

**$N(1710) P_{11}$** 

$$I(J^P) = \frac{1}{2}(\frac{1}{2}^+) \text{ Status: } ***$$

Most of the results published before 1975 are now obsolete and have been omitted. They may be found in our 1982 edition, Physics Letters **111B** (1982).

The various partial-wave analyses do not agree very well.

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### **$N(1710)$ BREIT-WIGNER MASS**

<u>VALUE (MeV)</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
<b>1680 to 1740 (<math>\approx</math> 1710) OUR ESTIMATE</b>			
1717 $\pm$ 28	MANLEY	92	IPWA $\pi N \rightarrow \pi N$ & $N\pi\pi$
1700 $\pm$ 50	CUTKOSKY	80	IPWA $\pi N \rightarrow \pi N$
1723 $\pm$ 9	HOEHLER	79	IPWA $\pi N \rightarrow \pi N$
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●			
1720 $\pm$ 10	ARNDT	96	IPWA $\gamma N \rightarrow \pi N$
1766 $\pm$ 34	<sup>1</sup> BATINIC	95	DPWA $\pi N \rightarrow N\pi, N\eta$
1706	CUTKOSKY	90	IPWA $\pi N \rightarrow \pi N$
1692	CRAWFORD	80	DPWA $\gamma N \rightarrow \pi N$
1730	SAXON	80	DPWA $\pi^- p \rightarrow \Lambda K^0$
1690	BAKER	79	DPWA $\pi^- p \rightarrow n\eta$
1650 to 1680	BAKER	78	DPWA $\pi^- p \rightarrow \Lambda K^0$
1721	BARBOUR	78	DPWA $\gamma N \rightarrow \pi N$
1625 $\pm$ 10	<sup>2</sup> BAKER	77	IPWA $\pi^- p \rightarrow \Lambda K^0$
1650	<sup>2</sup> BAKER	77	DPWA $\pi^- p \rightarrow \Lambda K^0$
1720	<sup>3</sup> LONGACRE	77	IPWA $\pi N \rightarrow N\pi\pi$
1670	KNASEL	75	DPWA $\pi^- p \rightarrow \Lambda K^0$
1710	<sup>4</sup> LONGACRE	75	IPWA $\pi N \rightarrow N\pi\pi$

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### **$N(1710)$ BREIT-WIGNER WIDTH**

<u>VALUE (MeV)</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
<b>50 to 250 (<math>\approx</math> 100) OUR ESTIMATE</b>			
480 $\pm$ 230	MANLEY	92	IPWA $\pi N \rightarrow \pi N$ & $N\pi\pi$
93 $\pm$ 30	CUTKOSKY	90	IPWA $\pi N \rightarrow \pi N$
90 $\pm$ 30	CUTKOSKY	80	IPWA $\pi N \rightarrow \pi N$
120 $\pm$ 15	HOEHLER	79	IPWA $\pi N \rightarrow \pi N$
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●			
105 $\pm$ 10	ARNDT	96	IPWA $\gamma N \rightarrow \pi N$
185 $\pm$ 61	BATINIC	95	DPWA $\pi N \rightarrow N\pi, N\eta$
540	BELL	83	DPWA $\pi^- p \rightarrow \Lambda K^0$
200	CRAWFORD	80	DPWA $\gamma N \rightarrow \pi N$
550	SAXON	80	DPWA $\pi^- p \rightarrow \Lambda K^0$
97	BAKER	79	DPWA $\pi^- p \rightarrow n\eta$
90 to 150	BAKER	78	DPWA $\pi^- p \rightarrow \Lambda K^0$

167		BARBOUR	78	DPWA	$\gamma N \rightarrow \pi N$
160 ± 6		<sup>2</sup> BAKER	77	IPWA	$\pi^- p \rightarrow \Lambda K^0$
95		<sup>2</sup> BAKER	77	DPWA	$\pi^- p \rightarrow \Lambda K^0$
120		<sup>3</sup> LONGACRE	77	IPWA	$\pi N \rightarrow N\pi\pi$
174		KNASEL	75	DPWA	$\pi^- p \rightarrow \Lambda K^0$
75		<sup>4</sup> LONGACRE	75	IPWA	$\pi N \rightarrow N\pi\pi$

### ***N*(1710) POLE POSITION**

#### **REAL PART**

<u>VALUE (MeV)</u>		<u>DOCUMENT ID</u>		<u>TECN</u>	<u>COMMENT</u>
<b>1670 to 1770 (<math>\approx</math> 1720) OUR ESTIMATE</b>					
1770		ARNDT	95	DPWA	$\pi N \rightarrow N\pi$
1690		<sup>5</sup> HOEHLER	93	SPED	$\pi N \rightarrow \pi N$
1698		CUTKOSKY	90	IPWA	$\pi N \rightarrow \pi N$
1690 ± 20		CUTKOSKY	80	IPWA	$\pi N \rightarrow \pi N$
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●					
1636		ARNDT	91	DPWA	$\pi N \rightarrow \pi N$ Soln SM90
1708 or 1712		<sup>6</sup> LONGACRE	78	IPWA	$\pi N \rightarrow N\pi\pi$
1720 or 1711		<sup>3</sup> LONGACRE	77	IPWA	$\pi N \rightarrow N\pi\pi$

#### **− 2×IMAGINARY PART**

<u>VALUE (MeV)</u>		<u>DOCUMENT ID</u>		<u>TECN</u>	<u>COMMENT</u>
<b>80 to 380 (<math>\approx</math> 230) OUR ESTIMATE</b>					
378		ARNDT	95	DPWA	$\pi N \rightarrow N\pi$
200		<sup>5</sup> HOEHLER	93	SPED	$\pi N \rightarrow \pi N$
88		CUTKOSKY	90	IPWA	$\pi N \rightarrow \pi N$
80 ± 20		CUTKOSKY	80	IPWA	$\pi N \rightarrow \pi N$
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●					
544		ARNDT	91	DPWA	$\pi N \rightarrow \pi N$ Soln SM90
17 or 22		<sup>6</sup> LONGACRE	78	IPWA	$\pi N \rightarrow N\pi\pi$
123 or 115		<sup>3</sup> LONGACRE	77	IPWA	$\pi N \rightarrow N\pi\pi$

### ***N*(1710) ELASTIC POLE RESIDUE**

#### **MODULUS $|r|$**

<u>VALUE (MeV)</u>		<u>DOCUMENT ID</u>		<u>TECN</u>	<u>COMMENT</u>
37		ARNDT	95	DPWA	$\pi N \rightarrow N\pi$
15		HOEHLER	93	SPED	$\pi N \rightarrow \pi N$
9		CUTKOSKY	90	IPWA	$\pi N \rightarrow \pi N$
8 ± 2		CUTKOSKY	80	IPWA	$\pi N \rightarrow \pi N$
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●					
149		ARNDT	91	DPWA	$\pi N \rightarrow \pi N$ Soln SM90

#### **PHASE $\theta$**

<u>VALUE (°)</u>		<u>DOCUMENT ID</u>		<u>TECN</u>	<u>COMMENT</u>
− 167		ARNDT	95	DPWA	$\pi N \rightarrow N\pi$
− 167		CUTKOSKY	90	IPWA	$\pi N \rightarrow \pi N$
175 ± 35		CUTKOSKY	80	IPWA	$\pi N \rightarrow \pi N$
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●					
149		ARNDT	91	DPWA	$\pi N \rightarrow \pi N$ Soln SM90

## N(1710) DECAY MODES

The following branching fractions are our estimates, not fits or averages.

Mode	Fraction ( $\Gamma_i/\Gamma$ )
$\Gamma_1$ $N\pi$	10–20 %
$\Gamma_2$ $N\eta$	
$\Gamma_3$ $\Lambda K$	5–25 %
$\Gamma_4$ $\Sigma K$	
$\Gamma_5$ $N\pi\pi$	40–90 %
$\Gamma_6$ $\Delta\pi$	15–40 %
$\Gamma_7$ $\Delta(1232)\pi$ , <i>P</i> -wave	
$\Gamma_8$ $N\rho$	5–25 %
$\Gamma_9$ $N\rho$ , $S=1/2$ , <i>P</i> -wave	
$\Gamma_{10}$ $N\rho$ , $S=3/2$ , <i>P</i> -wave	
$\Gamma_{11}$ $N(\pi\pi)_{S\text{-wave}}^{I=0}$	10–40 %
$\Gamma_{12}$ $p\gamma$	0.002–0.05%
$\Gamma_{13}$ $p\gamma$ , helicity=1/2	0.002–0.05%
$\Gamma_{14}$ $n\gamma$	0.0–0.02%
$\Gamma_{15}$ $n\gamma$ , helicity=1/2	0.0–0.02%

## N(1710) BRANCHING RATIOS

$\Gamma(N\pi)/\Gamma_{\text{total}}$   $\Gamma_1/\Gamma$

<u>VALUE</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
<b>0.10 to 0.20 OUR ESTIMATE</b>			
0.09±0.04	MANLEY	92	IPWA $\pi N \rightarrow \pi N$ & $N\pi\pi$
0.20±0.04	CUTKOSKY	80	IPWA $\pi N \rightarrow \pi N$
0.12±0.04	HOEHLER	79	IPWA $\pi N \rightarrow \pi N$
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●			
0.08±0.14	BATINIC	95	DPWA $\pi N \rightarrow N\pi, N\eta$

$\Gamma(N\eta)/\Gamma_{\text{total}}$   $\Gamma_2/\Gamma$

<u>VALUE</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●			
0.16±0.10	BATINIC	95	DPWA $\pi N \rightarrow N\pi, N\eta$

$(\Gamma_i\Gamma_f)^{1/2}/\Gamma_{\text{total}}$  in  $N\pi \rightarrow N(1710) \rightarrow N\eta$   $(\Gamma_1\Gamma_2)^{1/2}/\Gamma$

<u>VALUE</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●			
0.22	BAKER	79	DPWA $\pi^- p \rightarrow n\eta$
+0.383	FELTESSE	75	DPWA Soln A; see BAKER 79

$(\Gamma_i \Gamma_f)^{1/2} / \Gamma_{\text{total}}$ in $N\pi \rightarrow N(1710) \rightarrow \Lambda K$				$(\Gamma_1 \Gamma_3)^{1/2} / \Gamma$
VALUE	DOCUMENT ID	TECN	COMMENT	
<b>+0.12 to +0.18 OUR ESTIMATE</b>				
+0.16	BELL	83	DPWA	$\pi^- p \rightarrow \Lambda K^0$
+0.14	SAXON	80	DPWA	$\pi^- p \rightarrow \Lambda K^0$
• • • We do not use the following data for averages, fits, limits, etc. • • •				
-0.12	7 BAKER	78	DPWA	See SAXON 80
-0.05 ± 0.03	2 BAKER	77	IPWA	$\pi^- p \rightarrow \Lambda K^0$
-0.10	2 BAKER	77	DPWA	$\pi^- p \rightarrow \Lambda K^0$
0.10	KNASEL	75	DPWA	$\pi^- p \rightarrow \Lambda K^0$

$(\Gamma_i \Gamma_f)^{1/2} / \Gamma_{\text{total}}$ in $N\pi \rightarrow N(1710) \rightarrow \Sigma K$				$(\Gamma_1 \Gamma_4)^{1/2} / \Gamma$
VALUE	DOCUMENT ID	TECN	COMMENT	
• • • We do not use the following data for averages, fits, limits, etc. • • •				
-0.034	LIVANOS	80	DPWA	$\pi p \rightarrow \Sigma K$
0.075 to 0.203	8 DEANS	75	DPWA	$\pi N \rightarrow \Sigma K$

Note: Signs of couplings from  $\pi N \rightarrow N\pi\pi$  analyses were changed in the 1986 edition to agree with the baryon-first convention; the overall phase ambiguity is resolved by choosing a negative sign for the  $\Delta(1620) S_{31}$  coupling to  $\Delta(1232)\pi$ .

$(\Gamma_i \Gamma_f)^{1/2} / \Gamma_{\text{total}}$ in $N\pi \rightarrow N(1710) \rightarrow \Delta(1232)\pi$ , <i>P-wave</i>				$(\Gamma_1 \Gamma_7)^{1/2} / \Gamma$
VALUE	DOCUMENT ID	TECN	COMMENT	
<b>±0.16 to ±0.22 OUR ESTIMATE</b>				
-0.21 ± 0.04	MANLEY	92	IPWA	$\pi N \rightarrow \pi N$ & $N\pi\pi$
-0.17	3 LONGACRE	77	IPWA	$\pi N \rightarrow N\pi\pi$
+0.20	4 LONGACRE	75	IPWA	$\pi N \rightarrow N\pi\pi$

$(\Gamma_i \Gamma_f)^{1/2} / \Gamma_{\text{total}}$ in $N\pi \rightarrow N(1710) \rightarrow N\rho$ , <i>S=1/2, P-wave</i>				$(\Gamma_1 \Gamma_9)^{1/2} / \Gamma$
VALUE	DOCUMENT ID	TECN	COMMENT	
<b>±0.09 to ±0.19 OUR ESTIMATE</b>				
+0.05 ± 0.06	MANLEY	92	IPWA	$\pi N \rightarrow \pi N$ & $N\pi\pi$
+0.19	3 LONGACRE	77	IPWA	$\pi N \rightarrow N\pi\pi$
-0.20	4 LONGACRE	75	IPWA	$\pi N \rightarrow N\pi\pi$

$(\Gamma_i \Gamma_f)^{1/2} / \Gamma_{\text{total}}$ in $N\pi \rightarrow N(1710) \rightarrow N\rho$ , <i>S=3/2, P-wave</i>				$(\Gamma_1 \Gamma_{10})^{1/2} / \Gamma$
VALUE	DOCUMENT ID	TECN	COMMENT	
+0.31	3 LONGACRE	77	IPWA	$\pi N \rightarrow N\pi\pi$

$(\Gamma_i \Gamma_f)^{1/2} / \Gamma_{\text{total}}$ in $N\pi \rightarrow N(1710) \rightarrow N(\pi\pi)_{S=0}^{I=0}$				$(\Gamma_1 \Gamma_{11})^{1/2} / \Gamma$
VALUE	DOCUMENT ID	TECN	COMMENT	
<b>±0.14 to ±0.22 OUR ESTIMATE</b>				
+0.04 ± 0.05	MANLEY	92	IPWA	$\pi N \rightarrow \pi N$ & $N\pi\pi$
-0.26	3 LONGACRE	77	IPWA	$\pi N \rightarrow N\pi\pi$
-0.28	4 LONGACRE	75	IPWA	$\pi N \rightarrow N\pi\pi$

**$N(1710)$  PHOTON DECAY AMPLITUDES** **$N(1710) \rightarrow p\gamma$ , helicity-1/2 amplitude  $A_{1/2}$** 

<u>VALUE (GeV<sup>-1/2</sup>)</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
<b>+0.009±0.022 OUR ESTIMATE</b>			
0.007±0.015	ARNDT	96	IPWA $\gamma N \rightarrow \pi N$
0.006±0.018	CRAWFORD	83	IPWA $\gamma N \rightarrow \pi N$
0.028±0.009	AWAJI	81	DPWA $\gamma N \rightarrow \pi N$
-0.009±0.006	ARAI	80	DPWA $\gamma N \rightarrow \pi N$ (fit 1)
-0.012±0.005	ARAI	80	DPWA $\gamma N \rightarrow \pi N$ (fit 2)
0.015±0.025	CRAWFORD	80	DPWA $\gamma N \rightarrow \pi N$
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●			
-0.037±0.002	LI	93	IPWA $\gamma N \rightarrow \pi N$
+0.001±0.039	BARBOUR	78	DPWA $\gamma N \rightarrow \pi N$
+0.053±0.019	FELLER	76	DPWA $\gamma N \rightarrow \pi N$

 **$N(1710) \rightarrow n\gamma$ , helicity-1/2 amplitude  $A_{1/2}$** 

<u>VALUE (GeV<sup>-1/2</sup>)</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
<b>-0.002±0.014 OUR ESTIMATE</b>			
-0.002±0.015	ARNDT	96	IPWA $\gamma N \rightarrow \pi N$
0.000±0.018	AWAJI	81	DPWA $\gamma N \rightarrow \pi N$
-0.001±0.003	FUJII	81	DPWA $\gamma N \rightarrow \pi N$
0.005±0.013	ARAI	80	DPWA $\gamma N \rightarrow \pi N$ (fit 1)
0.011±0.021	ARAI	80	DPWA $\gamma N \rightarrow \pi N$ (fit 2)
-0.017±0.020	CRAWFORD	80	DPWA $\gamma N \rightarrow \pi N$
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●			
0.052±0.003	LI	93	IPWA $\gamma N \rightarrow \pi N$
-0.028±0.045	BARBOUR	78	DPWA $\gamma N \rightarrow \pi N$

 **$N(1710) \quad \gamma p \rightarrow \Lambda K^+$  AMPLITUDES** **$(\Gamma_i \Gamma_f)^{1/2} / \Gamma_{\text{total}}$  in  $p\gamma \rightarrow N(1710) \rightarrow \Lambda K^+$  ( $M_{1-}$  amplitude)**

<u>VALUE (units 10<sup>-3</sup>)</u>	<u>DOCUMENT ID</u>	<u>TECN</u>
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●		
-10.6 ±0.4	WORKMAN	90 DPWA
-7.21	TANABE	89 DPWA

 **$p\gamma \rightarrow N(1710) \rightarrow \Lambda K^+$  phase angle  $\theta$  ( $M_{1-}$  amplitude)**

<u>VALUE (degrees)</u>	<u>DOCUMENT ID</u>	<u>TECN</u>
● ● ● We do not use the following data for averages, fits, limits, etc. ● ● ●		
215 ±3	WORKMAN	90 DPWA
176.3	TANABE	89 DPWA

## N(1710) FOOTNOTES

- <sup>1</sup> BATINIC 95 finds a second state with a 6 MeV mass difference.
- <sup>2</sup> The two BAKER 77 entries are from an IPWA using the Barrelet-zero method and from a conventional energy-dependent analysis.
- <sup>3</sup> LONGACRE 77 pole positions are from a search for poles in the unitarized T-matrix; the first (second) value uses, in addition to  $\pi N \rightarrow N\pi\pi$  data, elastic amplitudes from a Saclay (CERN) partial-wave analysis. The other LONGACRE 77 values are from eyeball fits with Breit-Wigner circles to the T-matrix amplitudes.
- <sup>4</sup> From method II of LONGACRE 75: eyeball fits with Breit-Wigner circles to the T-matrix amplitudes.
- <sup>5</sup> See HOEHLER 93 for a detailed discussion of the evidence for and the pole parameters of  $N$  and  $\Delta$  resonances as determined from Argand diagrams of  $\pi N$  elastic partial-wave amplitudes and from plots of the speeds with which the amplitudes traverse the diagrams.
- <sup>6</sup> LONGACRE 78 values are from a search for poles in the unitarized T-matrix. The first (second) value uses, in addition to  $\pi N \rightarrow N\pi\pi$  data, elastic amplitudes from a Saclay (CERN) partial-wave analysis.
- <sup>7</sup> The overall phase of BAKER 78 couplings has been changed to agree with previous conventions.
- <sup>8</sup> The range given for DEANS 75 is from the four best solutions.

## N(1710) REFERENCES

For early references, see Physics Letters **111B** 70 (1982).

ARNDT	96	PR C53 430	+Strakovsky, Workman	(VPI)
ARNDT	95	PR C52 2120	+Strakovsky, Workman, Pavan	(VPI, BRCO)
BATINIC	95	PR C51 2310	+Slaus, Svarc, Nefkens	(BOSK, UCLA)
HOEHLER	93	$\pi N$ Newsletter 9 1		(KARL)
LI	93	PR C47 2759	+Arndt, Roper, Workman	(VPI)
MANLEY	92	PR D45 4002	+Saleski	(KENT) IJP
Also	84	PR D30 904	Manley, Arndt, Goradia, Teplitz	(VPI)
ARNDT	91	PR D43 2131	+Li, Roper, Workman, Ford	(VPI, TELE) IJP
CUTKOSKY	90	PR D42 235	+Wang	(CMU)
WORKMAN	90	PR C42 781		(VPI)
TANABE	89	PR C39 741	+Kohno, Bennhold	(MANZ)
Also	89	NC 102A 193	Kohno, Tanabe, Bennhold	(MANZ)
BELL	83	NP B222 389	+Blissett, Broome, Daley, Hart, Lintern+	(RL) IJP
CRAWFORD	83	NP B211 1	+Morton	(GLAS)
PDG	82	PL 111B	Roos, Porter, Aguilar-Benitez+	(HELS, CIT, CERN)
AWAJI	81	Bonn Conf. 352	+Kajikawa	(NAGO)
Also	82	NP B197 365	Fujii, Hayashii, Iwata, Kajikawa+	(NAGO)
FUJII	81	NP B187 53	+Hayashii, Iwata, Kajikawa+	(NAGO, OSAK)
ARAI	80	Toronto Conf. 93		(INUS)
Also	82	NP B194 251	Arai, Fujii	(INUS)
CRAWFORD	80	Toronto Conf. 107		(GLAS)
CUTKOSKY	80	Toronto Conf. 19	+Forsyth, Babcock, Kelly, Hendrick	(CMU, LBL) IJP
Also	79	PR D20 2839	Cutkosky, Forsyth, Hendrick, Kelly	(CMU, LBL) IJP
LIVANOS	80	Toronto Conf. 35	+Baton, Coutures, Kochowski, Neveu	(SACL) IJP
SAXON	80	NP B162 522	+Baker, Bell, Blissett, Bloodworth+	(RHEL, BRIS) IJP
BAKER	79	NP B156 93	+Brown, Clark, Davies, Depagter, Evans+	(RHEL) IJP
HOEHLER	79	PDAT 12-1	+Kaiser, Koch, Pietarinen	(KARLT) IJP
Also	80	Toronto Conf. 3	Koch	(KARLT) IJP
BAKER	78	NP B141 29	+Blissett, Bloodworth, Broome+	(RL, CAVE) IJP
BARBOUR	78	NP B141 253	+Crawford, Parsons	(GLAS)
LONGACRE	78	PR D17 1795	+Lasinski, Rosenfeld, Smadja+	(LBL, SLAC)
BAKER	77	NP B126 365	+Blissett, Bloodworth, Broome, Hart+	(RHEL) IJP
LONGACRE	77	NP B122 493	+Dolbeau	(SACL) IJP
Also	76	NP B108 365	Dolbeau, Triantis, Neveu, Cadiet	(SACL) IJP
FELLER	76	NP B104 219	+Fukushima, Horikawa, Kajikawa+	(NAGO, OSAK) IJP
DEANS	75	NP B96 90	+Mitchell, Montgomery+	(SFLA, ALAH) IJP
FELTESSE	75	NP B93 242	+Ayed, Bareyre, Borgeaud, David+	(SACL) IJP
KNASEL	75	PR D11 1	+Lindquist, Nelson+	(CHIC, WUSL, OSU, ANL) IJP
LONGACRE	75	PL 55B 415	+Rosenfeld, Lasinski, Smadja+	(LBL, SLAC) IJP