BISELLO 89B, BALTRUSAITIS 86B) found only pseudoscalar activity in the  $f_J(1710)$  region, but considered only the process  $J/\psi(1S) \rightarrow \gamma\rho\rho$ . In contrast, a spin 2 was found for the  $f_J(1710)$  in earlier analyses of the  $\eta\eta$  (BLOOM 83) or  $K^+ K^-$  (BALTRUSAITIS 87) systems based on less statistics. More recently, an analysis of the  $K^+ K^-$  channel finds indications for a lower mass tensor as well as a higher mass scalar state (BAI 96C).

In  $pp$  central production at 300 GeV/ $c$  in both  $K^+ K^-$  and  $K_S^0 K_S^0$ ,  $f_J(1710)$  is definitely spin 2 (ARMSTRONG 89D). More recent analyses with greater statistics (E690 Collaboration, unpublished) are, however, not able to differentiate between spin 0 and 2. Generally, analyses preferring spin 2 concentrate on angular distributions in the  $f_J(1710)$  region, and do not include possible interferences or distortion due to the nearby  $f_2'(1525)$ .

The  $f_J(1710)$  is also observed in  $K\bar{K}$  (FALVARD 88) in  $J/\psi(1S) \rightarrow \omega K\bar{K}$  and  $J/\psi(1S) \rightarrow \phi K\bar{K}$ , but with no spin-parity analysis. ARMSTRONG 93C also sees a broad peak at 1747 MeV in  $p\bar{p}$  annihilation into  $\eta\eta$ , which may be the  $f_J(1710)$ . This resonance is not observed in the hypercharge-exchange reactions  $K^-p \rightarrow K_S^0 K_S^0 \Lambda$  (ASTON 88D) and  $K^-p \rightarrow K_S^0 K_S^0 Y^*$  (BOLONKIN 86).

A partial-wave analysis of the  $K_S^0 K_S^0$  system in  $\pi^- p \rightarrow K_S^0 K_S^0 n$  (BOLONKIN 88) finds a  $D_0$ -wave behavior ( $J^{PC} = 2^{++}$ ) near 1700 MeV, but the width ( $\sim 30$  MeV) is much smaller than those observed in  $J/\psi(1S)$  decays and in hadroproduction. The  $0^{++}$  wave shows, however a broad enhancement around 1720 MeV.

### $f_J(1710)$ MASS

<u>VALUE (MeV)</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
<b>1712 ± 5 OUR AVERAGE</b>	Error	includes scale factor of 1.1.	
1713 ± 10	1 ARMSTRONG 89D	OMEG	300 $pp \rightarrow ppK^+K^-$
1706 ± 10	1 ARMSTRONG 89D	OMEG	300 $pp \rightarrow ppK_S^0 K_S^0$
1707 ± 10	2 AUGUSTIN 88	DM2	$J/\psi \rightarrow \gamma K^+ K^-$ , $K_S^0 K_S^0$
1698 ± 15	2 AUGUSTIN 87	DM2	$J/\psi \rightarrow \gamma \pi^+ \pi^-$
1720 ± 10 ± 10	3 BALTRUSAIT..87	MRK3	$J/\psi \rightarrow \gamma K^+ K^-$
1742 ± 15	2 WILLIAMS 84	MPSF	200 $\pi^- N \rightarrow 2K_S^0 X$
1670 ± 50	BLOOM 83	CBAL	$J/\psi \rightarrow \gamma 2\eta$
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●			
1704 <sup>+16</sup> <sub>-23</sub>	4 DUNWOODIE 97		$J/\psi \rightarrow K\bar{K}, \pi\pi$
1690 ± 11	5 ABREU 96C	DLPH	$\gamma\gamma \rightarrow K^+ K^- E_{cm}^{ee} = 91.2$ GeV
1696 ± 5 <sup>+9</sup> <sub>-34</sub>	3 BAI 96C	BES	$J/\psi \rightarrow \gamma K^+ K^-$
1781 ± 8 <sup>+10</sup> <sub>-31</sub>	6 BAI 96C	BES	$J/\psi \rightarrow \gamma K^+ K^-$
1768 ± 14	BALOSHIN 95	SPEC	40 $\pi^- C \rightarrow K_S^0 K_S^0 X$
1750 ± 15	7 BUGG 95	MRK3	$J/\psi \rightarrow \gamma \pi^+ \pi^- \pi^+ \pi^-$
1620 ± 16	3 BUGG 95	MRK3	$J/\psi \rightarrow \gamma \pi^+ \pi^- \pi^+ \pi^-$
1748 ± 10	2 ARMSTRONG 93C	E760	$\bar{p}p \rightarrow \pi^0 \eta \eta \rightarrow 6\gamma$
~ 1750	BREAKSTONE 93	SFM	$pp \rightarrow pp\pi^+ \pi^- \pi^+ \pi^-$

1744 ± 15	<sup>8</sup> ALDE	92D GAM2	38 $\pi^- p \rightarrow \eta\eta N^*$
1700 ± 15	<sup>3</sup> BOLONKIN	88 SPEC	40 $\pi^- p \rightarrow K_S^0 K_S^0 n$
1720 ± 60	<sup>6</sup> BOLONKIN	88 SPEC	40 $\pi^- p \rightarrow K_S^0 K_S^0 n$
1638 ± 10	<sup>9</sup> FALVARD	88 DM2	$J/\psi \rightarrow \phi K^+ K^-$ , $K_S^0 K_S^0$
1690 ± 4	<sup>10</sup> FALVARD	88 DM2	$J/\psi \rightarrow \phi K^+ K^-$ , $K_S^0 K_S^0$
1730 <sup>+</sup> <sub>-10</sub>	<sup>11</sup> LONGACRE	86 RVUE	22 $\pi^- p \rightarrow n 2K_S^0$
1650 ± 50	BURKE	82 MRK2	$J/\psi \rightarrow \gamma 2\rho$
1640 ± 50	<sup>12,13</sup> EDWARDS	82D CBAL	$J/\psi \rightarrow \gamma 2\eta$
1730 ± 10 ± 20	<sup>14</sup> ETKIN	82C MPS	23 $\pi^- p \rightarrow n 2K_S^0$

<sup>1</sup>  $J^P = 2^+$ , ( $0^+$  excluded).

<sup>2</sup> No  $J^{PC}$  determination.

<sup>3</sup>  $J^P = 2^+$ .

<sup>4</sup>  $J^P = 0^+$ , reanalysis of MARK III data.

<sup>5</sup> No  $J^{PC}$  determination, width not determined.

<sup>6</sup>  $J^P = 0^+$ .

<sup>7</sup> From a fit to the  $0^+$  partial wave.

<sup>8</sup> ALDE 92D combines all the GAMS-2000 data.

<sup>9</sup> From an analysis ignoring interference with  $f_2'(1525)$ .

<sup>10</sup> From an analysis including interference with  $f_2'(1525)$ .

<sup>11</sup> Uses MRK3 data. From a partial-wave analysis of data using a K-matrix formalism with 5 poles, but assuming spin 2. Fit with constrained inelasticity.

<sup>12</sup>  $J^P = 2^+$  preferred.

<sup>13</sup> From fit neglecting nearby  $f_2'(1525)$ . Replaced by BLOOM 83.

<sup>14</sup> Superseded by LONGACRE 86.

### $f_J(1710)$ WIDTH

VALUE (MeV)	CL%	DOCUMENT ID	TECN	COMMENT
<b>133 ± 14</b>	<b>OUR AVERAGE</b>	Error includes scale factor of 1.2.		
181 ± 30		<sup>15</sup> ARMSTRONG	89D OMEG	300 $pp \rightarrow pp K^+ K^-$
104 ± 30		<sup>15</sup> ARMSTRONG	89D OMEG	300 $pp \rightarrow pp K_S^0 K_S^0$
166.4 ± 33.2		<sup>16</sup> AUGUSTIN	88 DM2	$J/\psi \rightarrow \gamma K^+ K^-$ , $K_S^0 K_S^0$
136 ± 28		<sup>16</sup> AUGUSTIN	87 DM2	$J/\psi \rightarrow \gamma \pi^+ \pi^-$
130 ± 20		<sup>17</sup> BALTRUSAIT..	87 MRK3	$J/\psi \rightarrow \gamma K^+ K^-$
57 ± 38		<sup>2</sup> WILLIAMS	84 MPSF	200 $\pi^- N \rightarrow 2K_S^0 X$
160 ± 80		BLOOM	83 CBAL	$J/\psi \rightarrow \gamma 2\eta$
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●				
124 <sup>+</sup> <sub>-44</sub>		<sup>18</sup> DUNWOODIE	97	$J/\psi \rightarrow K\bar{K}, \pi\pi$
103 ± 18 <sup>+</sup> <sub>-11</sub>		<sup>17</sup> BAI	96C BES	$J/\psi \rightarrow \gamma K^+ K^-$
85 ± 24 <sup>+</sup> <sub>-19</sub>		<sup>19</sup> BAI	96C BES	$J/\psi \rightarrow \gamma K^+ K^-$
56 ± 19		BALOSHIN	95 SPEC	40 $\pi^- C \rightarrow K_S^0 K_S^0 X$
160 ± 40		<sup>20</sup> BUGG	95 MRK3	$J/\psi \rightarrow \gamma \pi^+ \pi^- \pi^+ \pi^-$

160 $\pm$ 60 - 20		17 BUGG	95 MRK3	$J/\psi \rightarrow \gamma \pi^+ \pi^- \pi^+ \pi^-$
264 $\pm$ 25		16 ARMSTRONG	93C E760	$\bar{p}p \rightarrow \pi^0 \eta \eta \rightarrow 6\gamma$
200 to 300		BREAKSTONE	93 SFM	$pp \rightarrow$ $pp\pi^+\pi^-\pi^+\pi^-$
< 80	90	21 ALDE	92D GAM2	38 $\pi^- p \rightarrow \eta \eta N^*$
30 $\pm$ 20		17 BOLONKIN	88 SPEC	40 $\pi^- p \rightarrow K_S^0 K_S^0 n$
350 $\pm$ 150		19 BOLONKIN	88 SPEC	40 $\pi^- p \rightarrow K_S^0 K_S^0 n$
148 $\pm$ 17		22 FALVARD	88 DM2	$J/\psi \rightarrow \phi K^+ K^-$ , $K_S^0 K_S^0$
184 $\pm$ 6		23 FALVARD	88 DM2	$J/\psi \rightarrow \phi K^+ K^-$ , $K_S^0 K_S^0$
122 $\pm$ 74 - 15		24 LONGACRE	86 RVUE	22 $\pi^- p \rightarrow n 2K_S^0$
200 $\pm$ 100		BURKE	82 MRK2	$J/\psi \rightarrow \gamma 2\rho$
220 $\pm$ 100 - 70	25,26	EDWARDS	82D CBAL	$J/\psi \rightarrow \gamma 2\eta$
200.0 $\pm$ 156.0 - 9.0	27	ETKIN	82B MPS	23 $\pi^- p \rightarrow n 2K_S^0$

15  $J^P = 2^+$ , ( $0^+$  excluded).

16 No  $J^{PC}$  determination.

17  $J^P = 2^+$ .

18  $J^P = 0^+$ , reanalysis of MARK III data.

19  $J^P = 0^+$ .

20 From a fit to the  $0^+$  partial wave.

21 ALDE 92D combines all the GAMS-2000 data.

22 From an analysis ignoring interference with  $f_2'(1525)$ .

23 From an analysis including interference with  $f_2'(1525)$ .

24 Uses MRK3 data. From a partial-wave analysis of data using a K-matrix formalism with 5 poles, but assuming spin 2. Fit with constrained inelasticity.

25  $J^P = 2^+$  preferred.

26 From fit neglecting nearby  $f_2'(1525)$ . Replaced by BLOOM 83.

27 From an amplitude analysis of the  $K_S^0 K_S^0$  system, superseded by LONGACRE 86.

### $f_J(1710)$ DECAY MODES

Mode	Fraction ( $\Gamma_i/\Gamma$ )
$\Gamma_1$ $K\bar{K}$	seen
$\Gamma_2$ $\eta\eta$	seen
$\Gamma_3$ $\pi\pi$	seen
$\Gamma_4$ $\rho\rho$	
$\Gamma_5$ $\gamma\gamma$	

**$f_J(1710) \Gamma(i)\Gamma(\gamma\gamma)/\Gamma(\text{total})$** 

$\Gamma(K\bar{K}) \times \Gamma(\gamma\gamma)/\Gamma_{\text{total}}$					$\Gamma_1\Gamma_5/\Gamma$
VALUE (keV)	CL%	DOCUMENT ID	TECN	COMMENT	
<0.11	95	<sup>28</sup> BEHREND	89C CELL	$\gamma\gamma \rightarrow K_S^0 K_S^0$	
• • • We do not use the following data for averages, fits, limits, etc. • • •					
<0.48	95	ALBRECHT	90G ARG	$\gamma\gamma \rightarrow K^+ K^-$	
<0.28	95	<sup>28</sup> ALTHOFF	85B TASS	$\gamma\gamma \rightarrow K\bar{K}\pi$	
<sup>28</sup> Assuming helicity 2.					

 **$f_J(1710)$  BRANCHING RATIOS**

$\Gamma(K\bar{K})/\Gamma_{\text{total}}$					$\Gamma_1/\Gamma$
VALUE	DOCUMENT ID	TECN	COMMENT		
• • • We do not use the following data for averages, fits, limits, etc. • • •					
$0.38^{+0.09}_{-0.19}$	<sup>29,30</sup> LONGACRE	86 MPS	$22 \pi^- p \rightarrow n 2K_S^0$		

$\Gamma(\eta\eta)/\Gamma_{\text{total}}$					$\Gamma_2/\Gamma$
VALUE	DOCUMENT ID	TECN			
• • • We do not use the following data for averages, fits, limits, etc. • • •					
$0.18^{+0.03}_{-0.13}$	<sup>29,30</sup> LONGACRE	86 RVUE			

$\Gamma(\pi\pi)/\Gamma_{\text{total}}$					$\Gamma_3/\Gamma$
VALUE	DOCUMENT ID	TECN			
• • • We do not use the following data for averages, fits, limits, etc. • • •					
$0.039^{+0.002}_{-0.024}$	<sup>29,30</sup> LONGACRE	86 RVUE			

$\Gamma(\pi\pi)/\Gamma(K\bar{K})$					$\Gamma_3/\Gamma_1$
VALUE	DOCUMENT ID	TECN	COMMENT		
$0.39 \pm 0.14$	ARMSTRONG 91	OMEG	$300 p p \rightarrow p p \pi \pi, p p K\bar{K}$		

$\Gamma(\eta\eta)/\Gamma(K\bar{K})$					$\Gamma_2/\Gamma_1$
VALUE	CL%	DOCUMENT ID	TECN	COMMENT	
• • • We do not use the following data for averages, fits, limits, etc. • • •					
<0.02	90	<sup>31</sup> PROKOSHKIN 91	GA24	$300 \pi^- p \rightarrow \pi^- p \eta \eta$	
<sup>29</sup> From a partial-wave analysis of data using a K-matrix formalism with 5 poles, but assuming spin 2.					
<sup>30</sup> Fit with constrained inelasticity.					
<sup>31</sup> Combining results of GAM4 with those of ARMSTRONG 89D.					

**$f_J(1710)$  REFERENCES**

DUNWOODIE	97	Hadron 97 Conf.	W. Dunwoodie	(SLAC)
ABREU	96C	PL B379 309	+Adam, Adye+	(DELPHI Collab.)
BAI	96C	PRL 77 3959	J.Z. Bai+	(BES Collab.)
BALOSHIN	95	PAN 58 46	+Bolonkin, Vladimirkii+	(ITEP)
		Translated from YAF 58 50.		
BUGG	95	PL B353 378	+Scott, Zoli+	(LOQM, PNPI, WASH)
ARMSTRONG	93C	PL B307 394	+Bettoni+	(FNAL, FERR, GENO, UCI, NWES+)
BREAKSTONE	93	ZPHY C58 251	+Campanini+	(IOWA, CERN, DORT, HEIDH, WARS)
ALDE	92D	PL B284 457	+Binon, Bricman+	(GAM2 Collab.)
Also	91	SJNP 54 451	Alde, Binon, Bricman+	(GAM2 Collab.)
		Translated from YAF 54 745.		
ARMSTRONG	91	ZPHY C51 351	+Benayoun+	(ATHU, BARI, BIRM, CERN, CDEF)
PROKOSHKIN	91	SPD 36 155		(GAM2, GAM4 Collab.)
		Translated from DANS 316 900.		
ALBRECHT	90G	ZPHY C48 183	+Ehrlichmann, Harder+	(ARGUS Collab.)
ARMSTRONG	89D	PL B227 186	+Benayoun	(ATHU, BARI, BIRM, CERN, CDEF)
BEHREND	89C	ZPHY C43 91	+Criegee, Dainton+	(CELLO Collab.)
AUGUSTIN	88	PRL 60 2238	+Calcaterra+	(DM2 Collab.)
BOLONKIN	88	NP B309 426	+Bloshenko, Gorin+	(ITEP, SERP)
FALVARD	88	PR D38 2706	+Ajaltouni+	(CLER, FRAS, LALO, PADO)
AUGUSTIN	87	ZPHY C36 369	+Cosme+	(LALO, CLER, FRAS, PADO)
BALTRUSAIT...	87	PR D35 2077	Baltrusaitis, Coffman, Dubois+	(Mark III Collab.)
LONGACRE	86	PL B177 223	+Etkin+	(BNL, BRAN, CUNY, DUKE, NDAM)
ALTHOFF	85B	ZPHY C29 189	+Braunschweig, Kirschfink+	(TASSO Collab.)
WILLIAMS	84	PR D30 877	+Diamond+	(VAND, NDAM, TUFTS, ARIZ, FNAL+)
BLOOM	83	ARNS 33 143	+Peck	(SLAC, CIT)
BURKE	82	PRL 49 632	+Trilling, Abrams, Alam, Blocker+	(LBL, SLAC)
EDWARDS	82D	PRL 48 458	+Partridge, Peck+	(CIT, HARV, PRIN, STAN, SLAC)
ETKIN	82B	PR D25 1786	+Foley, Lai+	(BNL, CUNY, TUFTS, VAND)
ETKIN	82C	PR D25 2446	+Foley, Lai+	(BNL, CUNY, TUFTS, VAND)

**OTHER RELATED PAPERS**

ANISOVICH	97	PL B395 123	+Sarantsev	(PNPI)
BISELLO	89B	PR D39 701	Busetto+	(DM2 Collab.)
ASTON	88D	NP B301 525	+Awaji, Bienz+	(SLAC, NAGO, CINC, INUS)
AKESSON	86	NP B264 154	+Albrow, Almedhed+	(Axial Field Spec. Collab.)
ARMSTRONG	86B	PL 167B 133	+Bloodworth, Carney+	(ATHU, BARI, BIRM, CERN)
BALTRUSAIT...	86B	PR D33 1222	Baltrusaitis, Coffman, Hauser+	(Mark III Collab.)
ALTHOFF	83	PL 121B 216	+Brandelik, Boerner, Burkhardt+	(TASSO Collab.)
BARNETT	83B	PL 120B 455	+Blockus, Burka, Chien, Christian+	(JHU)
ALTHOFF	82	ZPHY C16 13	+Boerner, Burkhardt+	(TASSO Collab.)
BARNES	82	PL B116 365	+Close	(RHEL)
BARNES	82B	NP B198 360	+Close, Monaghan	(RHEL, OXFTEP)
TANIMOTO	82	PL 116B 198		(BIEL)